



Metapath2vec

Antonio Longa^{1,2}

MobS¹ Lab, Fondazione Bruno Kessler, Trento, Italy
SML² Lab, University of Trento, Italy



Metapath 01

Metapath random walks 02

The model 03



TABLE OF CONTENTS

04 Training
(my laptop not powerful enough 😊)

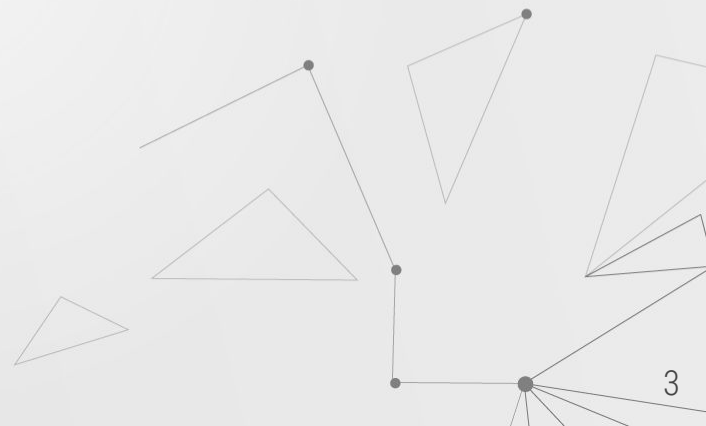
05 Load a pre trained model

06



01 Metapath

So far we saw some **homogeneous** type of graphs:

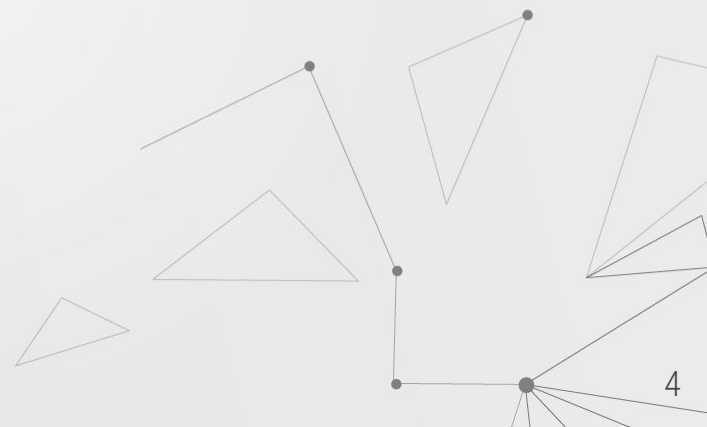
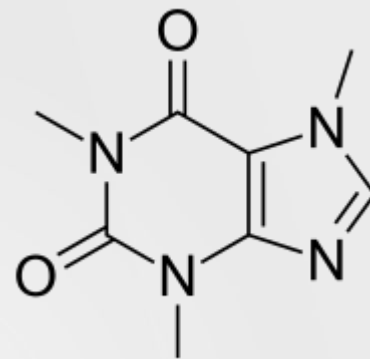




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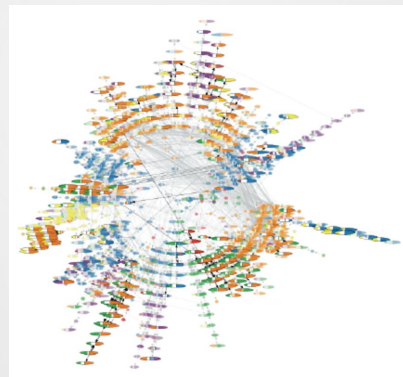
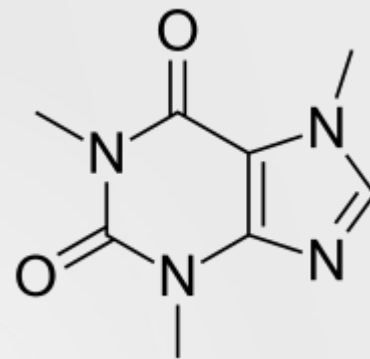
- **Molecules**
- CiteSeer
- Cora



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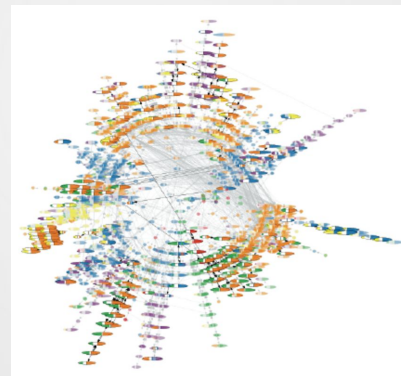
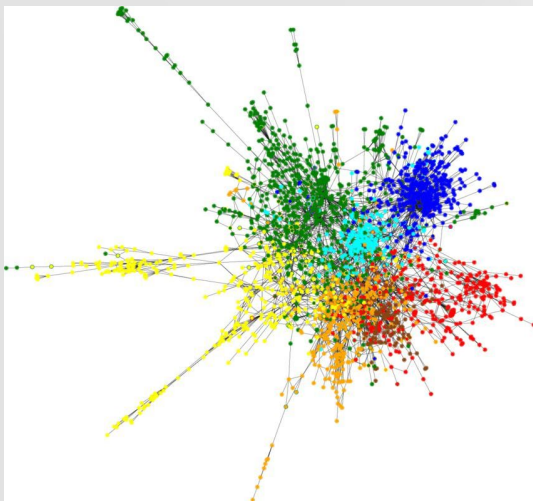
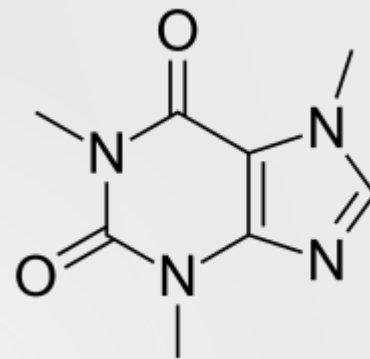
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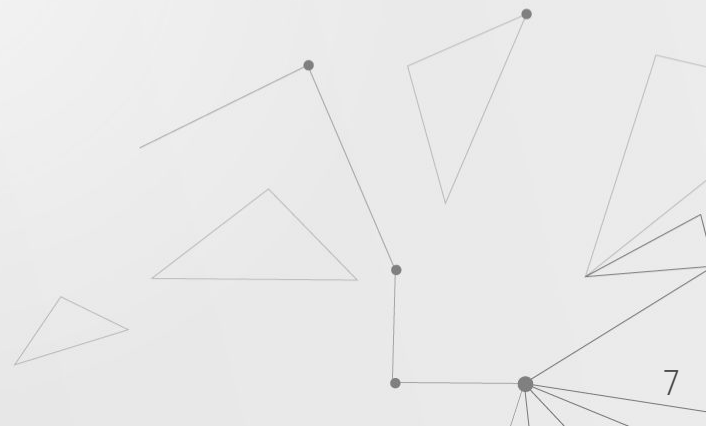
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01 Metapath

What are **heterogeneous** graph?

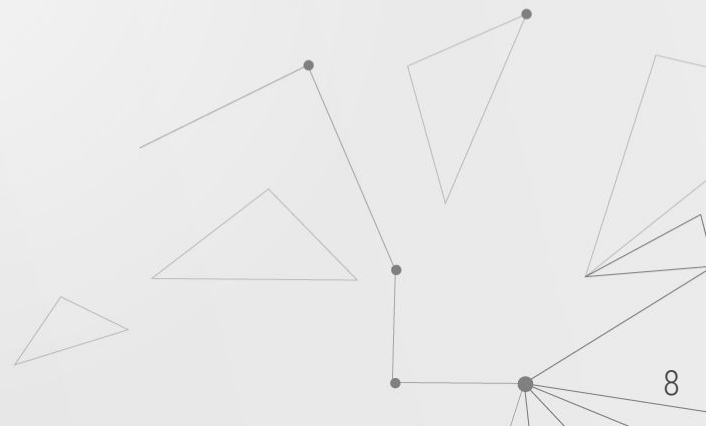




01 Metapath

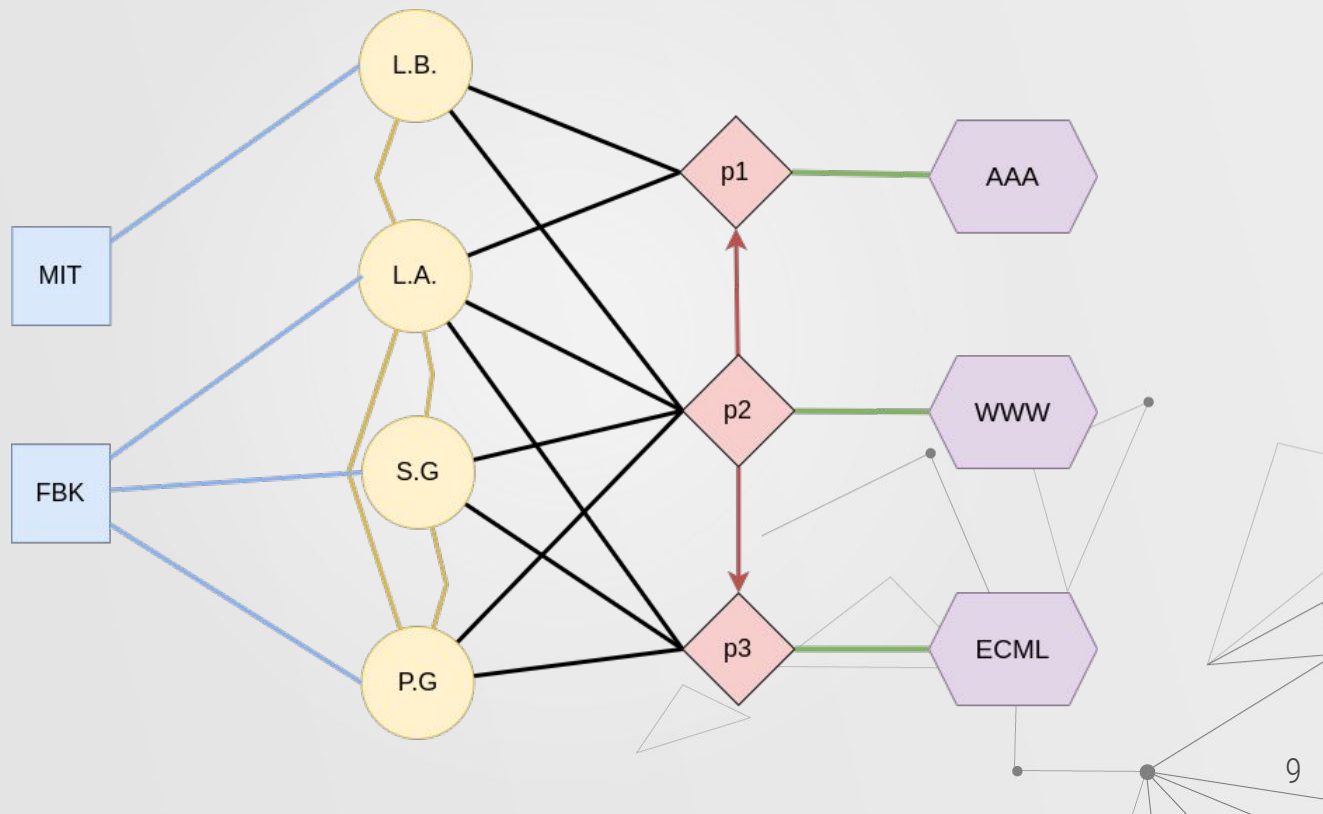
What are **heterogeneous** graph?

An heterogeneous graph is a graph in witch nodes and edges have differents types.



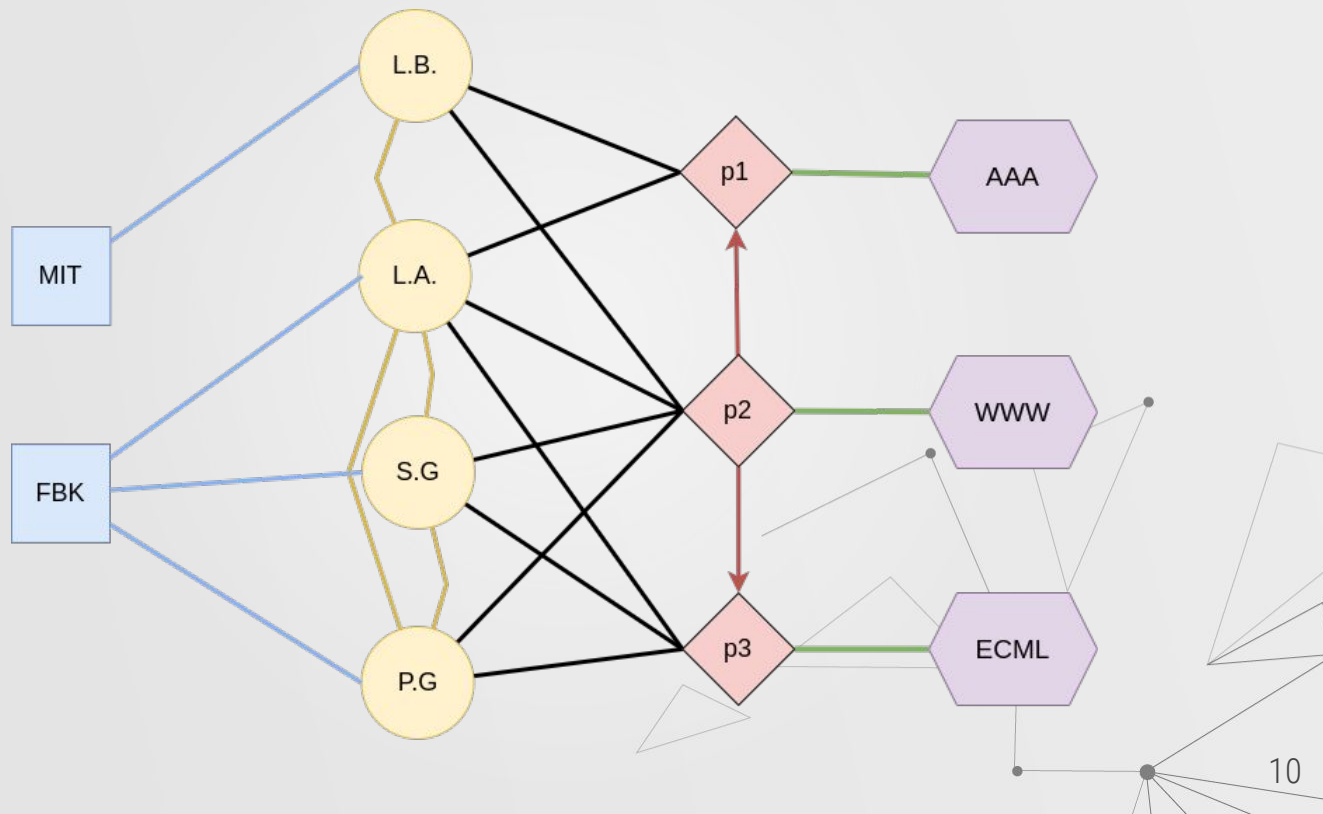
01 Metapath

For instance:



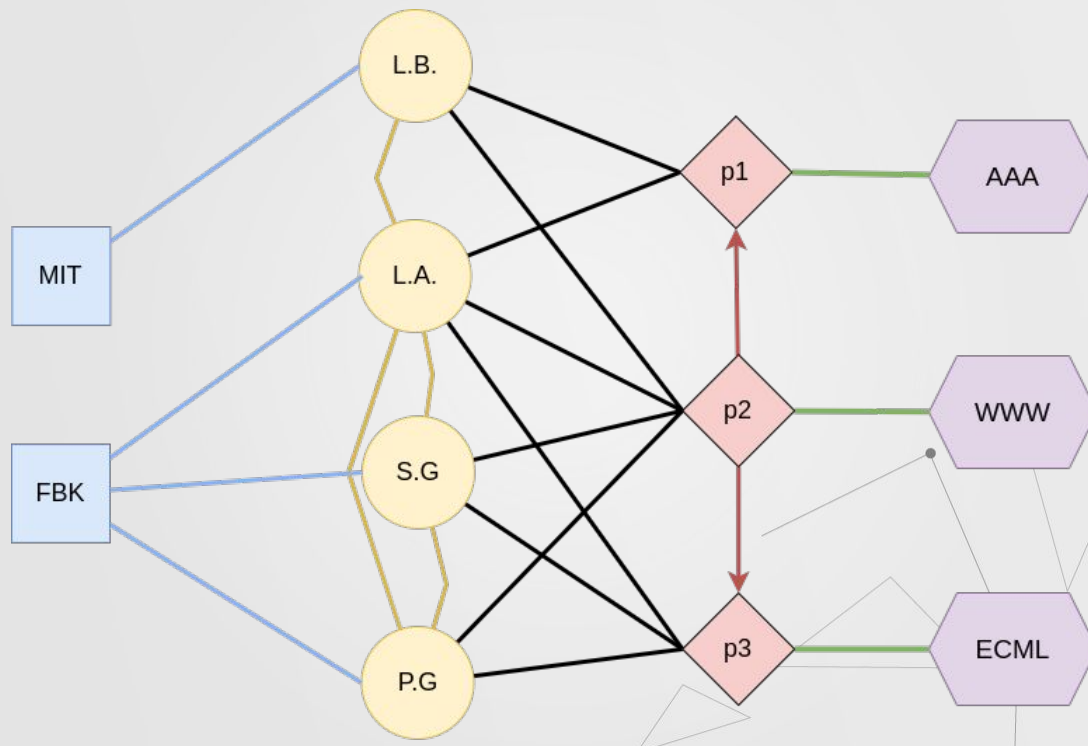
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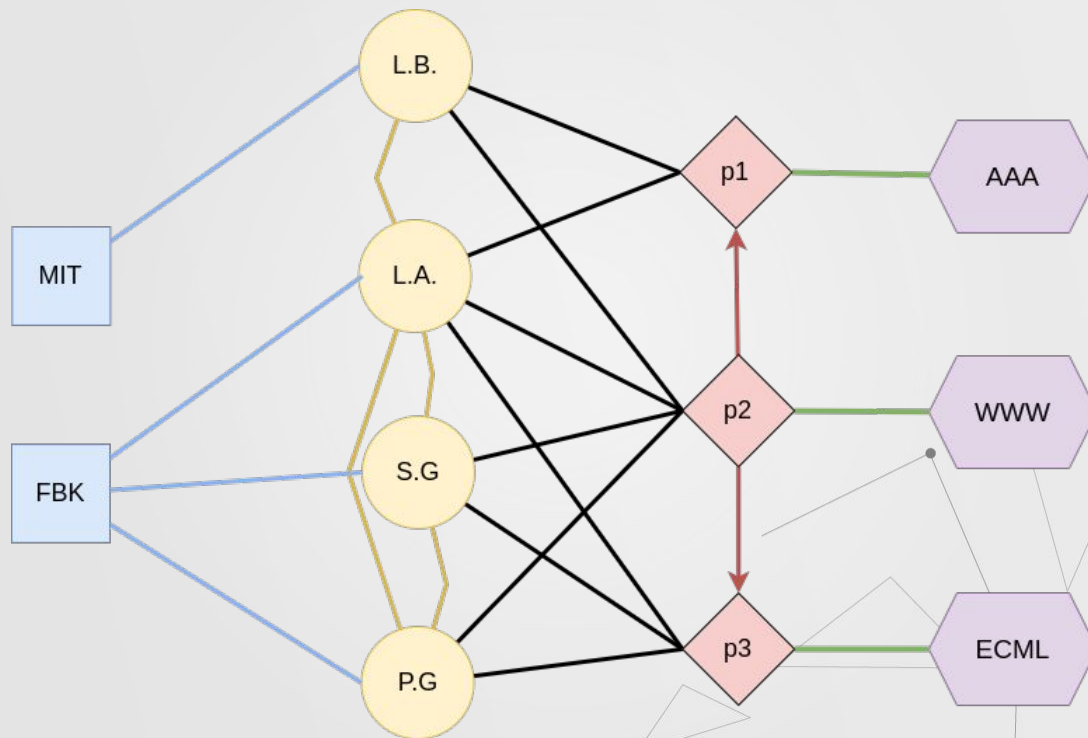
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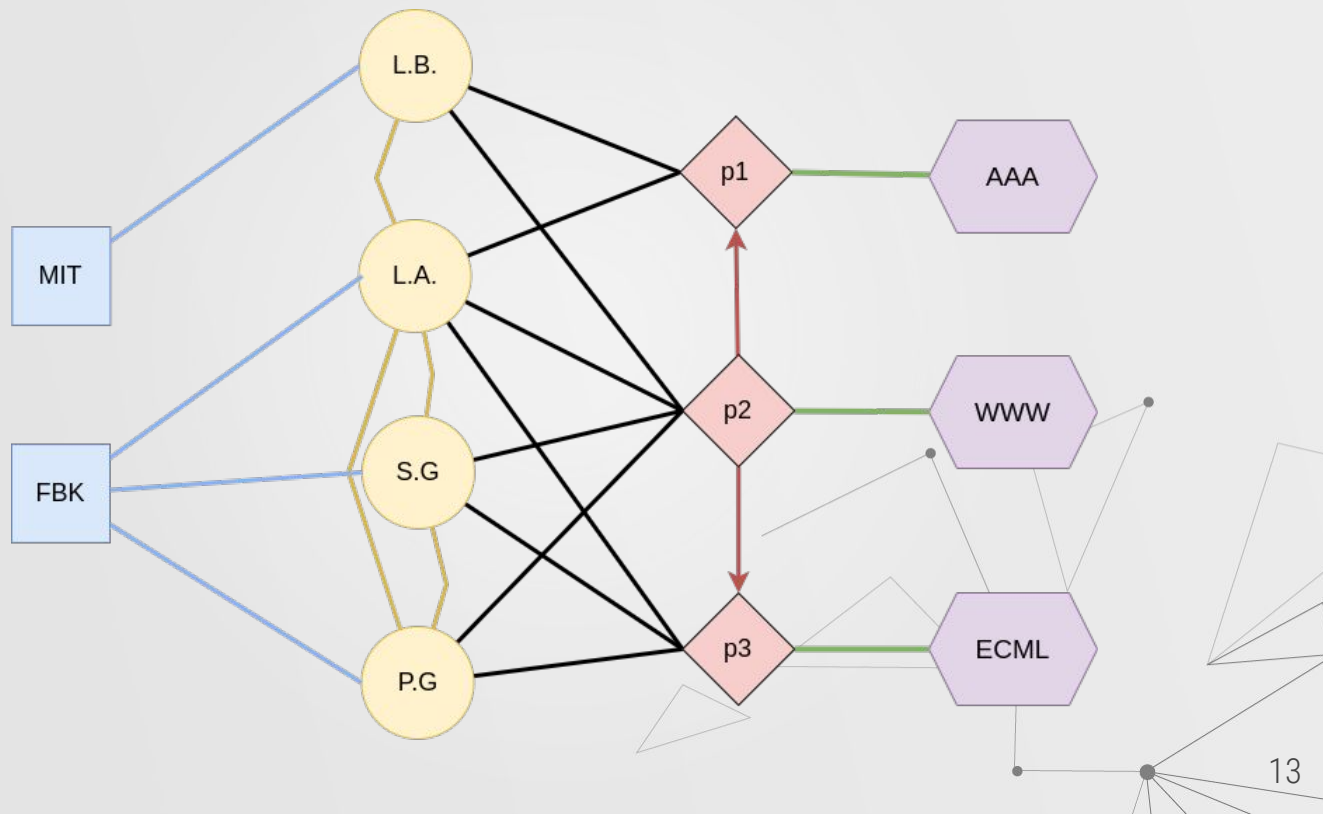
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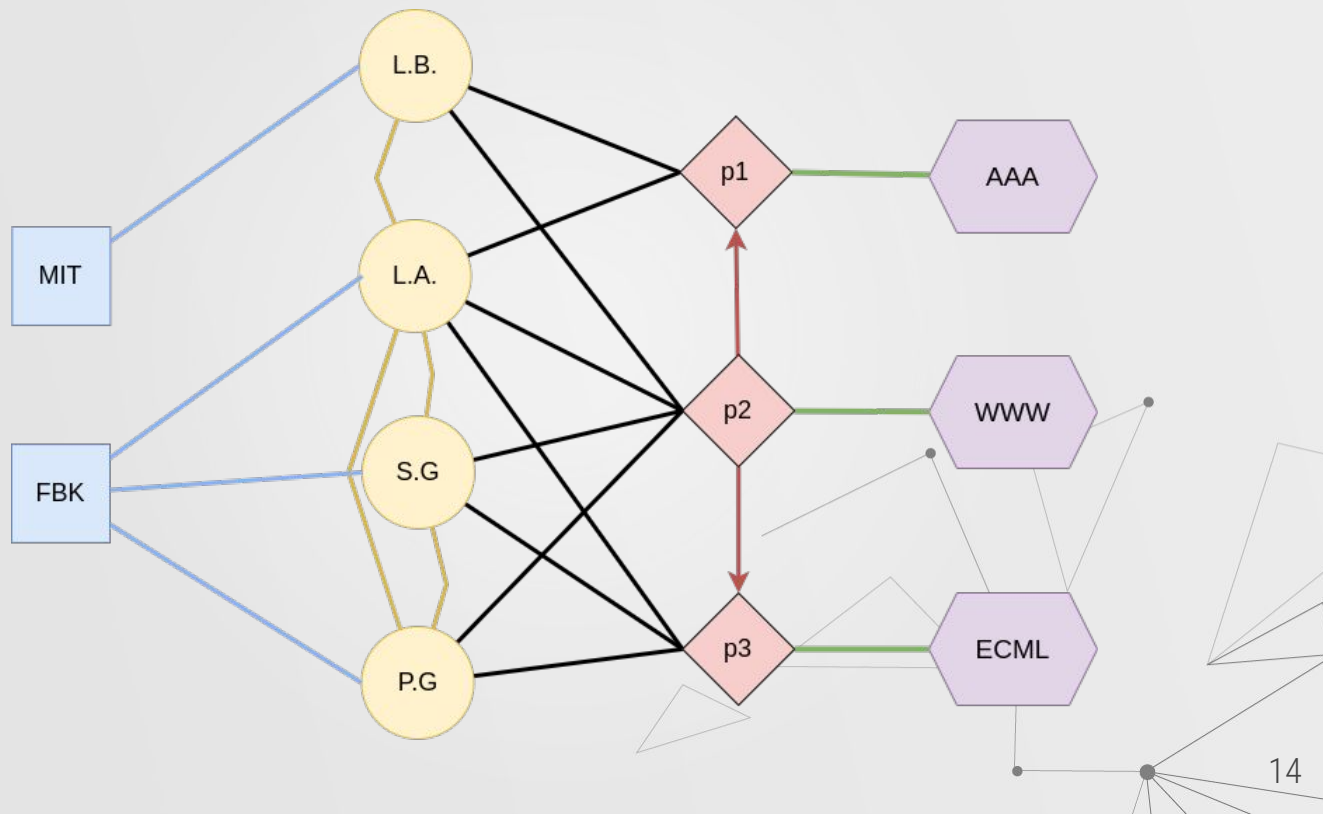
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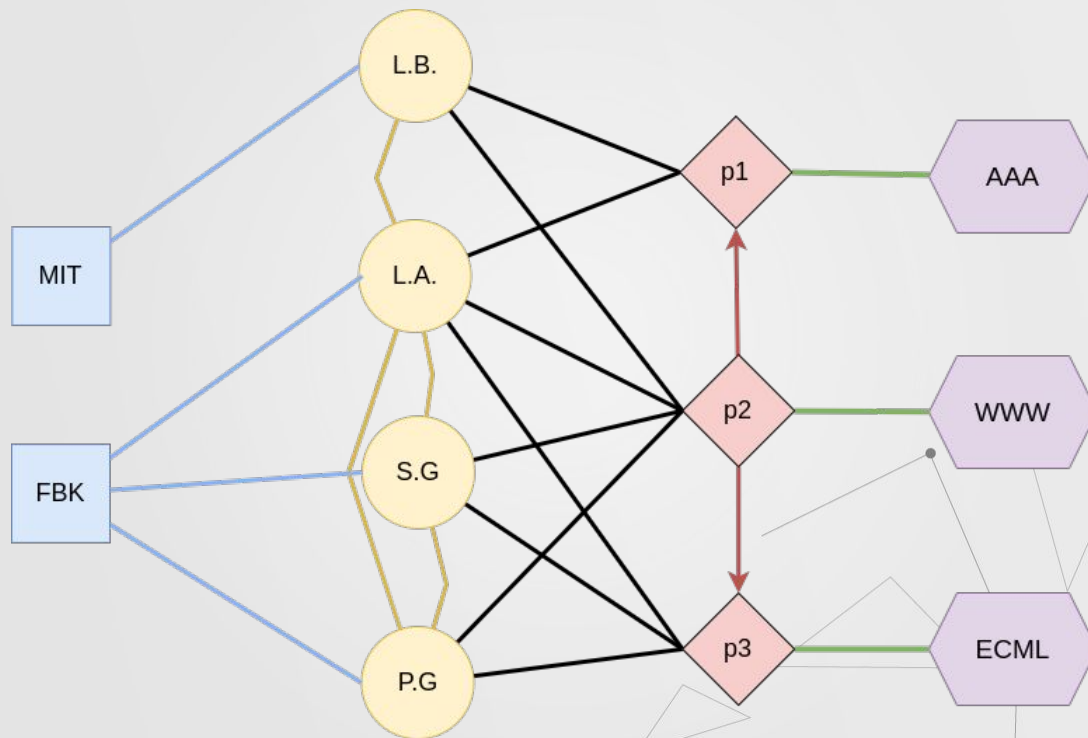
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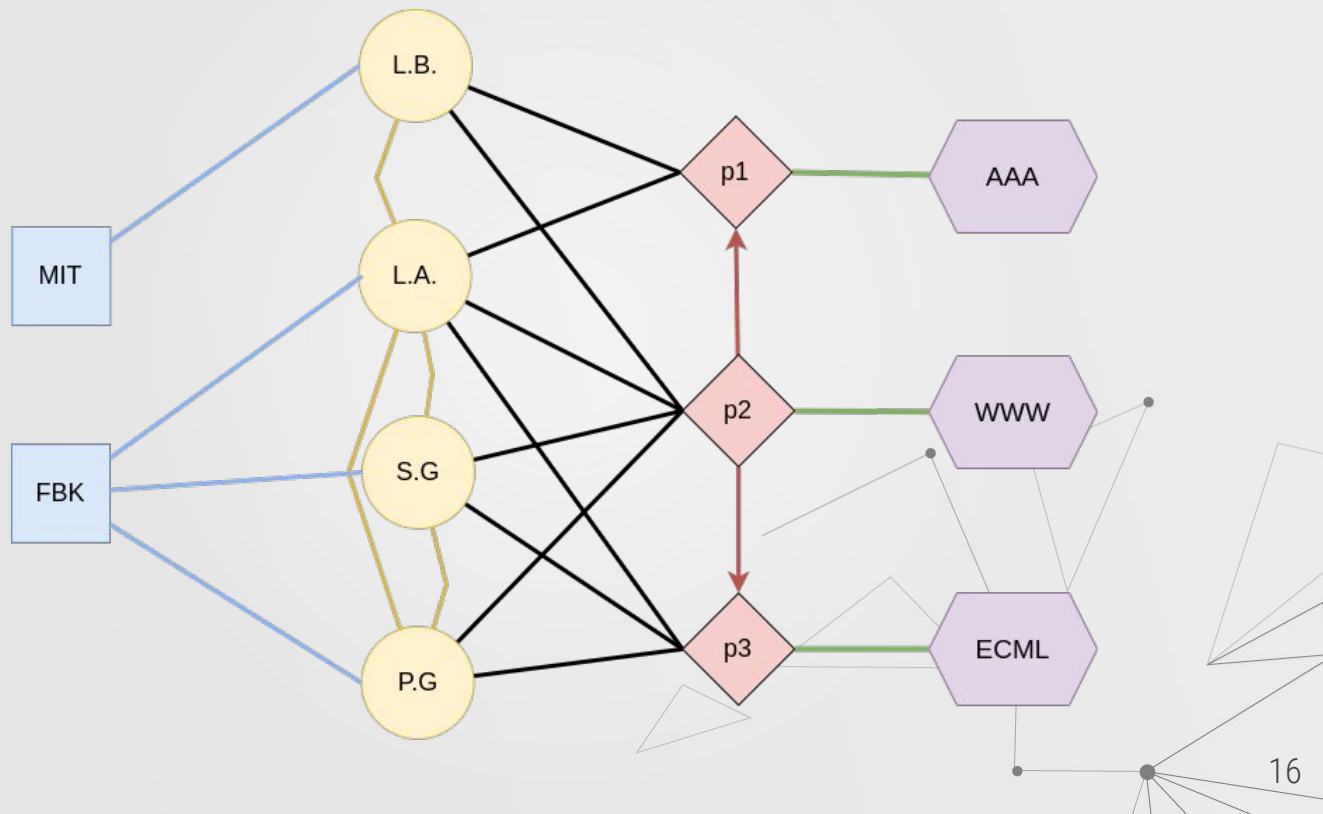
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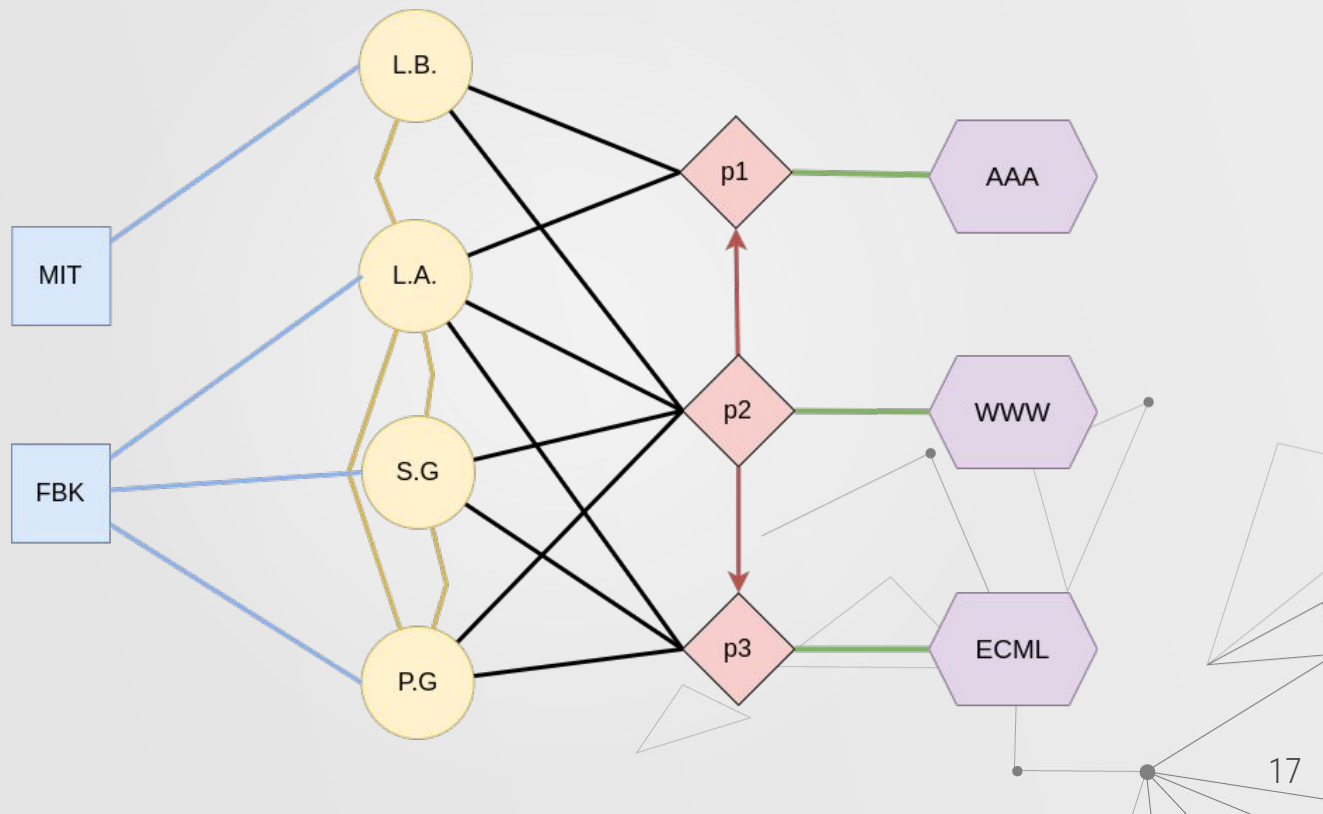
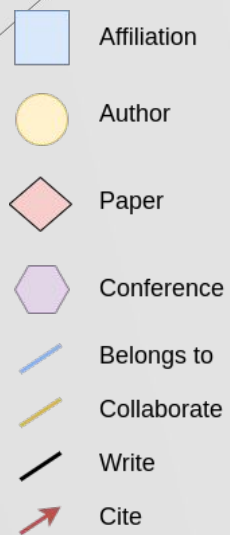
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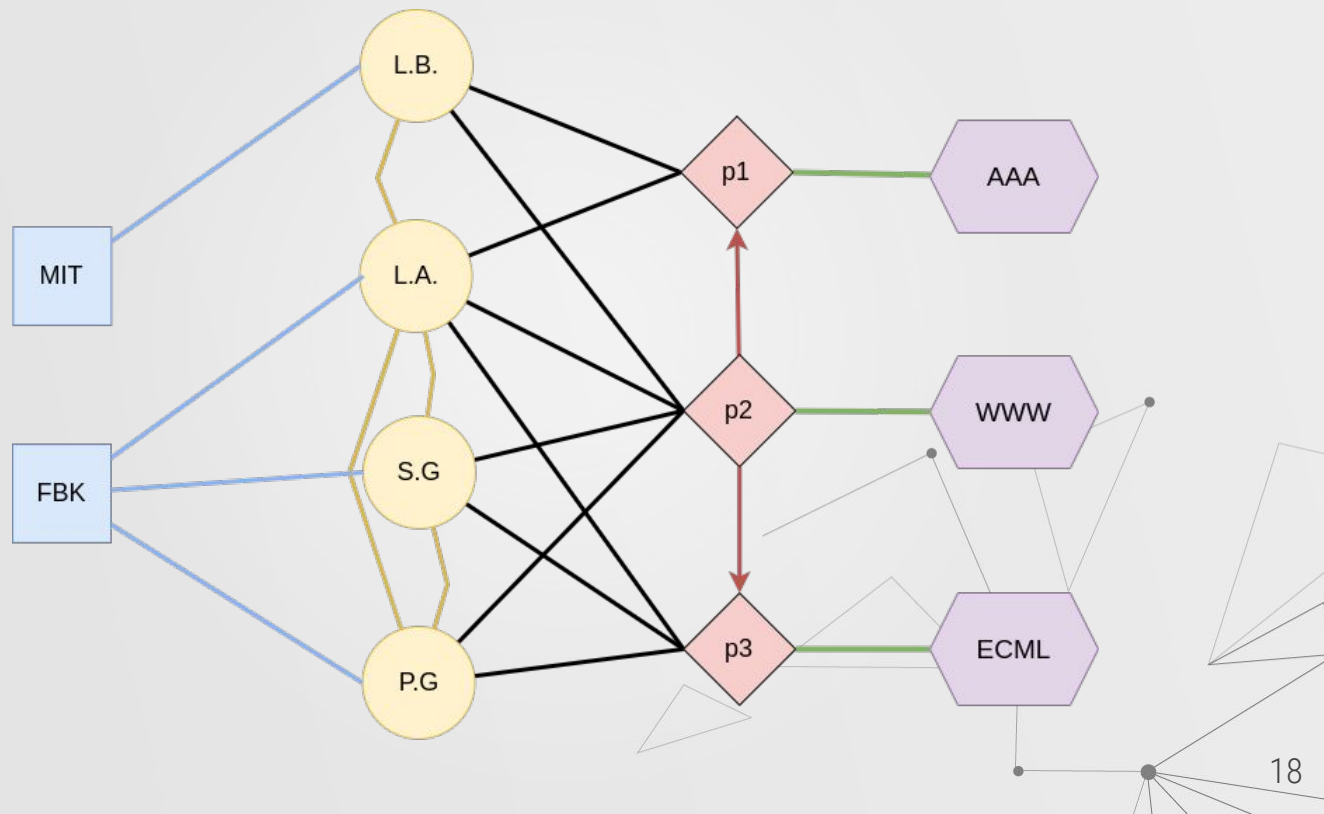
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Def:

A **meta path** in a heterogeneous graphs, is a path following a specific meta path scheme P .



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Def:

A **meta path scheme** P is defined as a path that is denoted in the form of :

$$V_1 \xrightarrow{r_1} V_2 \xrightarrow{r_2} V_3 \xrightarrow{r_3} V_4 \xrightarrow{r_4} \dots V_{l-1} \xrightarrow{r_{l-1}} V_l$$

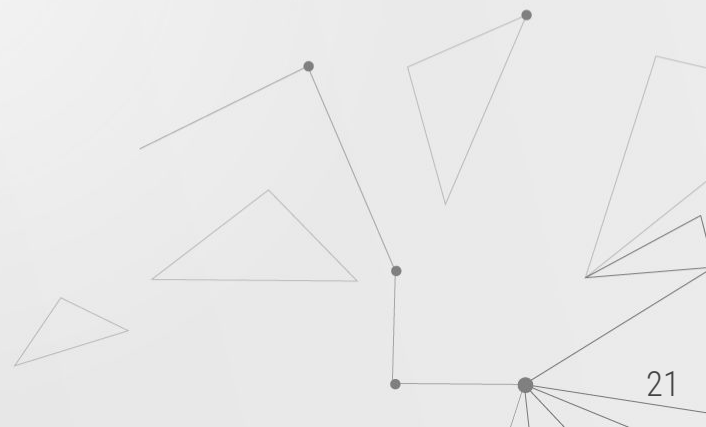
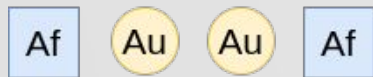
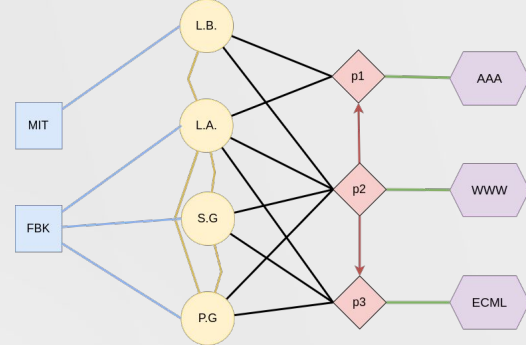
Wherein

$$R = R_1 \cdot R_2 \cdot R_3 \cdot \dots R_{l-1}$$

Defines the composite relations between nodes types V_1 and V_l

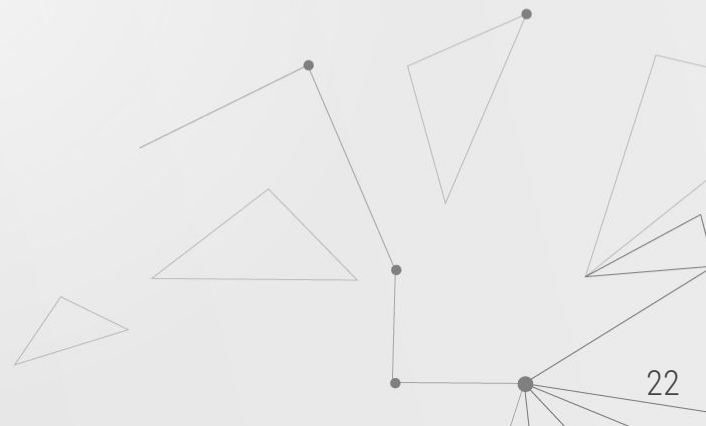
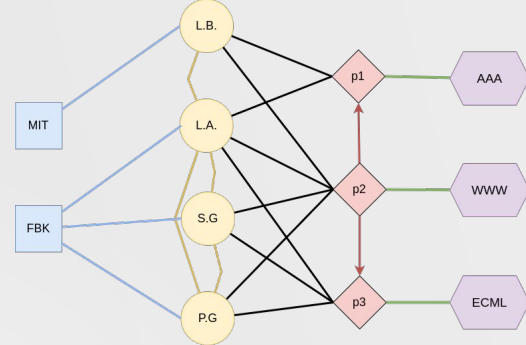
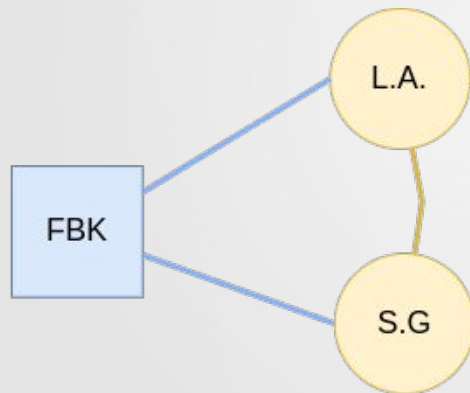
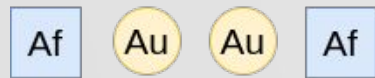
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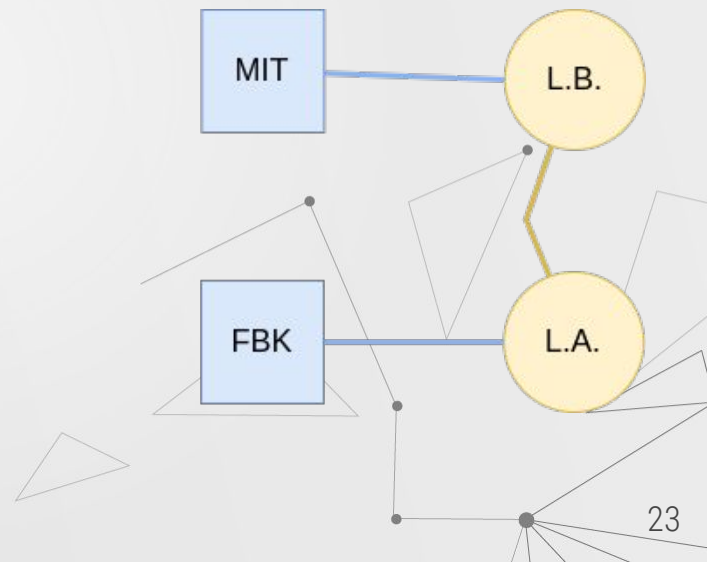
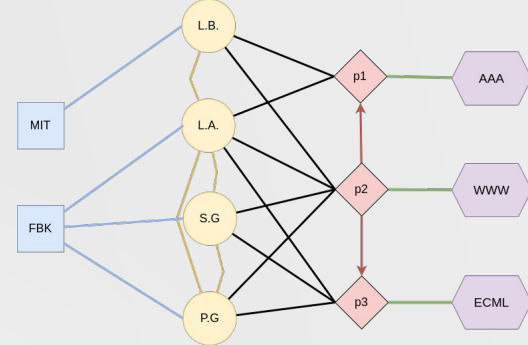
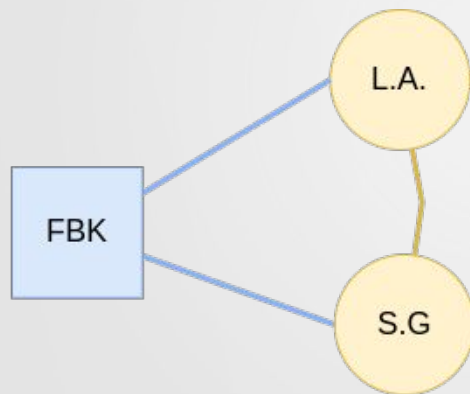
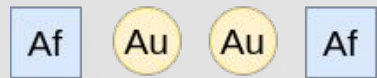
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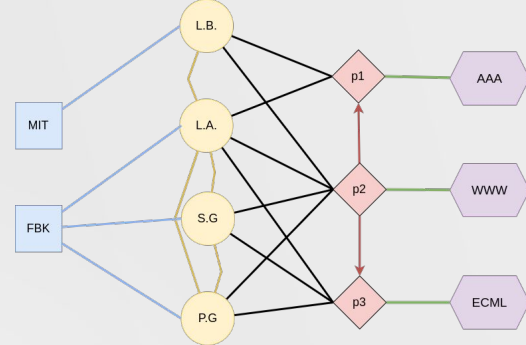
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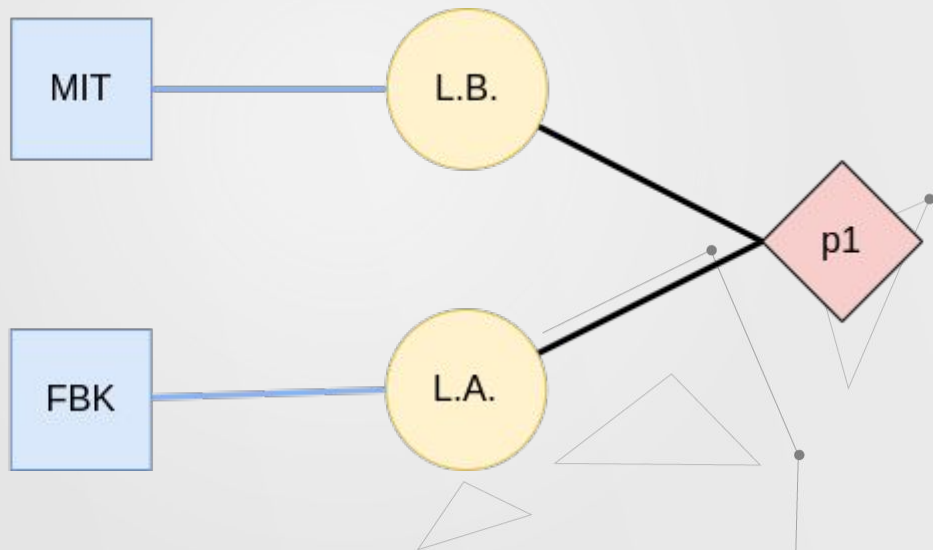
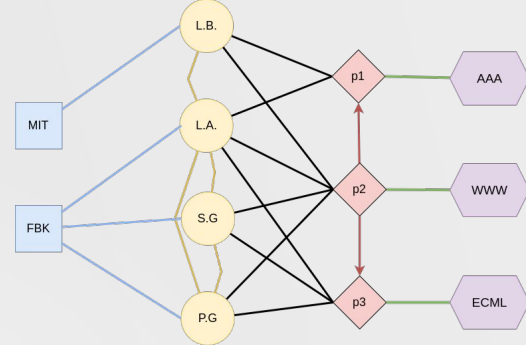
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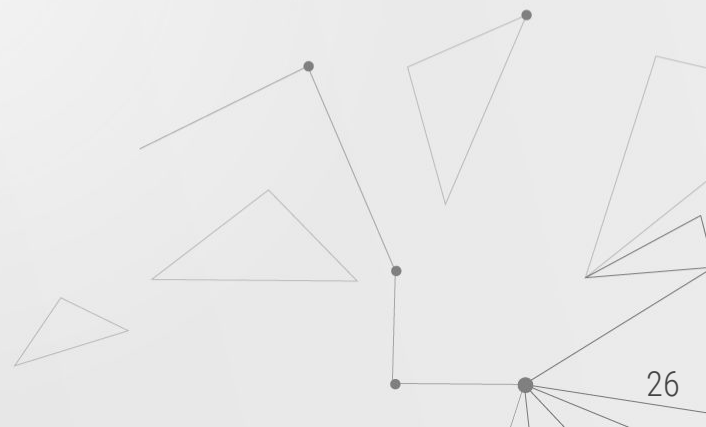


02 Metapath random walks

Def:

Given an heterogeneous network $G = (V, E, T)$ and a meta path scheme P .

The transition probability at step i is defined as follow:





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Given an heterogeneous network $G = (V, E, T)$ and a meta path scheme P .

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$$p(v^{i+1} | v_t^i, \mathcal{P}) = \begin{cases} \frac{1}{|N_{t+1}(v_t^i)|} & (v^{i+1}, v_t^i) \in E, \phi(v^{i+1}) = t+1 \\ 0 & (v^{i+1}, v_t^i) \in E, \phi(v^{i+1}) \neq t+1 \\ 0 & (v^{i+1}, v_t^i) \notin E \end{cases}$$

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Scheme

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Def:

Given an heterogeneous network $G = (V, E, T)$ and a meta path scheme P .

Function that compute the
type of a node

The transition probability at step i is defined as follow:

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Node at time $i+1$

Node at time i
of type t

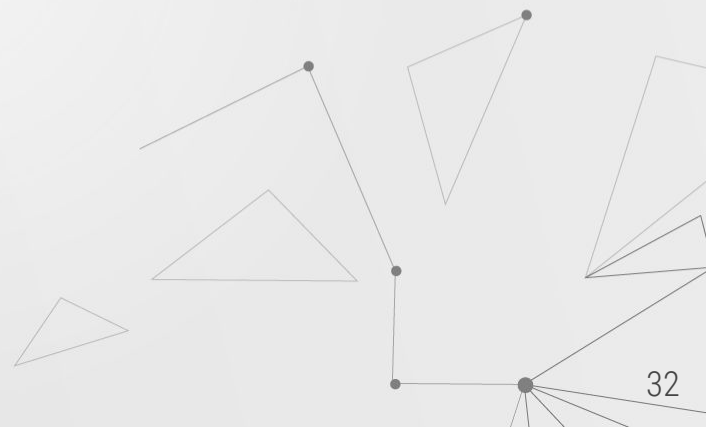
Scheme



03 The model

Metapath2vec

- Given a specific Scheme P

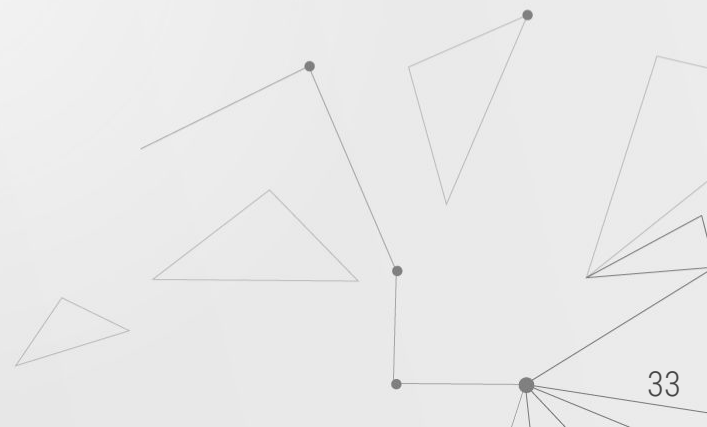




03 The model

Metapath2vec

- Given a specific Scheme P
- Extract random meta path from the input graph





03 The model

Metapath2vec

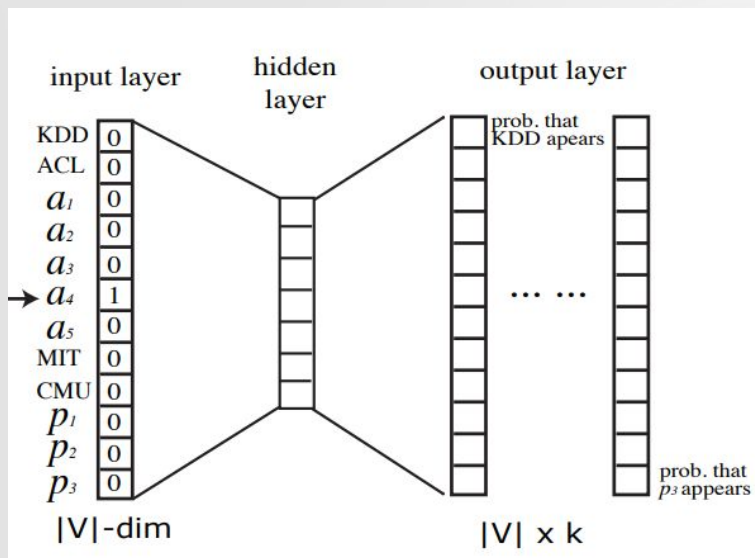
- Given a specific Scheme P
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- Use the skip-gram model



03 The model

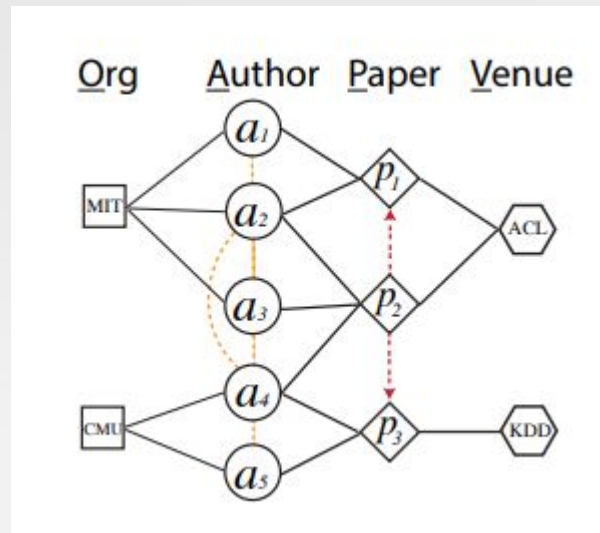
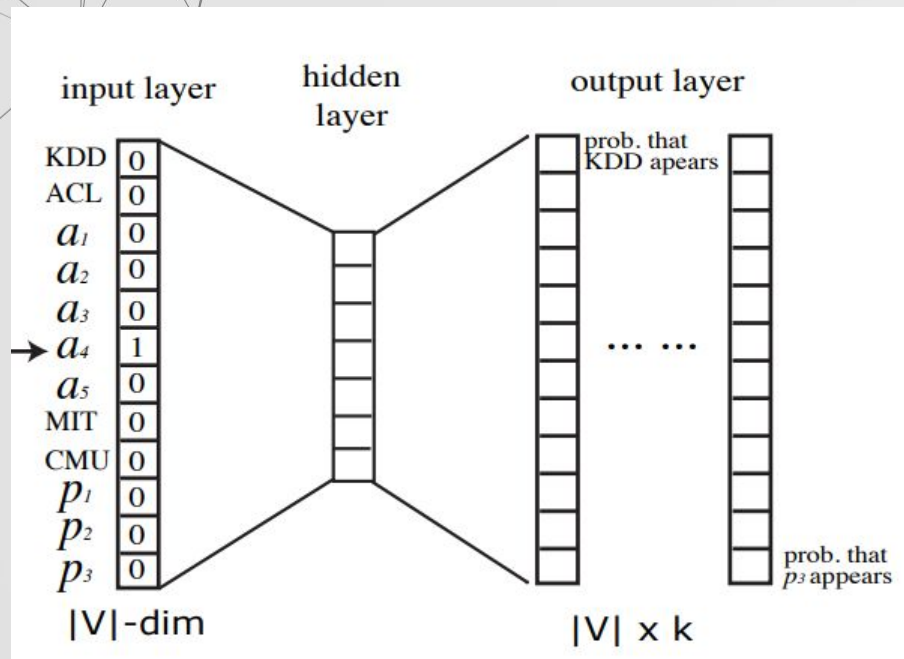
Metapath2vec

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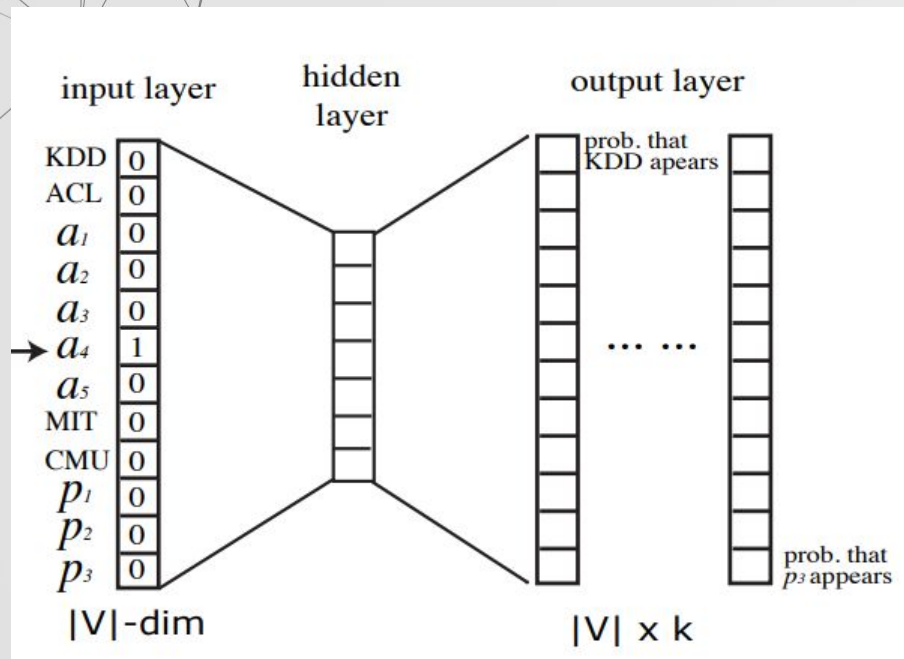
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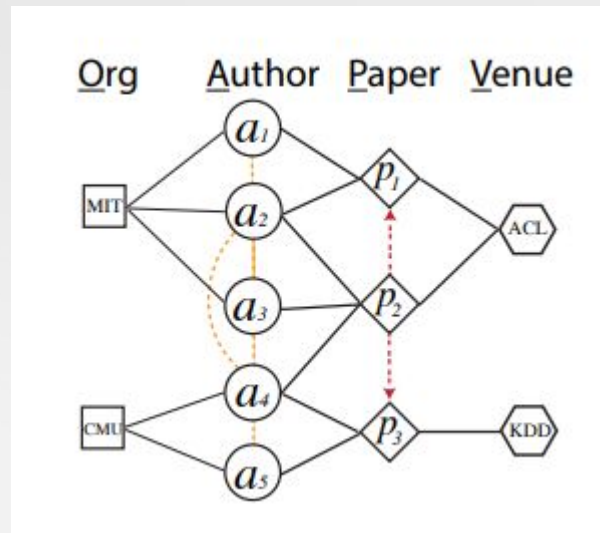


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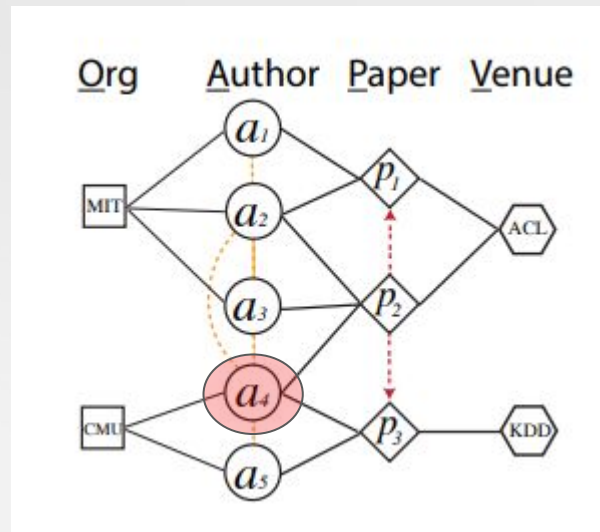
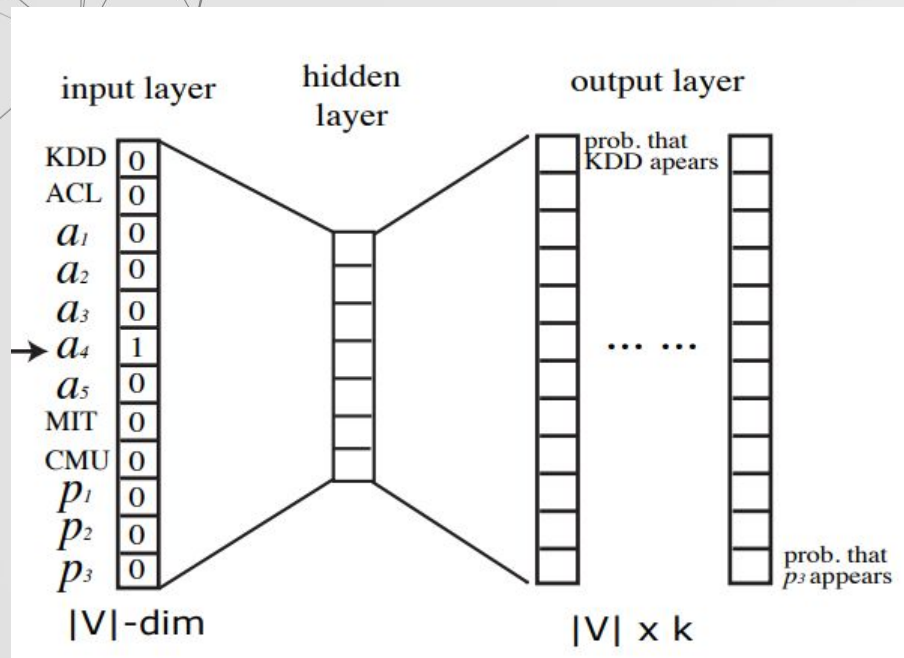


In the case of a_4 , the output layer is a **12x8**, because...



03 The model

Metapath2vec

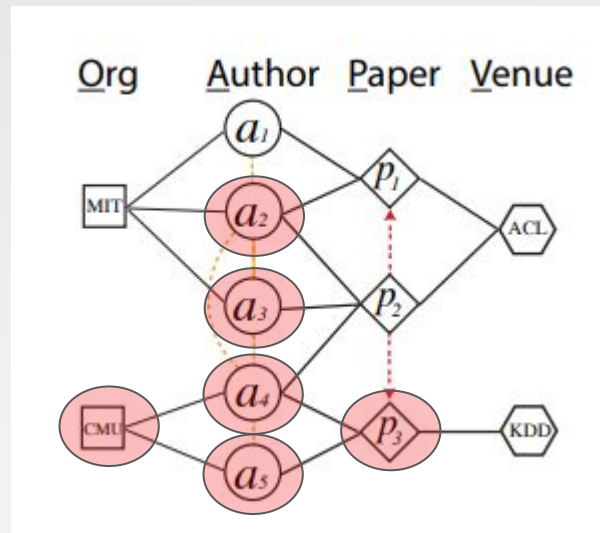
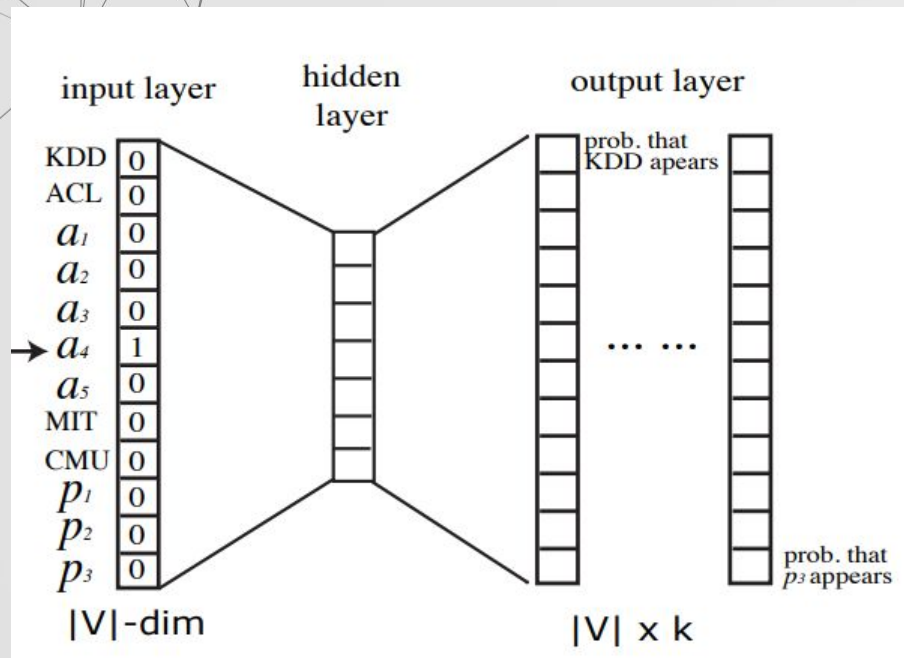


12x0

In the case of a_4 , the output layer is a **12x8**, because...

03 The model

Metapath2vec

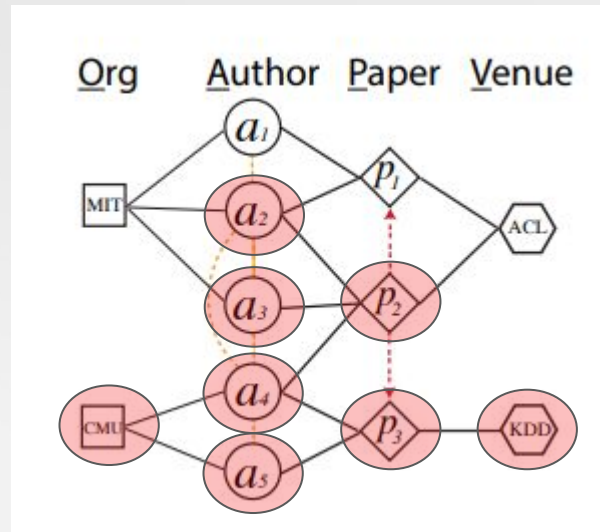
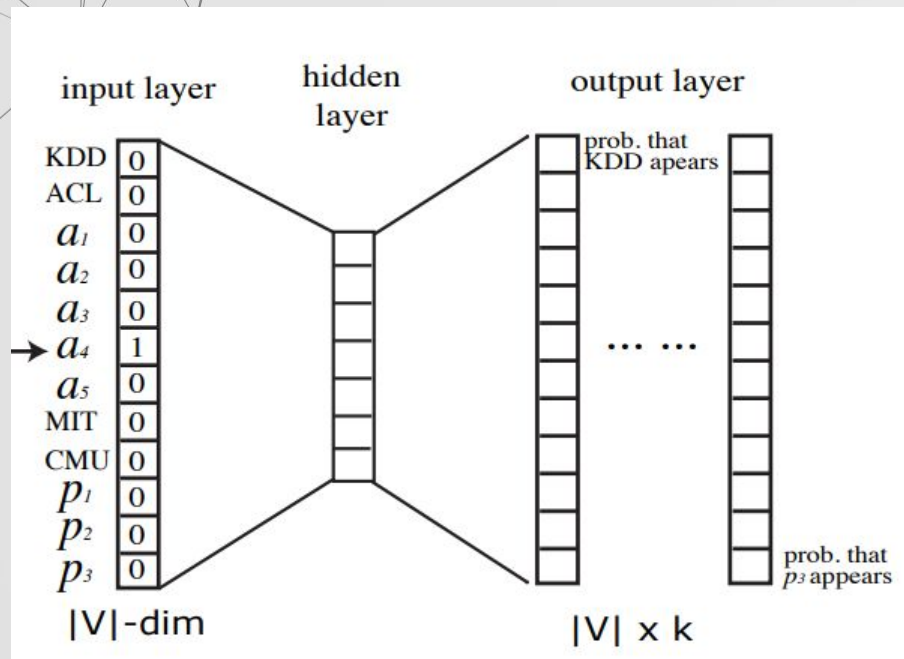


12x5

In the case of a_4 , the output layer is a **12x8**, because...

03 The model

Metapath2vec

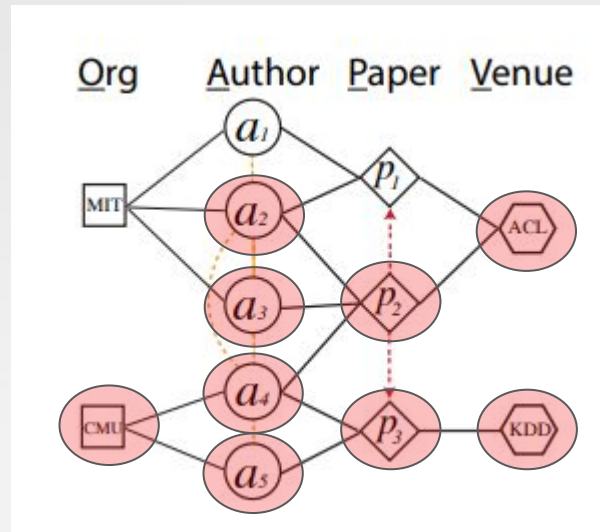
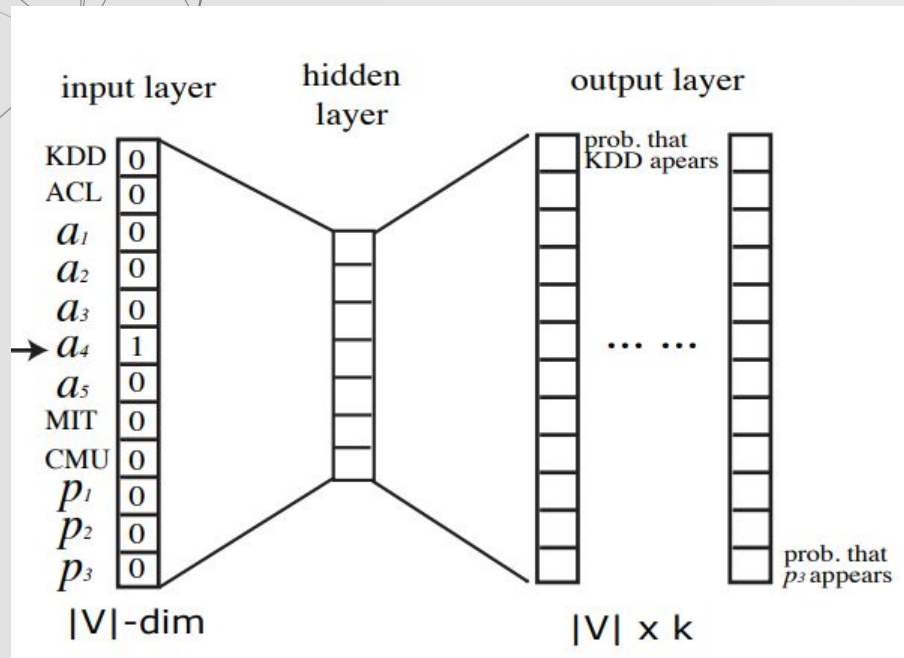


12x7

In the case of a_4 , the output layer is a **12x8**, because...

03 The model

Metapath2vec



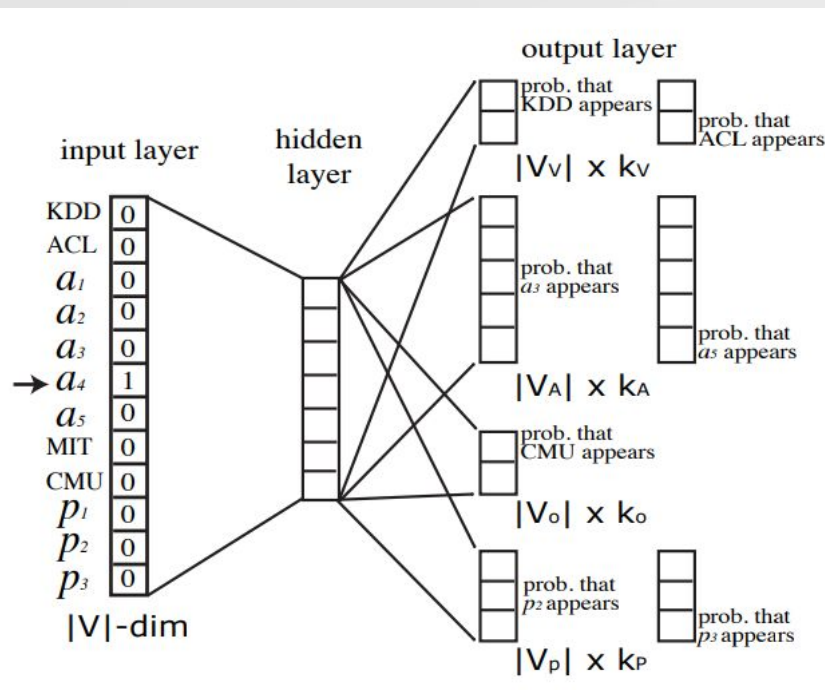
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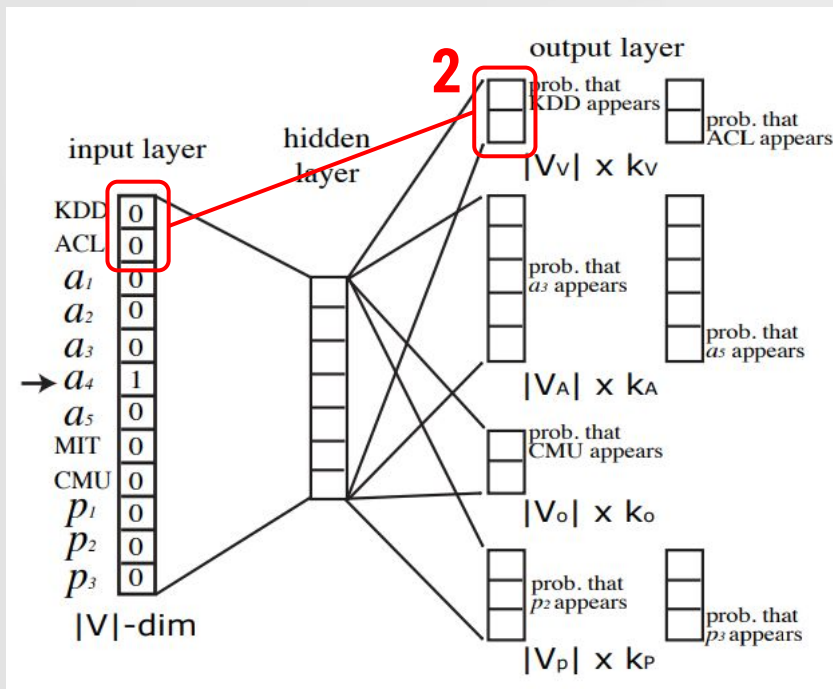
Metapath2vec++



In the case of a_4 , there are 4 output layers, each of them with different size

03 The model

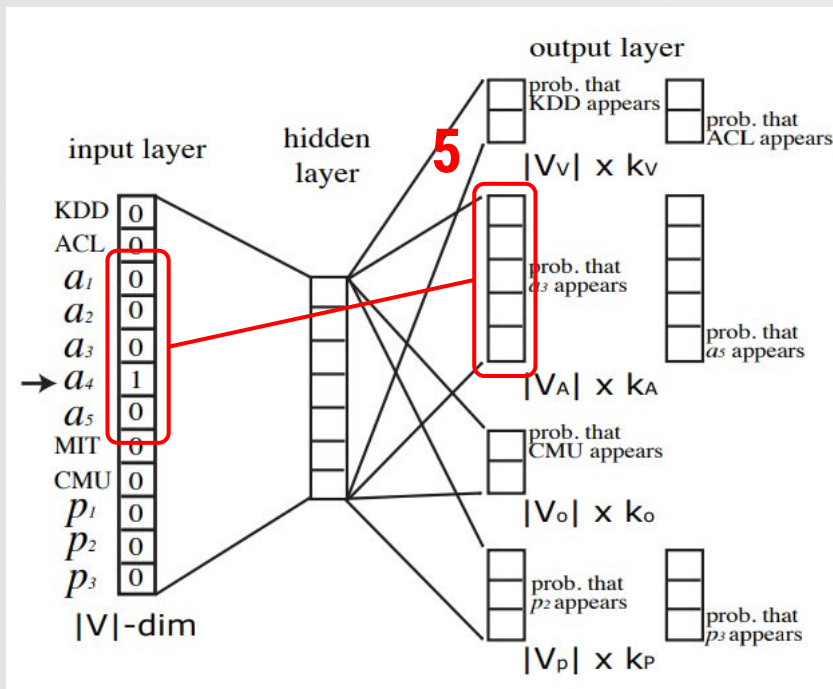
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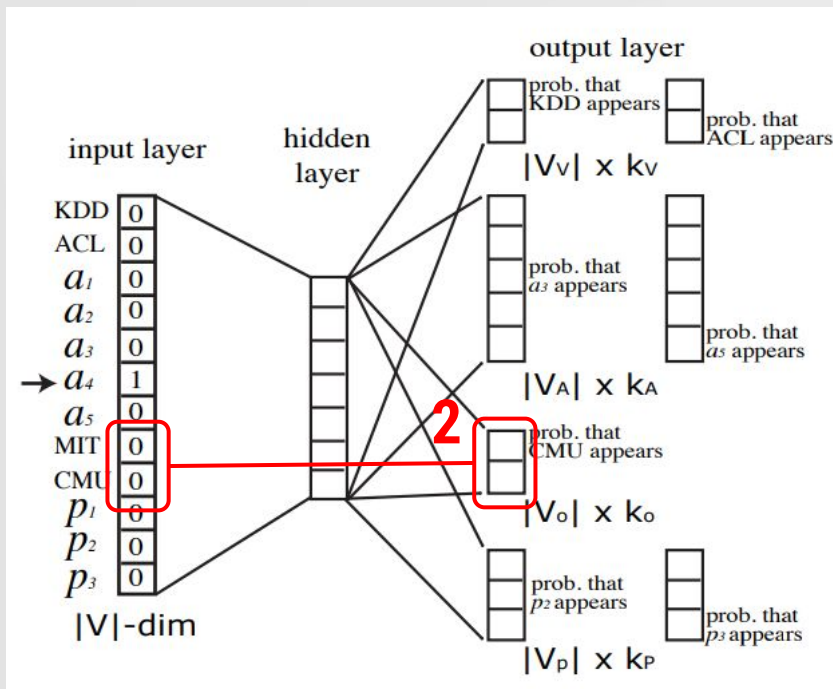
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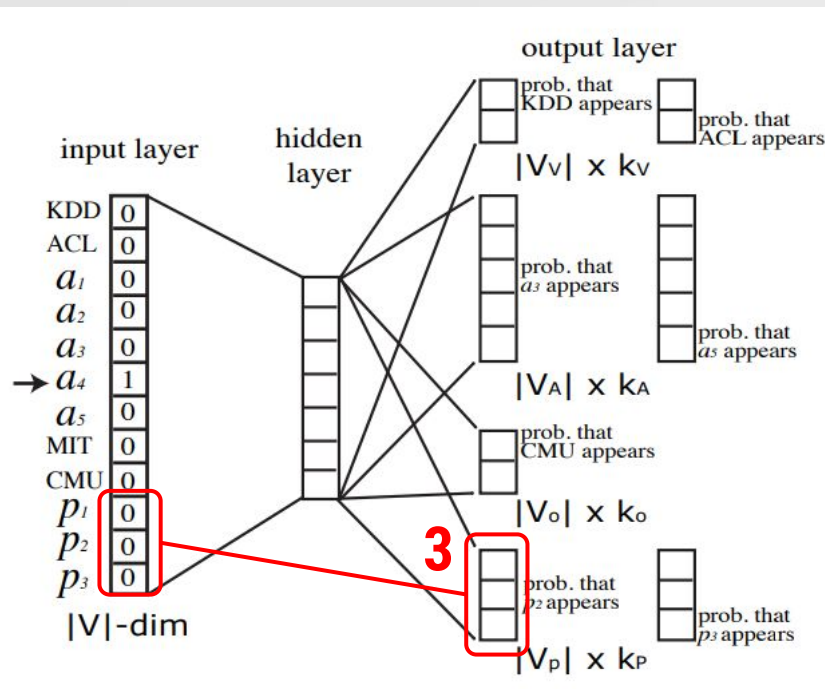
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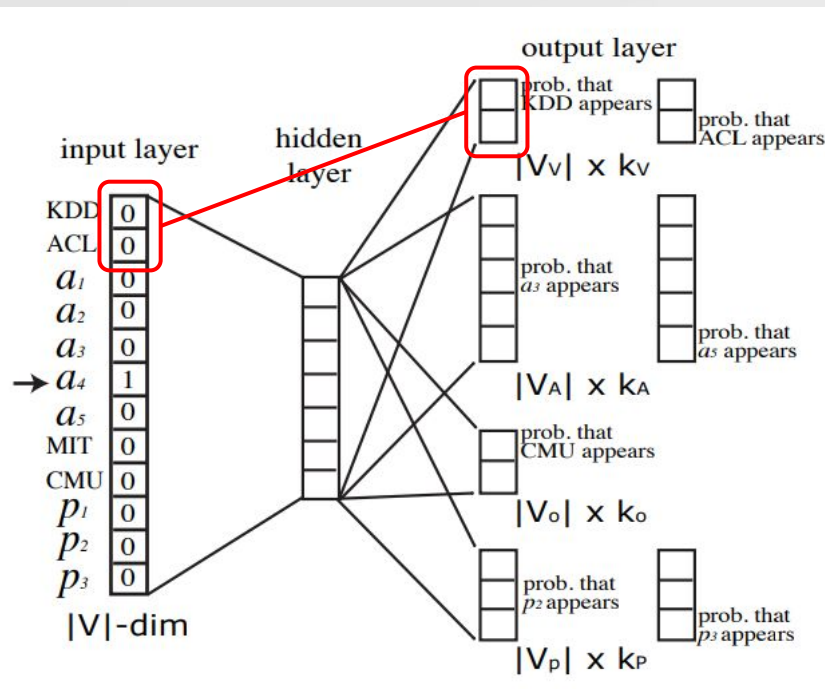
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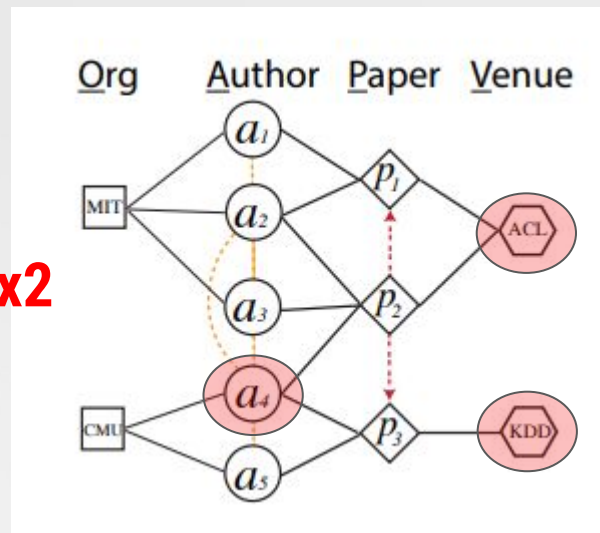
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03 The model

Metapath2vec++



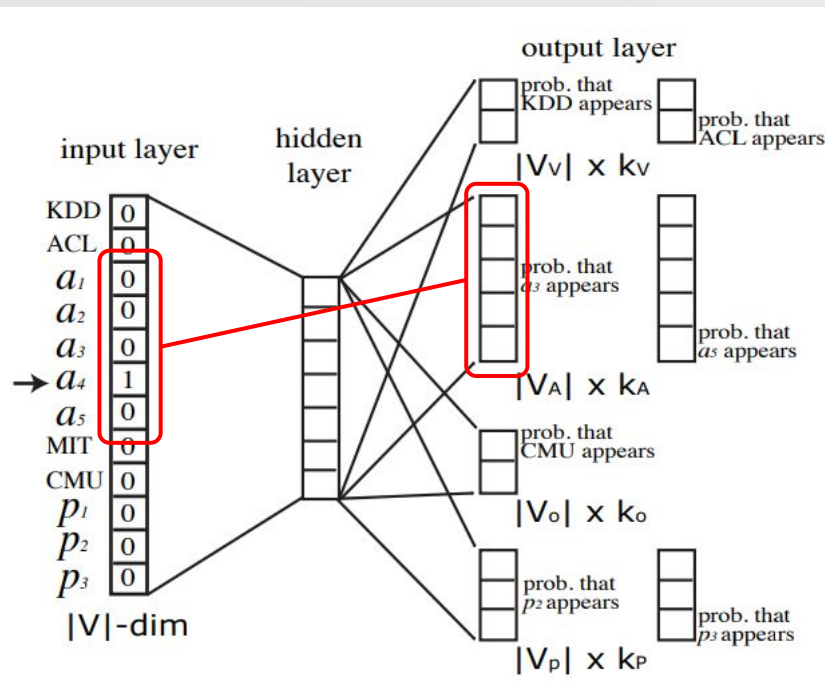
2x2



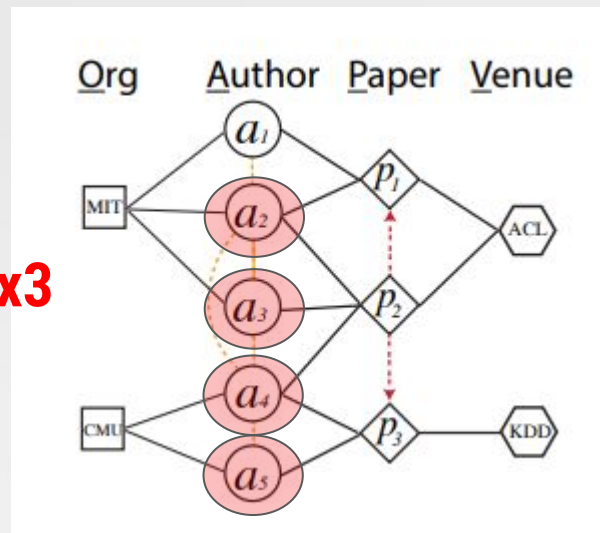
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Metapath2vec++



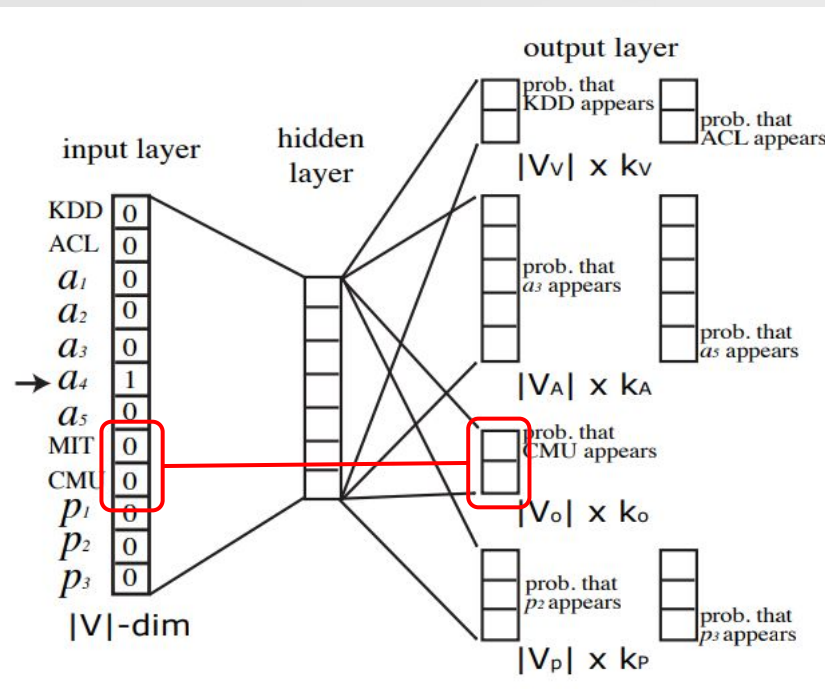
4x3



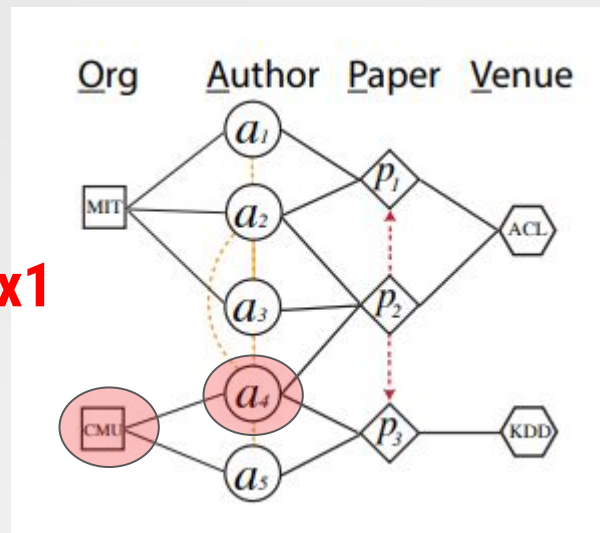
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03 The model

Metapath2vec++



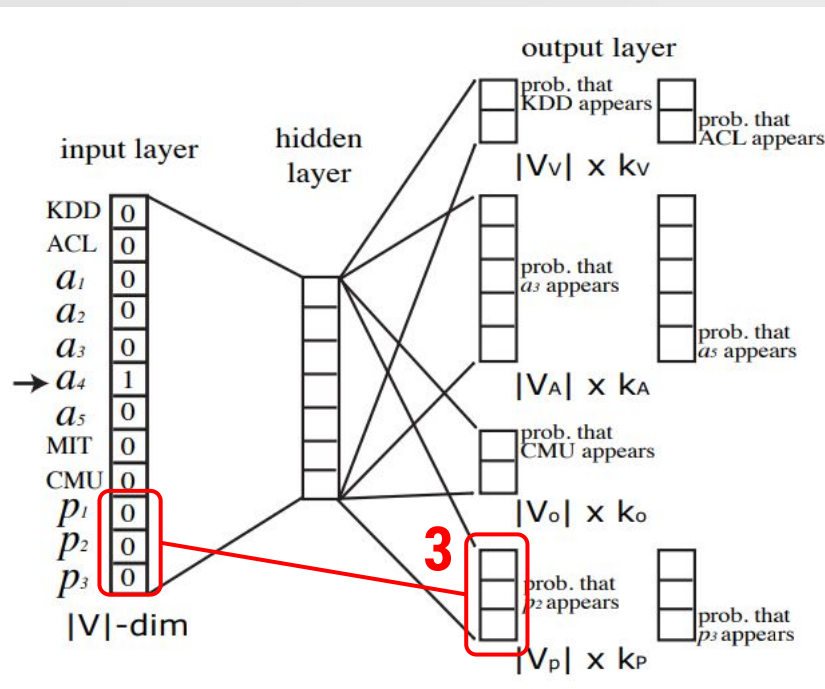
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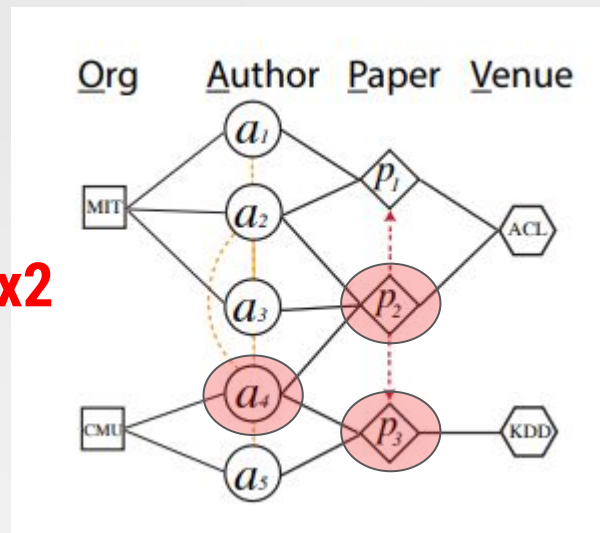
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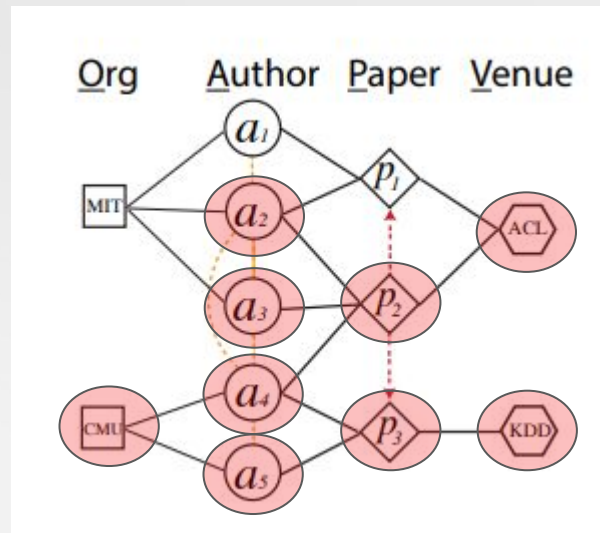
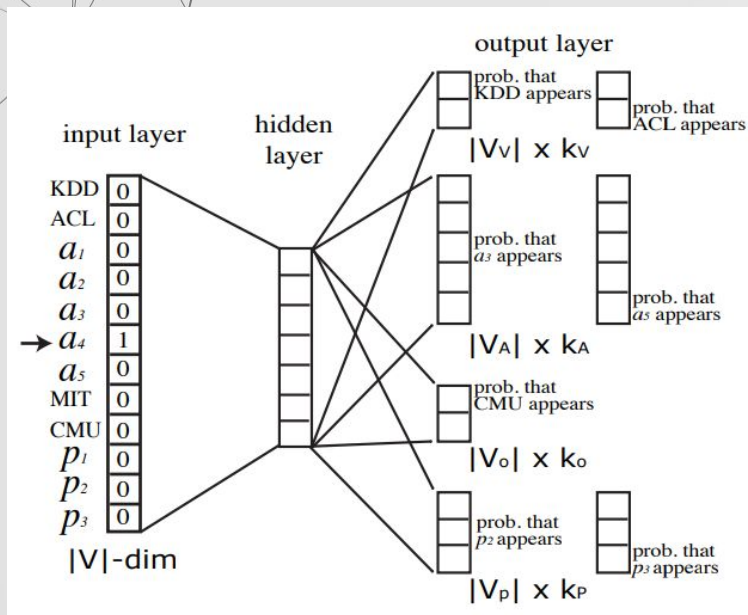
3x2



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03 The model

Metapath2vec++



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04 Training

```
CLASS MetaPath2Vec ( edge_index_dict, embedding_dim, metapath, walk_length, context_size,  
walks_per_node=1, num_negative_samples=1, num_nodes_dict=None, sparse=False ) \[source\]
```

04 Training

```
{('paper',  
  'written by',  
  'author'): tensor([[ 0, 1,  
    [ 0, 1, 2, ...  
('author',  
  'wrote',  
  'paper'): tensor([[ 0, 0,  
    [ 0, 45988, 124807, ...  
('paper',  
  'published in',  
  'venue'): tensor([[ 0, 1,  
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('venue',  
  'published',  
  'paper'): tensor([[ 0, 0,  
    [2203069, 2203070, 2203071, ...
```



CLASS `MetaPath2Vec` (`edge_index_dict`, `embedding_dim`, `metapath`, `walk_length`, `context_size`,
`walks_per_node=1`, `num_negative_samples=1`, `num_nodes_dict=None`, `sparse=False`) [\[source\]](#)

04 Training

```
{('paper',  
  'written by',  
  'author'): tensor([[ 0, 1,  
    [ 0, 1, 2, ...  
(('author',  
  'wrote',  
  'paper'): tensor([[ 0, 0,  
    [ 0, 45988, 124807, ...  
(('paper',  
  'published in',  
  'venue'): tensor([[ 0, 1,  
    [ 2190, 2190, 2190, ...  
(('venue',  
  'published',  
  'paper'): tensor([[ 0, 0,  
    [2203069, 2203070, 2203071, ...
```

Size of the output
embedding

CLASS MetaPath2Vec (edge_index_dict, embedding_dim, metapath, walk_length, context_size, walks_per_node=1, num_negative_samples=1, num_nodes_dict=None, sparse=False) [\[source\]](#)

04 Training

```
{('paper',  
  'written by',  
  'author'): tensor([[ 0, 1,  
    [ 0, 1, 2, ...  
(('author',  
  'wrote',  
  'paper'): tensor([[ 0, 0,  
    [ 0, 45988, 124807, ...  
(('paper',  
  'published in',  
  'venue'): tensor([[ 0, 1,  
    [ 2190, 2190, 2190, ...  
(('venue',  
  'published',  
  'paper'): tensor([[ 0, 0,  
    [2203069, 2203070, 2203071, ...
```

```
[('author', 'wrote', 'paper'),  
 ('paper', 'published in', 'venue'),  
 ('venue', 'published', 'paper'),  
 ('paper', 'written by', 'author')]
```

Size of the output
embedding

```
CLASS MetaPath2Vec ( edge_index_dict, embedding_dim, metapath, walk_length, context_size,  
walks_per_node=1, num_negative_samples=1, num_nodes_dict=None, sparse=False ) \[source\]
```


04 Training

```
{('paper',  
  'written by',  
  'author'): tensor([[ 0, 1,  
    [ 0, 1, 2, ...  
('author',  
  'wrote',  
  'paper'): tensor([[ 0, 0,  
    [ 0, 45988, 124807, ...  
('paper',  
  'published in',  
  'venue'): tensor([[ 0, 1,  
    [ 2190, 2190, 2190, ...  
('venue',  
  'published',  
  'paper'): tensor([[ 0, 0,  
    [2203069, 2203070, 2203071, ...
```

```
[('author', 'wrote', 'paper'),  
 ('paper', 'published in', 'venue'),  
 ('venue', 'published', 'paper'),  
 ('paper', 'written by', 'author')]
```

Size of the output
embedding

Equal to
Node2Vec

```
CLASS MetaPath2Vec ( edge_index_dict, embedding_dim, metapath, walk_length, context_size,  
walks_per_node=1, num_negative_samples=1, num_nodes_dict=None, sparse=False ) \[source\]
```

Equal to
Node2Vec



04 Training

Jupyter notebook



05 Load a pre trained model

Jupyter notebook