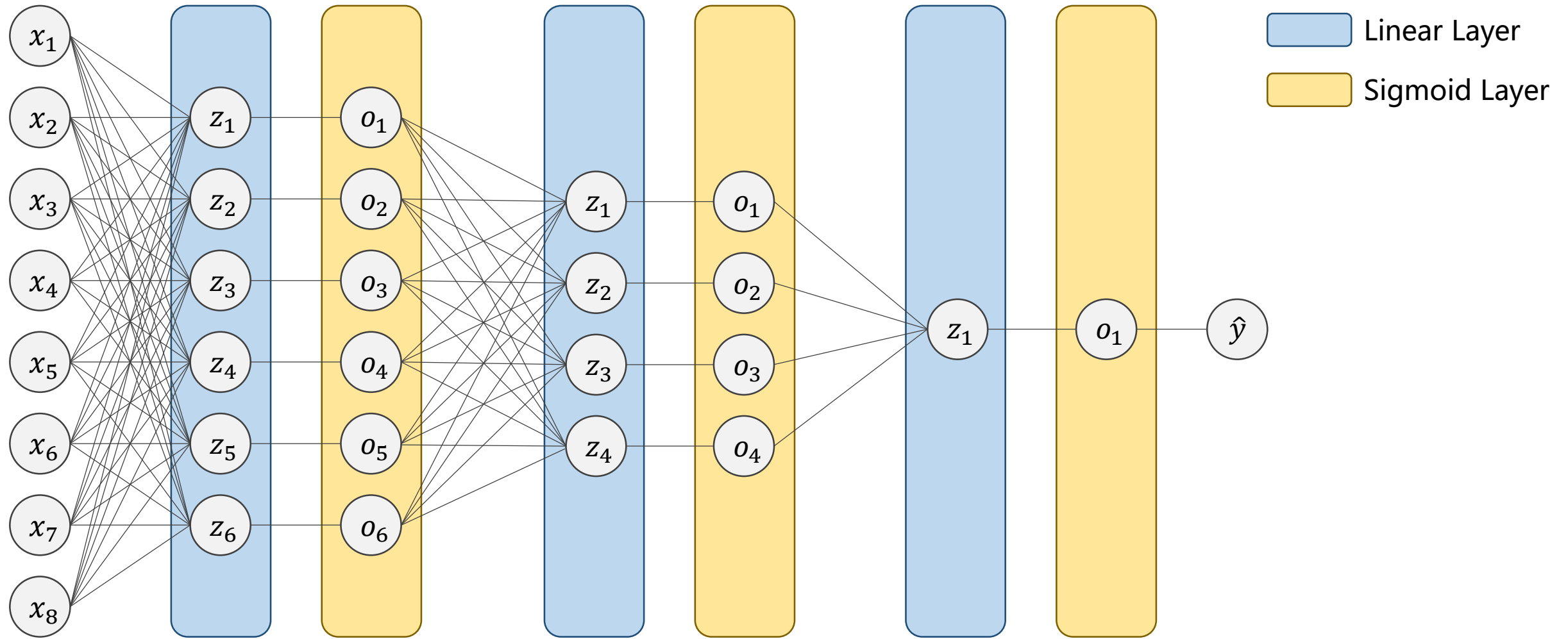




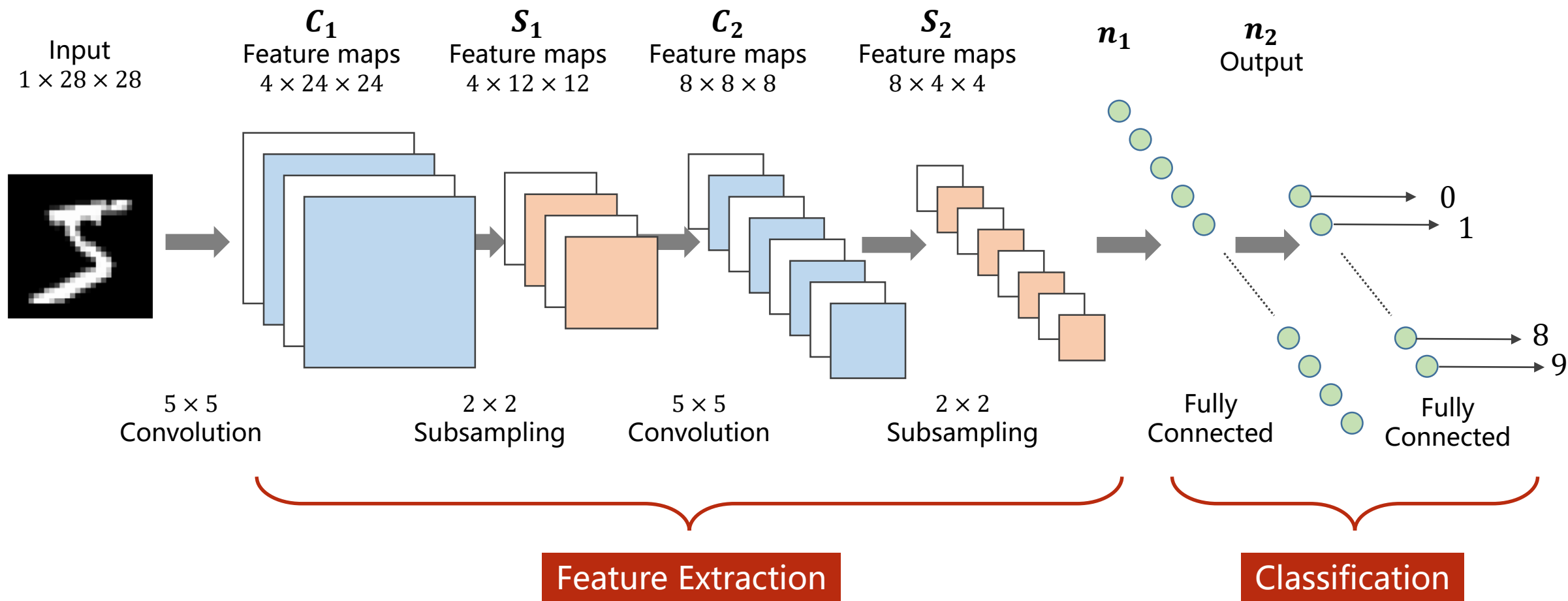
PyTorch Tutorial

12. Basic RNN

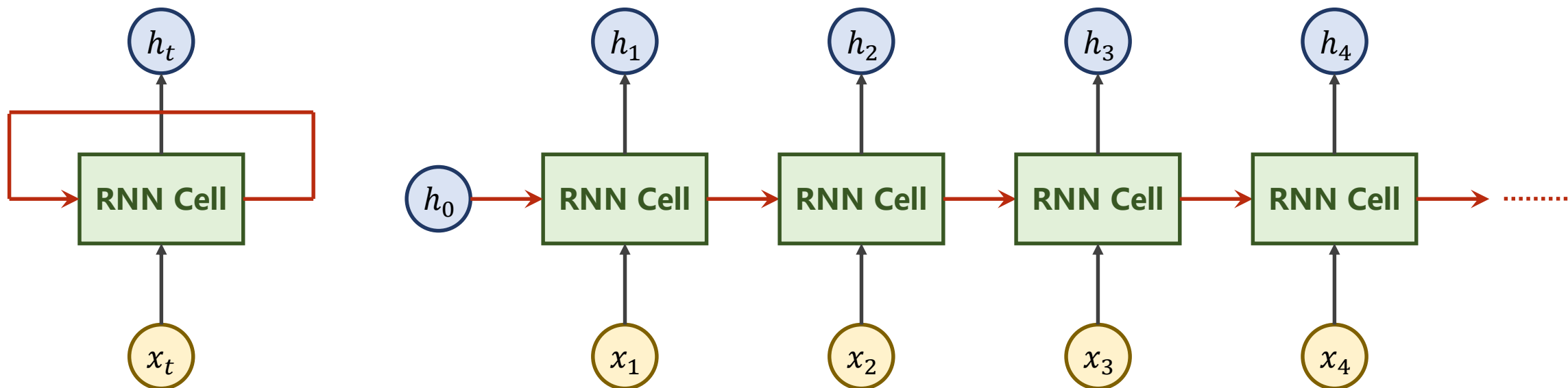
Revision: DNN



Revision: CNN

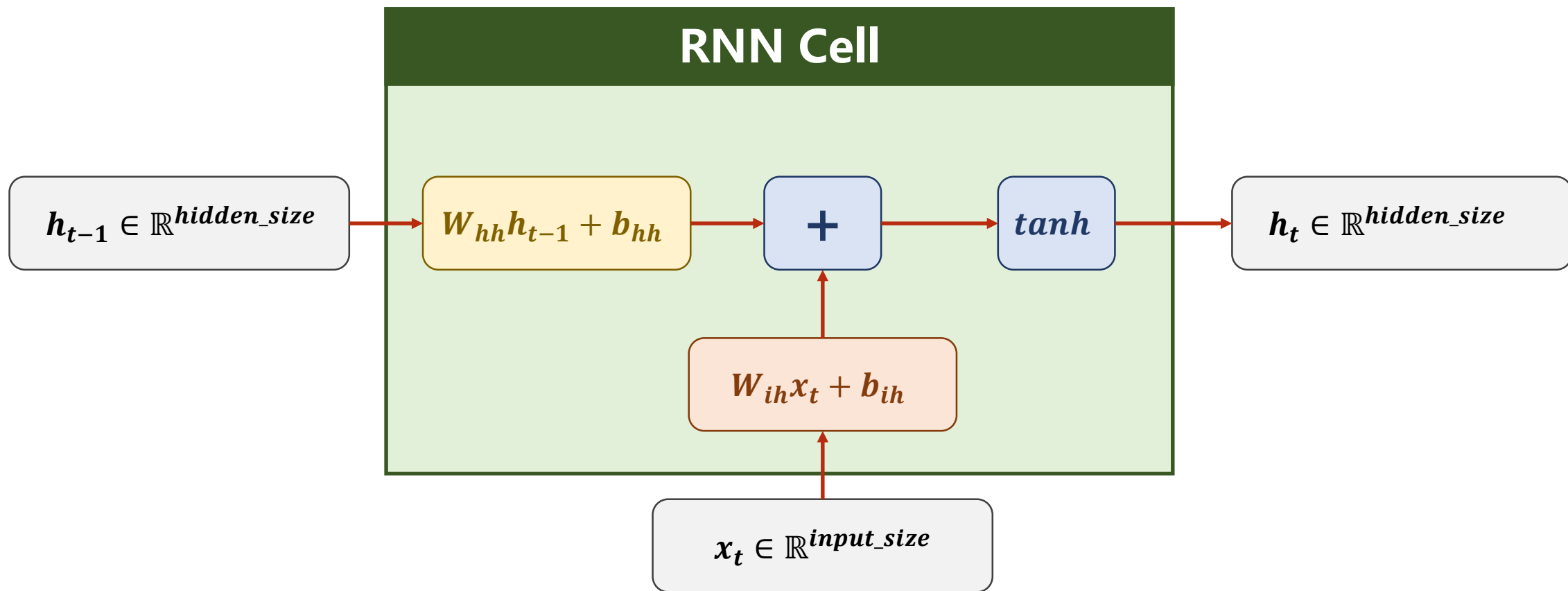


What is RNNs?

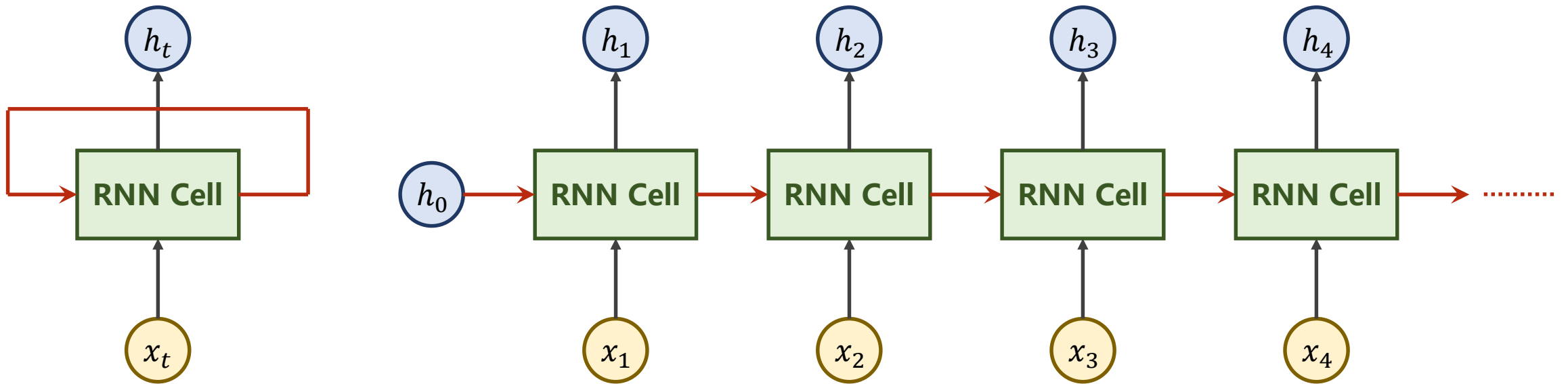


What is RNN?

$$h_t = \tanh(W_{ih}x_t + b_{ih} + W_{hh}h_{t-1} + b_{hh})$$

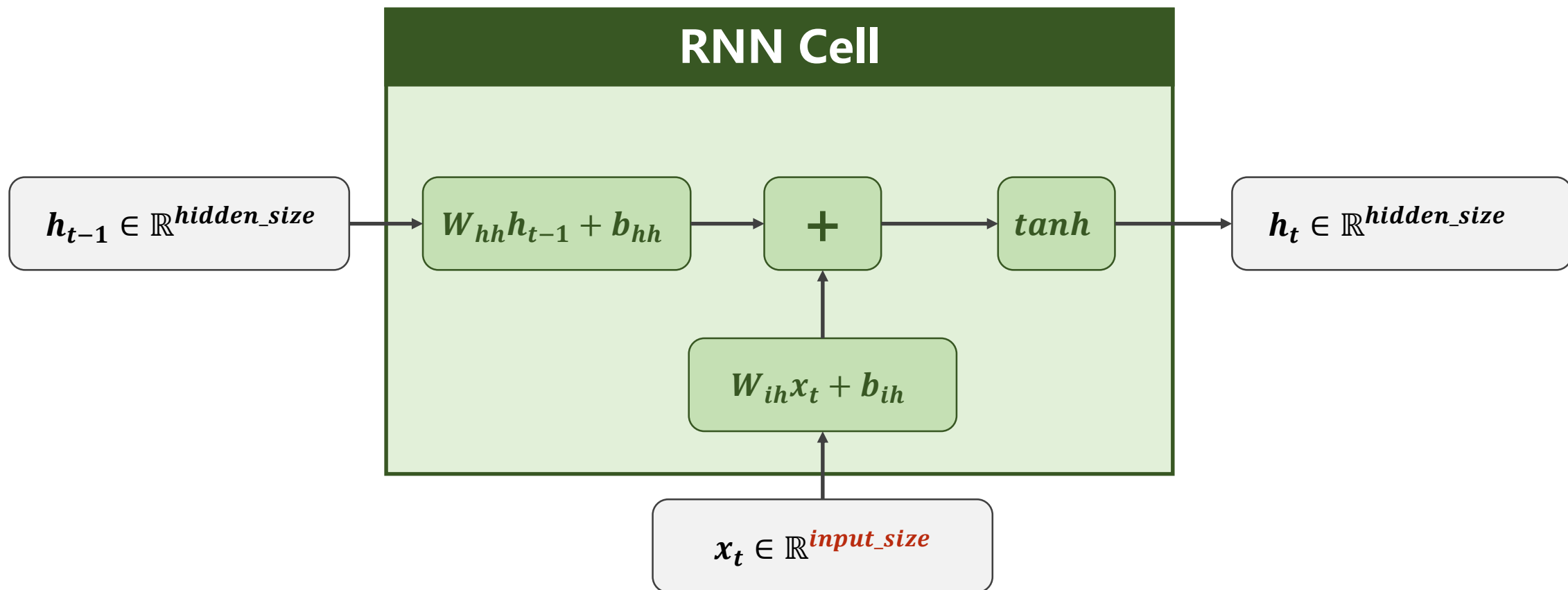


What is RNNs?



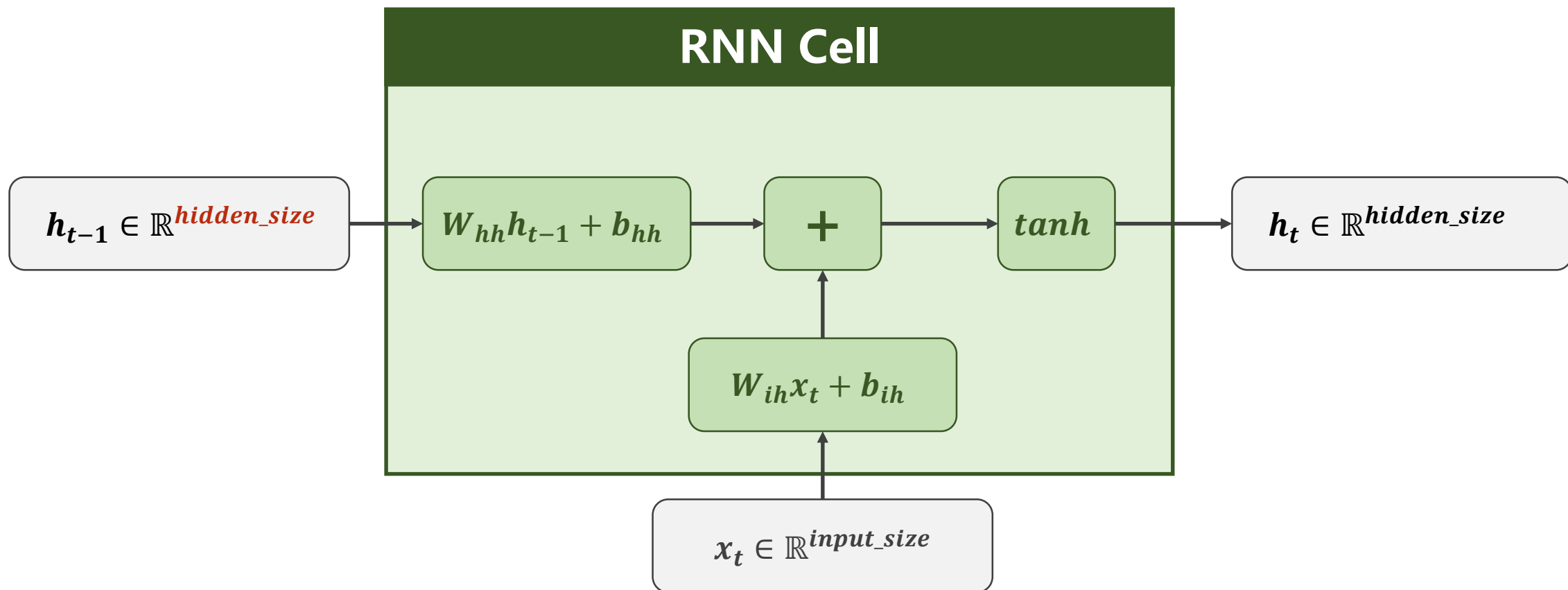
RNN Cell in PyTorch

```
cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)
```



RNN Cell in PyTorch

```
cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)
```



RNN Cell in PyTorch

```
cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)
```

```
hidden = cell(input, hidden)
```

input

input of shape $(batch, input_size)$
hidden of shape $(batch, hidden_size)$

output

hidden of shape $(batch, hidden_size)$

How to use RNNCell

- Suppose we have sequence with below properties:
 - *batchSize* = 1
 - *seqLen* = 3
 - *inputSize* = 4
 - *hiddenSize* = 2

How to use RNNCell

- Suppose we have sequence with below properties:
 - *batchSize* = 1
 - *seqLen* = 3
 - *inputSize* = 4
 - *hiddenSize* = 2
- So the shape of inputs and outputs of RNNCell:
 - *input.shape* = (*batchSize*, *inputSize*)
 - *output.shape* = (*batchSize*, *hiddenSize*)

How to use RNNCell

- Suppose we have sequence with below properties:
 - ***batchSize*** = 1
 - *seqLen* = 3
 - *inputSize* = 4
 - ***hiddenSize*** = 2
- So the shape of inputs and outputs of RNNCell:
 - *input.shape* = (*batchSize*, *inputSize*)
 - ***output.shape*** = (***batchSize***, ***hiddenSize***)

How to use RNNCell

- Suppose we have sequence with below properties:
 - *batchSize* = 1
 - *seqLen* = 3
 - *inputSize* = 4
 - *hiddenSize* = 2
- So the shape of inputs and outputs of RNNCell:
 - *input.shape* = (*batchSize*, *inputSize*)
 - *output.shape* = (*batchSize*, *hiddenSize*)
- The sequence can be warped in one Tensor with shape:
 - *dataset.shape* = (*seqLen*, *batchSize*, *inputSize*)

How to use RNNCell

```
import torch
```

```
batch_size = 1
```

```
seq_len = 3
```

```
input_size = 4
```

```
hidden_size = 2
```

Parameters

```
cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)
```

```
# (seq, batch, features)
```

```
dataset = torch.randn(seq_len, batch_size, input_size)
```

```
hidden = torch.zeros(batch_size, hidden_size)
```

```
for idx, input in enumerate(dataset):
```

```
    print('=' * 20, idx, '=' * 20)
```

```
    print('Input size: ', input.shape)
```

```
    hidden = cell(input, hidden)
```

```
    print('outputs size: ', hidden.shape)
```

```
    print(hidden)
```

How to use RNNCell

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2

cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)

# (seq, batch, features)
dataset = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(batch_size, hidden_size)

for idx, input in enumerate(dataset):
    print('=' * 20, idx, '=' * 20)
    print('Input size: ', input.shape)

    hidden = cell(input, hidden)

    print('outputs size: ', hidden.shape)
    print(hidden)
```

Construction of RNNCell

How to use RNNCell

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2

cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)

# (seq, batch, features)
dataset = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(batch_size, hidden_size)

for idx, input in enumerate(dataset):
    print('=' * 20, idx, '=' * 20)
    print('Input size: ', input.shape)

    hidden = cell(input, hidden)

    print('outputs size: ', hidden.shape)
    print(hidden)
```

Wrapping the sequence into:
(seqLen, batchSize, inputSize)

How to use RNNCell

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2

cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)

# (seq, batch, features)
dataset = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(batch_size, hidden_size)

for idx, input in enumerate(dataset):
    print('=' * 20, idx, '=' * 20)
    print('Input size: ', input.shape)

    hidden = cell(input, hidden)

    print('outputs size: ', hidden.shape)
    print(hidden)
```

Initializing the *hidden* to zero

How to use RNNCell

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2

cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)

# (seq, batch, features)
dataset = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(batch_size, hidden_size)

for idx, input in enumerate(dataset):
    print('=' * 20, idx, '=' * 20)
    print('Input size: ', input.shape)

    hidden = cell(input, hidden)

print('outputs size: ', hidden.shape)
print(hidden)
```

The shape of input is:
(batchSize, inputSize)

Input size: torch.Size([1, 4])

How to use RNNCell

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2

cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)

# (seq, batch, features)
dataset = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(batch_size, hidden_size)

for idx, input in enumerate(dataset):
    print('=' * 20, idx, '=' * 20)
    print('Input size: ', input.shape)

    hidden = cell(input, hidden)

    print('hidden size: ', hidden.shape)
    print(hidden)
```

The shape of *hidden* is:
(*batchSize*, *hiddenSize*)

hidden size: torch.Size([1, 2])

How to use RNNCell

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2

cell = torch.nn.RNNCell(input_size=input_size, hidden_size=hidden_size)

# (seq, batch, features)
dataset = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(batch_size, hidden_size)

for idx, input in enumerate(dataset):
    print('=' * 20, idx, '=' * 20)
    print('Input size: ', input.shape)

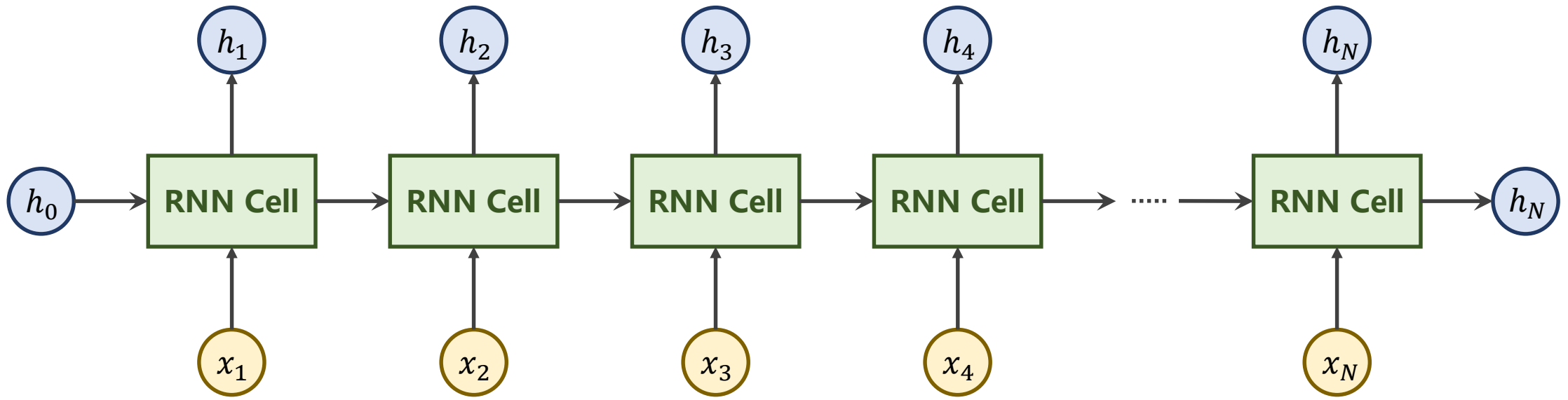
    hidden = cell(input, hidden)

    print('outputs size: ', hidden.shape)
    print(hidden)
```

```
===== 0 =====
Input size: torch.Size([1, 4])
outputs size: torch.Size([1, 2])
tensor([[ -0.1579,  0.5140]])
===== 1 =====
Input size: torch.Size([1, 4])
outputs size: torch.Size([1, 2])
tensor([[ -0.9577,  0.6502]])
===== 2 =====
Input size: torch.Size([1, 4])
outputs size: torch.Size([1, 2])
tensor([[ -0.7661, -0.9128]])
```

How to use RNN

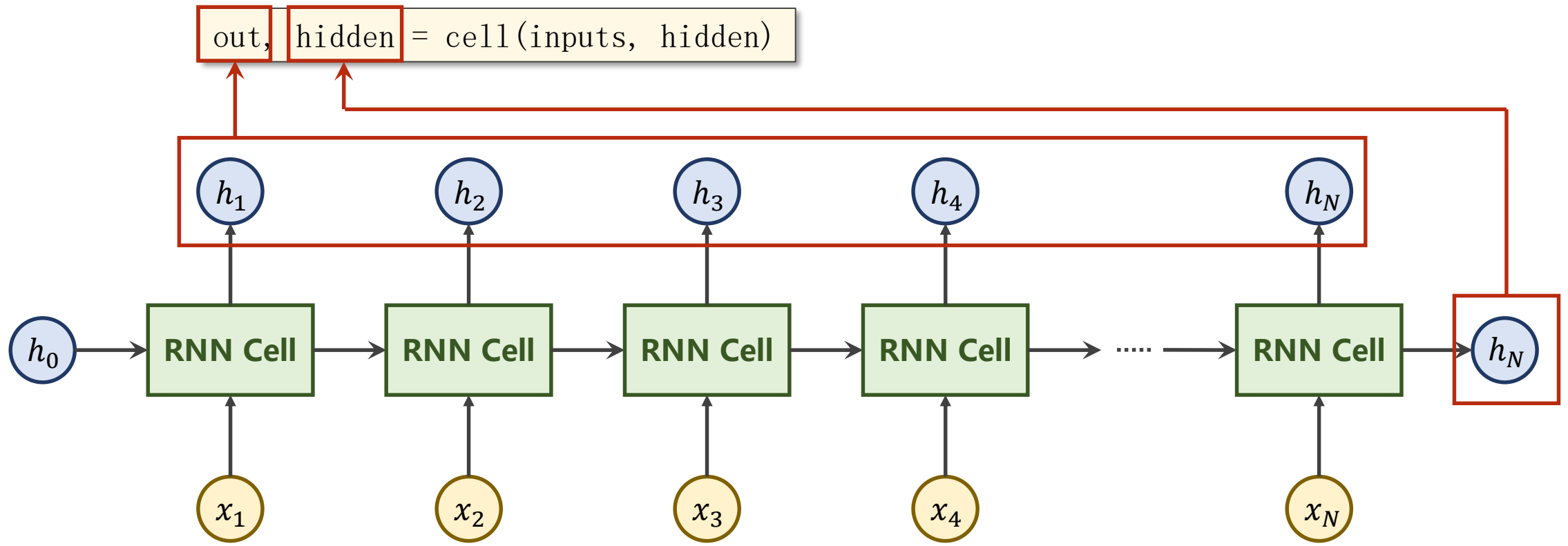
```
cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,  
                    num_layers=num_layers)
```



How to use RNN

```
cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,  
                    num_layers=num_layers)
```

```
out, hidden = cell(inputs, hidden)
```



How to use RNN

```
cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,  
                    num_layers=num_layers)
```

```
out, hidden = cell(inputs, hidden)
```

input

input of shape $(seqSize, batch, input_size)$

hidden of shape $(numLayers, batch, hidden_size)$

output

Output of shape $(seqLen, batch, hidden_size)$

hidden of shape $(numLayers, batch, hidden_size)$

How to use RNN

- Suppose we have sequence with below properties:
 - *batchSize*
 - *seqLen*
 - *inputSize, hiddenSize,*
 - *numLayers*

How to use RNN

- Suppose we have sequence with below properties:
 - *batchSize*
 - *seqLen*
 - *inputSize*, *hiddenSize*,
 - *numLayers*
- The shape of *input* and *h_0* of RNN:
 - *input.shape* = (*seqLen*, *batchSize*, *inputSize*)
 - *h_0.shape* = (*numLayers*, *batchSize*, *hiddenSize*)

How to use RNN

- Suppose we have sequence with below properties:
 - *batchSize*
 - *seqLen*
 - *inputSize*, *hiddenSize*,
 - *numLayers*
- The shape of *input* and *h_0* of RNN:
 - *input.shape* = (*seqLen*, *batchSize*, *inputSize*)
 - *h_0.shape* = (*numLayers*, *batchSize*, *hiddenSize*)

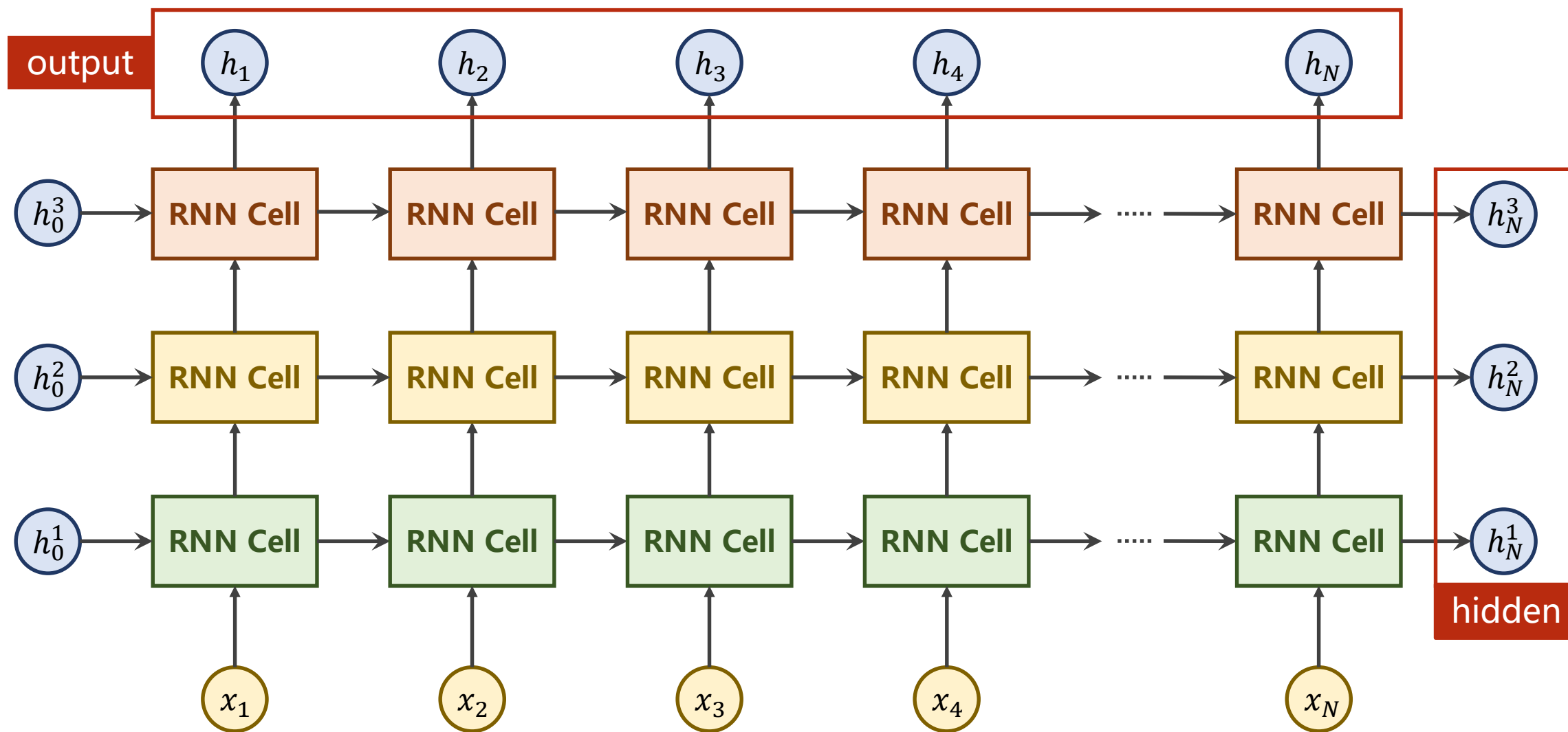
How to use RNN

- Suppose we have sequence with below properties:
 - *batchSize*
 - *seqLen*
 - *inputSize*, *hiddenSize*,
 - *numLayers*
- The shape of *input* and *h_0* of RNN:
 - *input.shape* = (*seqLen*, *batchSize*, *inputSize*)
 - *h_0.shape* = (*numLayers*, *batchSize*, *hiddenSize*)
- The shape of *output* and *h_n* of RNN:
 - *output.shape* = (*seqLen*, *batchSize*, *hiddenSize*)
 - *h_n.shape* = (*numLayers*, *batchSize*, *hiddenSize*)

How to use RNN

- Suppose we have sequence with below properties:
 - *batchSize*
 - *seqLen*
 - *inputSize*, *hiddenSize*,
 - *numLayers*
- The shape of *input* and *h_0* of RNN:
 - *input.shape* = (*seqLen*, *batchSize*, *inputSize*)
 - *h_0.shape* = (*numLayers*, *batchSize*, *hiddenSize*)
- The shape of *output* and *h_n* of RNN:
 - *output.shape* = (*seqLen*, *batchSize*, *hiddenSize*)
 - *h_n.shape* = (*numLayers*, *batchSize*, *hiddenSize*)

How to use RNN - numLayers



How to use RNN

```
import torch
```

```
batch_size = 1
```

```
seq_len = 3
```

```
input_size = 4
```

```
hidden_size = 2
```

```
num_layers = 1
```

Parameters

```
cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,  
                    num_layers=num_layers)
```

```
# (seqLen, batchSize, inputSize)
```

```
inputs = torch.randn(seq_len, batch_size, input_size)
```

```
hidden = torch.zeros(num_layers, batch_size, hidden_size)
```

```
out, hidden = cell(inputs, hidden)
```

```
print('Output size:', out.shape)
```

```
print('Output:', out)
```

```
print('Hidden size: ', hidden.shape)
```

```
print('Hidden: ', hidden)
```

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2
num_layers = 1

cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
                    num_layers=num_layers)

# (seqLen, batchSize, inputSize)
inputs = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

Construction of RNN

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2
num_layers = 1

cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
                    num_layers=num_layers)

# (seqLen, batchSize, inputSize)
inputs = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

Wrapping the sequence into:
(seqLen, batchSize, inputSize)

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
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cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
                    num_layers=num_layers)

# (seqLen, batchSize, inputSize)
inputs = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

Initializing the *hidden* to zero

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2
num_layers = 1

cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
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# (seqLen, batchSize, inputSize)
inputs = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

The shape of *output* is:
(seqSize, batchSize, hiddenSize)

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2
num_layers = 1

cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
                    num_layers=num_layers)

# (seqLen, batchSize, inputSize)
inputs = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

The shape of *hidden* is:
(*numLayers*, *batchSize*, *hiddenSize*)

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2
num_layers = 1

cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
                    num_layers=num_layers)

# (seqLen, batchSize, inputSize)
inputs = torch.randn(seq_len, batch_size, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

```
Output size: torch.Size([3, 1, 2])
Output: tensor([
  [ 0.2360, -0.5550]],
  [ 0.2685,  0.0106]],
  [ 0.1172, -0.2262]])
Hidden size: torch.Size([1, 1, 2])
Hidden: tensor([[[ 0.1172, -0.2262]]])
```

How to use RNN

- **batch_first**: if True, the input and output tensors are provided as:
 - *(batchSize, seqLen, input_size)*

```
cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,  
                    num_layers=num_layers, batch_first=True)
```

```
inputs = torch.randn(seq_len, batch_size, input_size)
```



```
inputs = torch.randn(batch_size, seq_len, input_size)
```

How to use RNN

```
import torch

batch_size = 1
seq_len = 3
input_size = 4
hidden_size = 2
num_layers = 1

cell = torch.nn.RNN(input_size=input_size, hidden_size=hidden_size,
                    num_layers=num_layers, batch_first=True)

# (seqLen, batchSize, inputSize)
inputs = torch.randn(batch_size, seq_len, input_size)
hidden = torch.zeros(num_layers, batch_size, hidden_size)

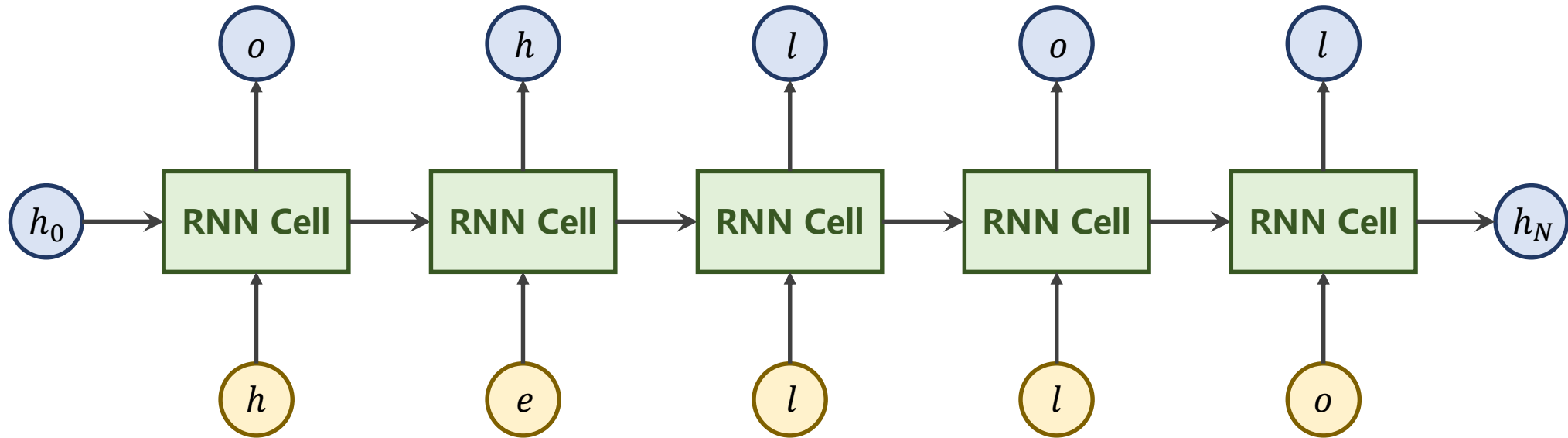
out, hidden = cell(inputs, hidden)

print('Output size:', out.shape)
print('Output:', out)
print('Hidden size: ', hidden.shape)
print('Hidden: ', hidden)
```

Output size: torch.Size([1, 3, 2])
Output: tensor([[0.6582, -0.7281],
[0.5021, -0.8324],
[-0.5225, -0.5621]])
Hidden size: torch.Size([1, 1, 2])
Hidden: tensor([[[[-0.5225, -0.5621]]]])

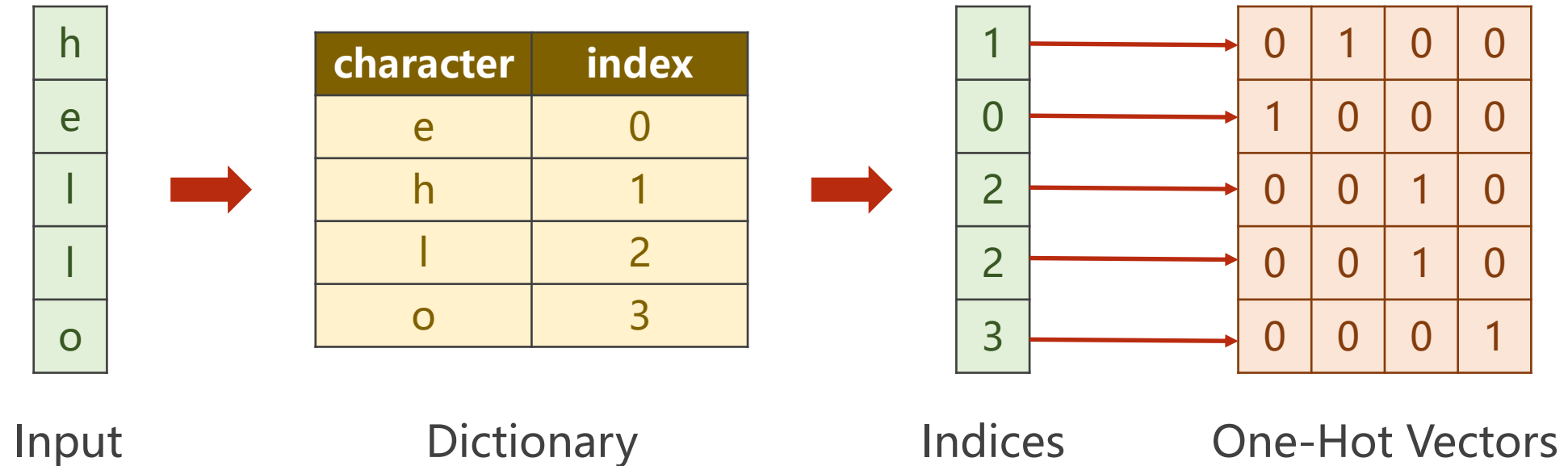
Example 12-1: Using RNNCell

- Train a model to learn:
 - "hello" -> "ohlol"



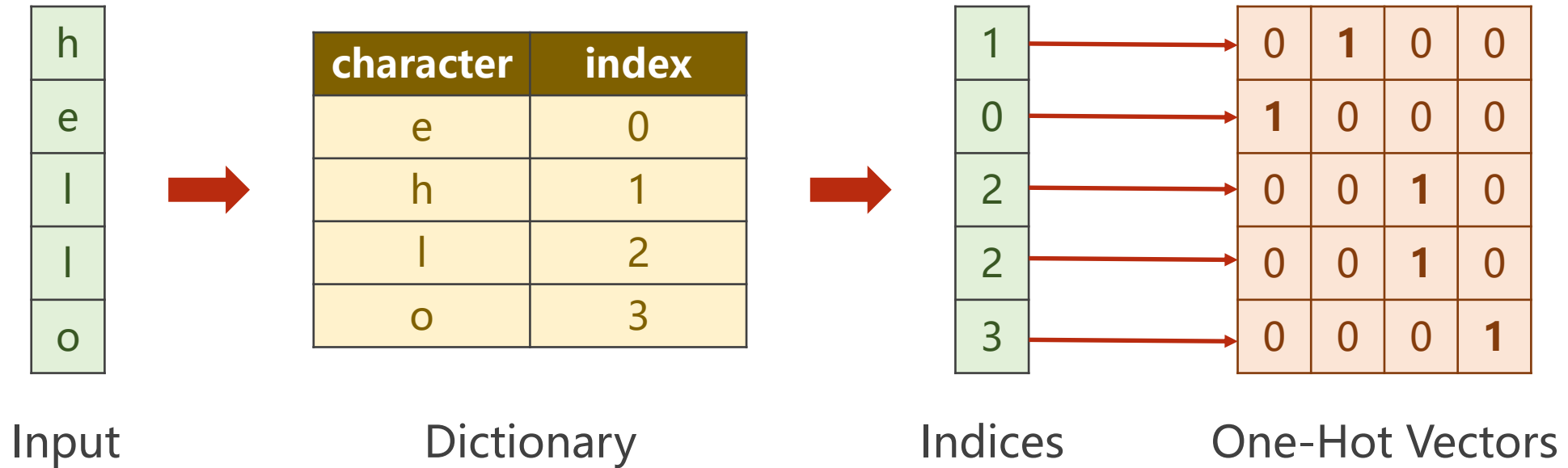
Example 12-1: Using RNNCell

- The inputs of RNN Cell should be vectors of numbers.



Example 12-1: Using RNNCell

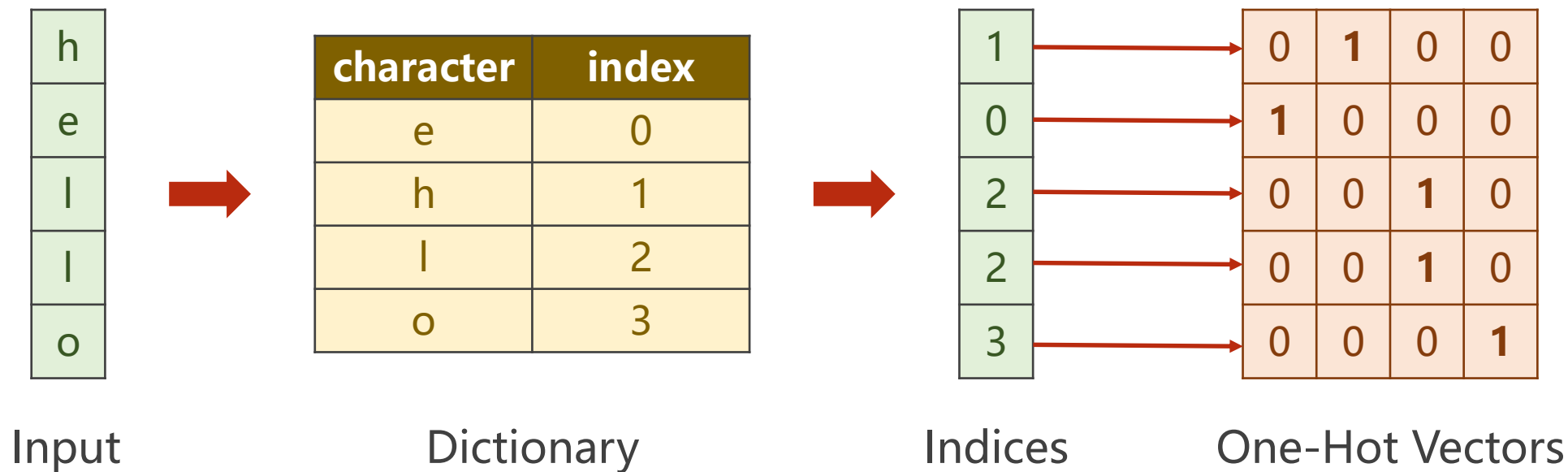
- The inputs of RNN Cell should be vectors of numbers.



inputSize = ?

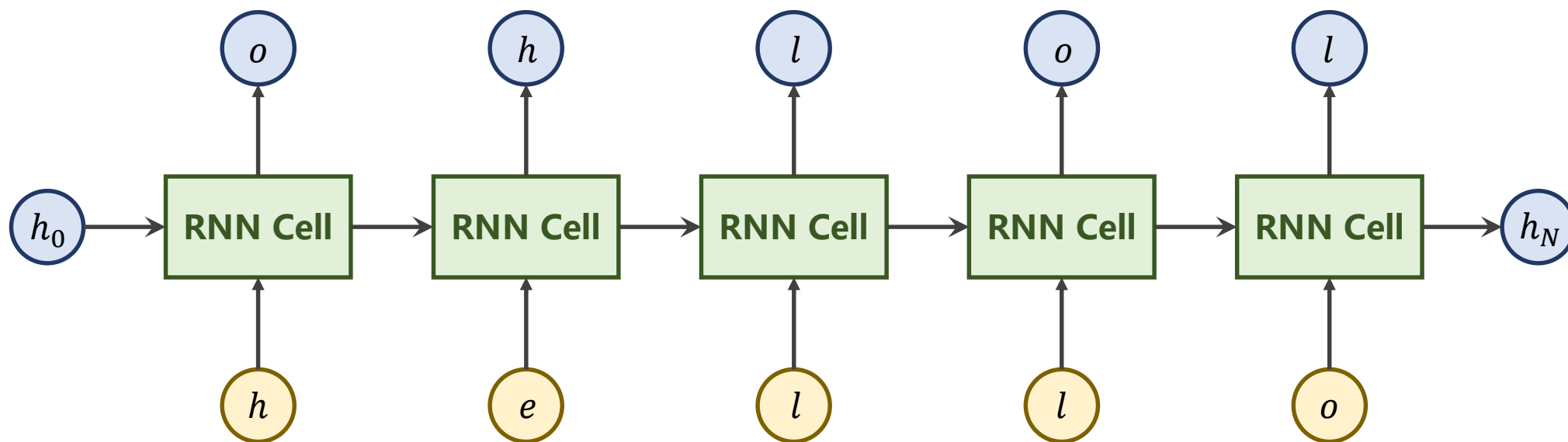
Example 12-1: Using RNNCell

- The inputs of RNN Cell should be vectors of numbers.



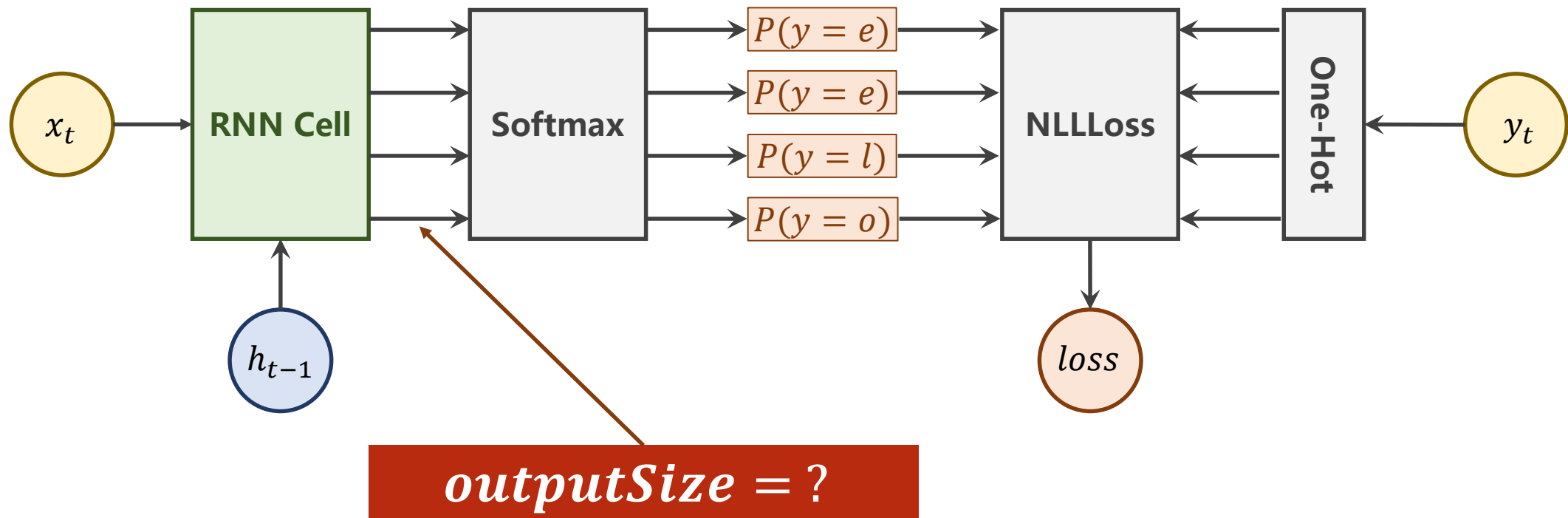
inputSize = 4

Example 12-1: Using RNNCell



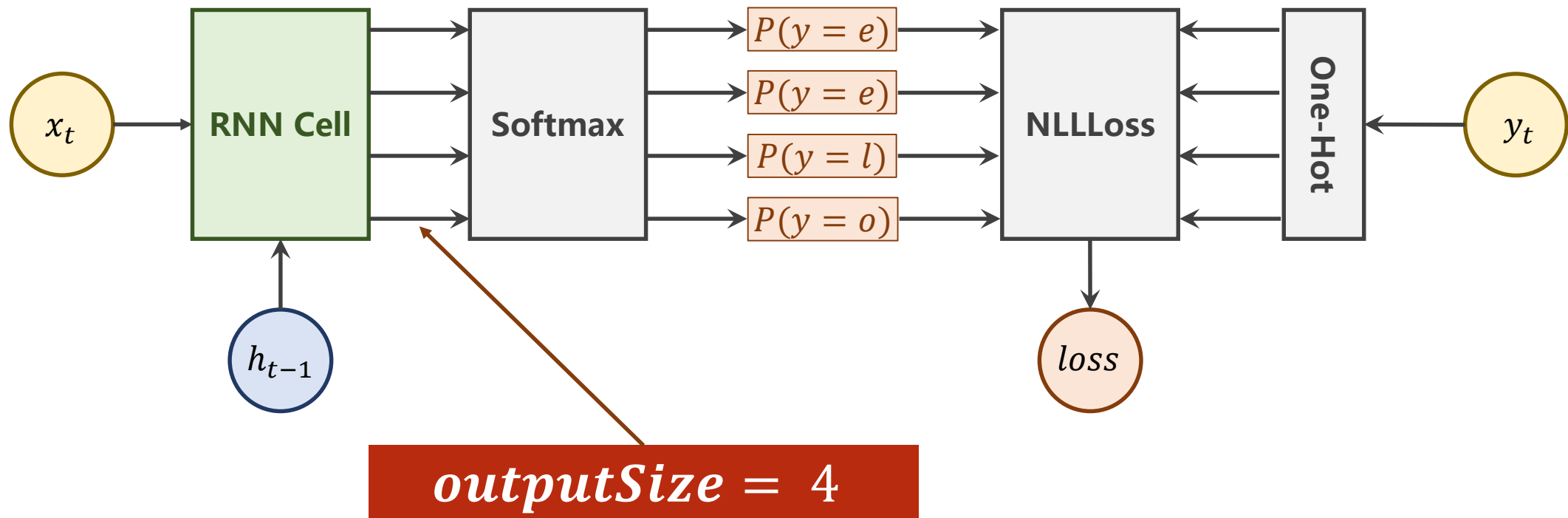
Example 12-1: Using RNNCell

- The outputs of RNN Cell should be vectors of prediction.



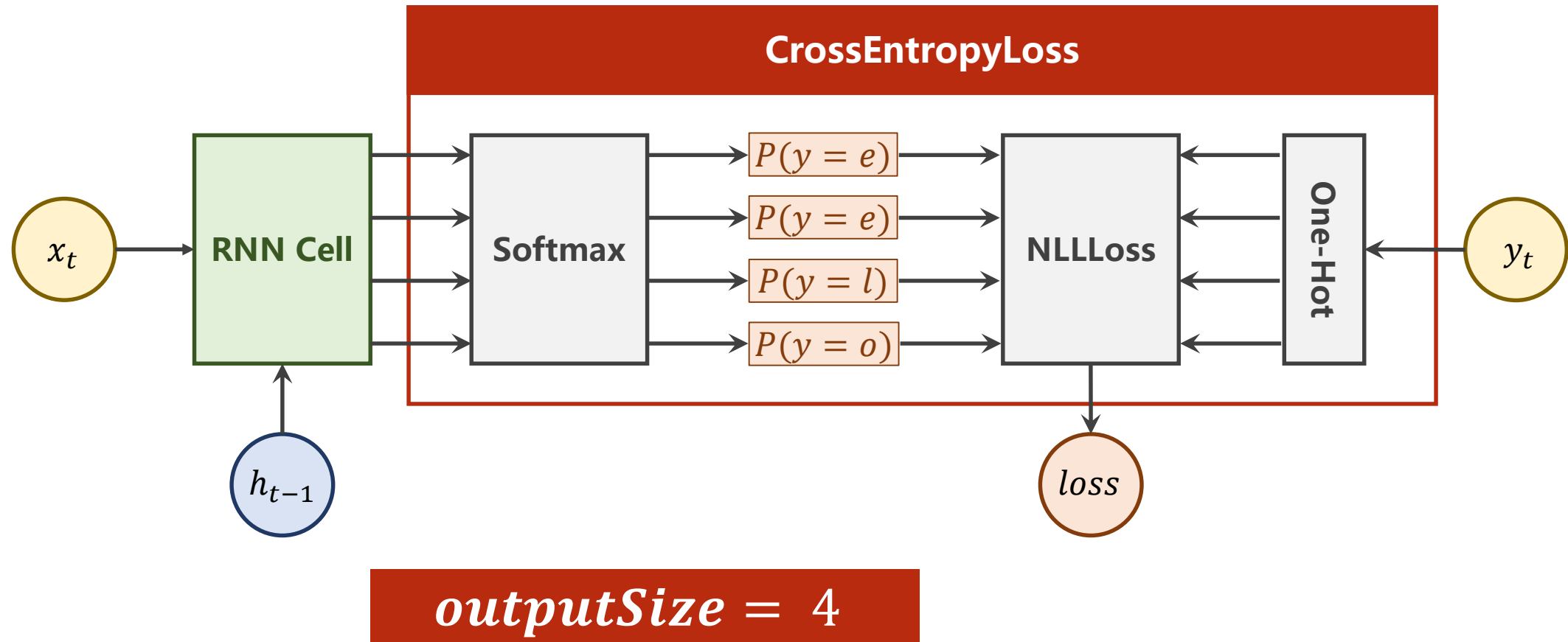
Example 12-1: Using RNNCell

- The outputs of RNN Cell should be vectors of prediction.



Example 12-1: Using RNNCell

- The outputs of RNN Cell should be vectors of prediction.



Example 12-1: Code – Parameters

```
import torch

input_size = 4
hidden_size = 4
batch_size = 1
```

Example 12-1: Code – Prepare Data

```
idx2char = ['e', 'h', 'l', 'o']
```

```
x_data = [1, 0, 2, 2, 3]
```

```
y_data = [3, 1, 2, 3, 2]
```

```
one_hot_lookup = [[1, 0, 0, 0],  
                  [0, 1, 0, 0],  
                  [0, 0, 1, 0],  
                  [0, 0, 0, 1]]
```

```
x_one_hot = [one_hot_lookup[x] for x in x_data]
```

```
inputs = torch.Tensor(x_one_hot).view(-1, batch_size, input_size)
```

```
labels = torch.LongTensor(y_data).view(-1, 1)
```

The dictionary

Example 12-1: Code – Prepare Data

```
idx2char = ['e', 'h', 'l', 'o']
```

```
x_data = [1, 0, 2, 2, 3]
```

```
y_data = [3, 1, 2, 3, 2]
```

```
one_hot_lookup = [[1, 0, 0, 0],
```

```
                  [0, 1, 0, 0],
```

```
                  [0, 0, 1, 0],
```

```
                  [0, 0, 0, 1]]
```

```
x_one_hot = [one_hot_lookup[x] for x in x_data]
```

```
inputs = torch.Tensor(x_one_hot).view(-1, batch_size, input_size)
```

```
labels = torch.LongTensor(y_data).view(-1, 1)
```

The input sequence is 'hello'

Example 12-1: Code – Prepare Data

```
idx2char = ['e', 'h', 'l', 'o']
x_data = [1, 0, 2, 2, 3]
y_data = [3, 1, 2, 3, 2]

one_hot_lookup = [[1, 0, 0, 0],
                  [0, 1, 0, 0],
                  [0, 0, 1, 0],
                  [0, 0, 0, 1]]
x_one_hot = [one_hot_lookup[x] for x in x_data]

inputs = torch.Tensor(x_one_hot).view(-1, batch_size, input_size)
labels = torch.LongTensor(y_data).view(-1, 1)
```

The output sequence is 'ohlol'

Example 12-1: Code – Prepare Data

```
idx2char = ['e', 'h', 'l', 'o']
x_data = [1, 0, 2, 2, 3]
y_data = [3, 1, 2, 3, 2]

one_hot_lookup = [[1, 0, 0, 0],
                  [0, 1, 0, 0],
                  [0, 0, 1, 0],
                  [0, 0, 0, 1]]
x_one_hot = [one_hot_lookup[x] for x in x_data]

inputs = torch.Tensor(x_one_hot).view(-1, batch_size, input_size)
labels = torch.LongTensor(y_data).view(-1, 1)
```

Convert indices into one-hot vector

Example 12-1: Code – Prepare Data

```
idx2char = ['e', 'h', 'l', 'o']
x_data = [1, 0, 2, 2, 3]
y_data = [3, 1, 2, 3, 2]

one_hot_lookup = [[1, 0, 0, 0],
                  [0, 1, 0, 0],
                  [0, 0, 1, 0],
                  [0, 0, 0, 1]]
x_one_hot = [one_hot_lookup[x] for x in x_data]

inputs = torch.Tensor(x_one_hot).view(-1, batch_size, input_size)
labels = torch.LongTensor(y_data).view(-1, 1)
```

Reshape the inputs to
(seqLen, batchSize, inputSize)

Example 12-1: Code – Prepare Data

```
idx2char = ['e', 'h', 'l', 'o']
x_data = [1, 0, 2, 2, 3]
y_data = [3, 1, 2, 3, 2]

one_hot_lookup = [[1, 0, 0, 0],
                  [0, 1, 0, 0],
                  [0, 0, 1, 0],
                  [0, 0, 0, 1]]
x_one_hot = [one_hot_lookup[x] for x in x_data]

inputs = torch.Tensor(x_one_hot).view(-1, batch_size, input_size)
labels = torch.LongTensor(y_data).view(-1, 1)
```

Reshape the labels to
(*seqLen*, 1)

Example 12-1: Code – Design Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size):
        super(Model, self).__init__()
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn_cell = torch.nn.RNNCell(input_size=self.input_size,
                                          hidden_size=self.hidden_size)

    def forward(self, input, hidden):
        hidden = self.rnn_cell(input, hidden)
        return hidden

    def init_hidden(self):
        return torch.zeros(self.batch_size, self.hidden_size)

net = Model(input_size, hidden_size, batch_size)
```

Initial the parameters

Example 12-1: Code – Design Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size):
        super(Model, self).__init__()
        # self.num_layers = num_layers
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn_cell = torch.nn.RNNCell(input_size=self.input_size,
                                          hidden_size=self.hidden_size)

    def forward(self, input, hidden):
        hidden = self.rnn_cell(input, hidden)
        return hidden

    def init_hidden(self):
        return torch.zeros(self.batch_size, self.hidden_size)

net = Model(input_size, hidden_size, batch_size)
```

Shape of inputs :

(batchSize, inputSize)

Shape of hidden:

(batchSize, hiddenSize)

Example 12-1: Code – Design Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size):
        super(Model, self).__init__()
        # self.num_layers = num_layers
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn_cell = torch.nn.RNNCell(input_size=self.input_size,
                                          hidden_size=self.hidden_size)

    def forward(self, input, hidden):
        hidden = self.rnn_cell(input, hidden)
        return hidden

    def init_hidden(self):
        return torch.zeros(self.batch_size, self.hidden_size)

net = Model(input_size, hidden_size, batch_size)
```

Provide initial hidden

Example 12-1: Code – Loss and Optimizer

```
criterion = torch.nn.CrossEntropyLoss()  
optimizer = torch.optim.Adam(net.parameters(), lr=0.1)
```

Example 12-1: Code – Training Cycle

```
for epoch in range(15):
    loss = 0
    optimizer.zero_grad()
    hidden = net.init_hidden()
    print('Predicted string: ', end='')
    for input, label in zip(inputs, labels):
        hidden = net(input, hidden)
        loss += criterion(hidden, label)
        _, idx = hidden.max(dim=1)
        print(idx2char[idx.item()], end='')
    loss.backward()
    optimizer.step()
    print(', Epoch [%d/15] loss=%.4f' % (epoch+1, loss.item()))
```

Training steps

Example 12-1: Code – Training Cycle

```
for epoch in range(15):
    loss = 0
    optimizer.zero_grad()
    hidden = net.init_hidden()
    print('Predicted string: ', end='')
    for input, label in zip(inputs, labels):
        hidden = net(input, hidden)
        loss += criterion(hidden, label)
        _, idx = hidden.max(dim=1)
        print(idx2char[idx.item()], end='')
    loss.backward()
    optimizer.step()
    print(', Epoch [%d/15] loss=%.4f' % (epoch+1, loss.item()))
```

Shape of *inputs*:

(seqLen, batchSize, inputSize)

Shape of *input*:

(batchSize, hiddenSize)

Example 12-1: Code – Training Cycle

```
for epoch in range(15):
    loss = 0
    optimizer.zero_grad()
    hidden = net.init_hidden()
    print('Predicted string: ', end='')
    for input, label in zip(inputs, labels):
        hidden = net(input, hidden)
        loss += criterion(hidden, label)
        _, idx = hidden.max(dim=1)
        print(idx2char[idx.item()], end='')
    loss.backward()
    optimizer.step()
    print(', Epoch [%d/15] loss=%.4f' % (epoch+1, loss.item()))
```

Shape of *labels*:

(*seqSize*, 1)

Shape of *label*:

(1)

Example 12-1: Code – Training Cycle

```
for epoch in range(15):
    loss = 0
    optimizer.zero_grad()
    hidden = net.init_hidden()
    print('Predicted string: ', end='')
    for input, label in zip(inputs, labels):
        hidden = net(input, hidden)
        loss += criterion(hidden, label)
        _, idx = hidden.max(dim=1)
        print(idx2char[idx.item()], end='')
    loss.backward()
    optimizer.step()
    print(', Epoch [%d/15] loss=%.4f' % (epoch+1, loss.item()))
```

RNN Cell

Example 12-1: Code – Training Cycle

```
for epoch in range(15):
    loss = 0
    optimizer.zero_grad()
    hidden = net.init_hidden()
    print('Predicted string: ', end='')
    for input, label in zip(inputs, labels):
        hidden = net(input, hidden)
        loss += criterion(hidden, label)
        _, idx = hidden.max(dim=1)
        print(idx2char[idx.item()], end='')
    loss.backward()
    optimizer.step()
    print(', Epoch [%d/15] loss=%.4f' % (epoch+1, loss.item()))
```

Output prediction

Example 12-1: Code – Result


```
Predicted string: loeeh, Epoch [1/15] loss=8.0117  
Predicted string: oooeh, Epoch [2/15] loss=7.2082  
Predicted string: oooooh, Epoch [3/15] loss=6.6208  
Predicted string: oooooh, Epoch [4/15] loss=6.1802  
Predicted string: oooooh, Epoch [5/15] loss=5.8060  
Predicted string: oooooh, Epoch [6/15] loss=5.4739  
Predicted string: oooooh, Epoch [7/15] loss=5.1593  
Predicted string: oooool, Epoch [8/15] loss=4.8593  
Predicted string: oooool, Epoch [9/15] loss=4.5819  
Predicted string: ohool, Epoch [10/15] loss=4.3287  
Predicted string: ohlol, Epoch [11/15] loss=4.0909  
Predicted string: ohlol, Epoch [12/15] loss=3.8573  
Predicted string: ohlol, Epoch [13/15] loss=3.6246  
Predicted string: ohlol, Epoch [14/15] loss=3.4007  
Predicted string: ohlol, Epoch [15/15] loss=3.2005
```

Example 12-2 Using RNN Module

```
criterion = torch.nn.CrossEntropyLoss()
optimizer = torch.optim.Adam(net.parameters(), lr=0.05)

for epoch in range(15):
    optimizer.zero_grad()
    outputs = net(inputs)
    loss = criterion(outputs, labels)
    loss.backward()
    optimizer.step()

    _, idx = outputs.max(dim=1)
    idx = idx.data.numpy()
    print('Predicted: ', ''.join([idx2char[x] for x in idx]), end='')
    print(', Epoch [%d/15] loss = %.3f' % (epoch + 1, loss.item()))
```



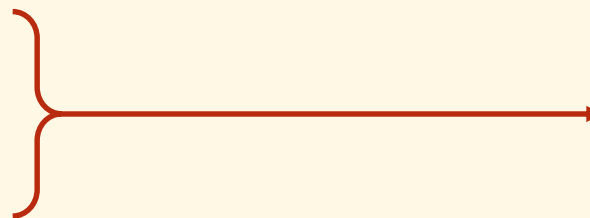
Training steps

Example 12-2 Change Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size, num_layers=1):
        super(Model, self).__init__()
        self.num_layers = num_layers
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn = torch.nn.RNN(input_size=self.input_size,
                                hidden_size=self.hidden_size,
                                num_layers=num_layers)

    def forward(self, input):
        hidden = torch.zeros(self.num_layers,
                              self.batch_size,
                              self.hidden_size)
        out, _ = self.rnn(input, hidden)
        return out.view(-1, self.hidden_size)

net = Model(input_size, hidden_size, batch_size, num_layers)
```



input_size = 4
hidden_size = 4
num_layers = 1
batch_size = 1
seq_len = 5

Example 12-2 Change Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size, num_layers=1):
        super(Model, self).__init__()
        self.num_layers = num_layers
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn = torch.nn.RNN(input_size=self.input_size,
                                hidden_size=self.hidden_size,
                                num_layers=num_layers)

    def forward(self, input):
        hidden = torch.zeros(self.num_layers,
                              self.batch_size,
                              self.hidden_size)
        out, _ = self.rnn(input, hidden)
        return out.view(-1, self.hidden_size)

net = Model(input_size, hidden_size, batch_size, num_layers)
```

```
input_size = 4
hidden_size = 4
num_layers = 1
batch_size = 1
seq_len = 5
```

Example 12-2 Change Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size, num_layers=1):
        super(Model, self).__init__()
        self.num_layers = num_layers
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn = torch.nn.RNN(input_size=self.input_size,
                                hidden_size=self.hidden_size,
                                num_layers=num_layers)

    def forward(self, input):
        hidden = torch.zeros(self.num_layers,
                            self.batch_size,
                            self.hidden_size)
        out, _ = self.rnn(input, hidden)
        return out.view(-1, self.hidden_size)

net = Model(input_size, hidden_size, batch_size, num_layers)
```

```
input_size = 4
hidden_size = 4
num_layers = 1
batch_size = 1
seq_len = 5
```

Shape of *hidden*:
(numLayers, batchSize, hiddenSize)

Example 12-2 Change Model

```
class Model(torch.nn.Module):
    def __init__(self, input_size, hidden_size, batch_size, num_layers=1):
        super(Model, self).__init__()
        self.num_layers = num_layers
        self.batch_size = batch_size
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.rnn = torch.nn.RNN(input_size=self.input_size,
                                hidden_size=self.hidden_size,
                                num_layers=num_layers)

    def forward(self, input):
        hidden = torch.zeros(self.num_layers,
                              self.batch_size,
                              self.hidden_size)
        out, _ = self.rnn(input, hidden)
        return out.view(-1, self.hidden_size)
```

Reshape *out* to:

(seqLen × batchSize, hiddenSize)

```
net = Model(input_size, hidden_size, batch_size, num_layers)
```

Example 12-2 Change Data

```
idx2char = ['e', 'h', 'l', 'o']  
x_data = [1, 0, 2, 2, 3]  
y_data = [3, 1, 2, 3, 2]
```

```
one_hot_lookup = [[1, 0, 0, 0],  
                  [0, 1, 0, 0],  
                  [0, 0, 1, 0],  
                  [0, 0, 0, 1]]  
x_one_hot = [one_hot_lookup[x] for x in x_data]
```

```
inputs = torch.Tensor(x_one_hot).view(seq_len, batch_size, input_size)  
labels = torch.LongTensor(y_data)
```

```
input_size = 4  
hidden_size = 4  
num_layers = 1  
batch_size = 1  
seq_len = 5
```

Shape of *inputs*:
(seqLen, batchSize, hiddenSize)

Example 12-2 Change Data

```
idx2char = ['e', 'h', 'l', 'o']  
x_data = [1, 0, 2, 2, 3]  
y_data = [3, 1, 2, 3, 2]
```

```
one_hot_lookup = [[1, 0, 0, 0],  
                  [0, 1, 0, 0],  
                  [0, 0, 1, 0],  
                  [0, 0, 0, 1]]
```

```
x_one_hot = [one_hot_lookup[x] for x in x_data]
```

```
inputs = torch.Tensor(x_one_hot).view(seq_len, batch_size, input_size)  
labels = torch.LongTensor(y_data)
```

```
input_size = 4  
hidden_size = 4  
num_layers = 1  
batch_size = 1  
seq_len = 5
```

Shape of *labels*:

(seqLen × batchSize, 1)

Example 12-2 Result

```
Predicted: lhhhh, Epoch [1/15] loss = 1.325
Predicted: loh hh, Epoch [2/15] loss = 1.190
Predicted: lolol, Epoch [3/15] loss = 1.090
Predicted: lolol, Epoch [4/15] loss = 1.017
Predicted: oolol, Epoch [5/15] loss = 0.958
Predicted: oolol, Epoch [6/15] loss = 0.904
Predicted: oolol, Epoch [7/15] loss = 0.852
Predicted: oolol, Epoch [8/15] loss = 0.804
Predicted: oolol, Epoch [9/15] loss = 0.759
Predicted: ohlol, Epoch [10/15] loss = 0.716
Predicted: ohlol, Epoch [11/15] loss = 0.678
Predicted: ohlol, Epoch [12/15] loss = 0.643
Predicted: ohlol, Epoch [13/15] loss = 0.613
Predicted: ohlol, Epoch [14/15] loss = 0.588
Predicted: ohlol, Epoch [15/15] loss = 0.568
```

Associate a vector with a word/character

- One-hot encoding of words and characters
 - The one-hot vectors are **high-dimension**.
 - The one-hot vectors are **sparse**.
 - The one-hot vectors are **hardcoded**.

Associate a vector with a word/character

- One-hot encoding of words and characters
 - The one-hot vectors are high-dimension.
 - The one-hot vectors are sparse.
 - The one-hot vectors are hardcoded.
- Do we have a way to associate a vector with a word/character with following specification:
 - **Lower-dimension**
 - **Dense**
 - **Learned from data**
- A popular and powerful way is called EMBEDDING.

Associate a vector with a word/character

- One-hot encoding of words and characters
 - The one-hot vectors are high-dimension.
 - The one-hot vectors are sparse.
 - The one-hot vectors are hardcoded.
- Do we have a way to associate a vector with a word/character with following specification:
 - Lower-dimension
 - Dense
 - Learned from data
- A popular and powerful way is called **EMBEDDING**.

One-hot vs Embedding

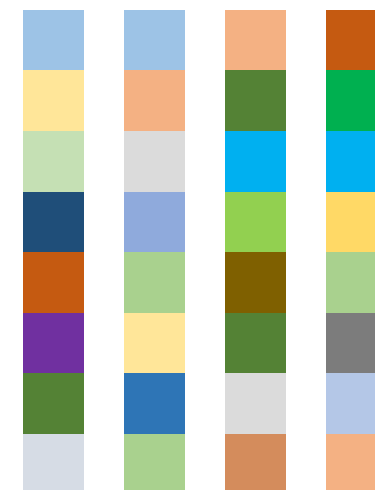
One-hot vectors:

- High-dimension
- Sparse
- Hardcoded



Embedding vectors:

- Lower-dimension
- Dense
- Learned from data



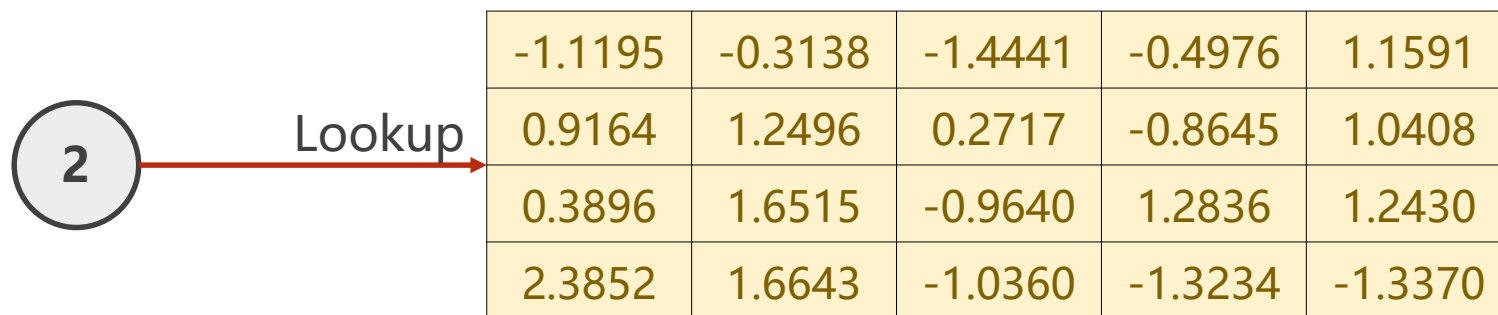
Embedding in PyTorch

embeddingSize

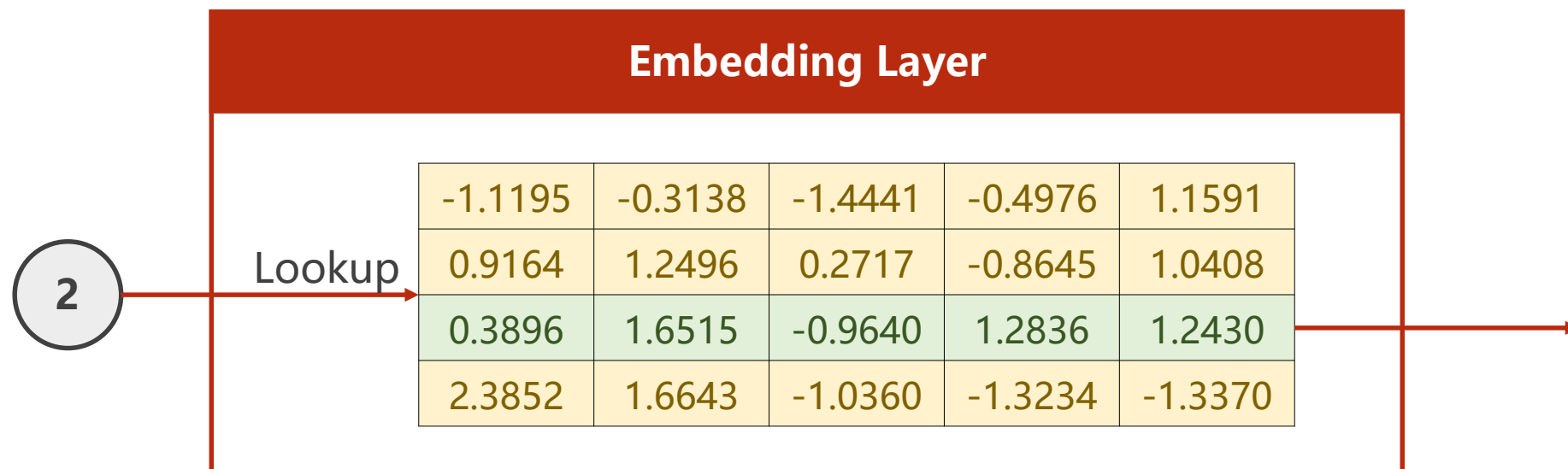
inputSize

-1.1195	-0.3138	-1.4441	-0.4976	1.1591
0.9164	1.2496	0.2717	-0.8645	1.0408
0.3896	1.6515	-0.9640	1.2836	1.2430
2.3852	1.6643	-1.0360	-1.3234	-1.3370

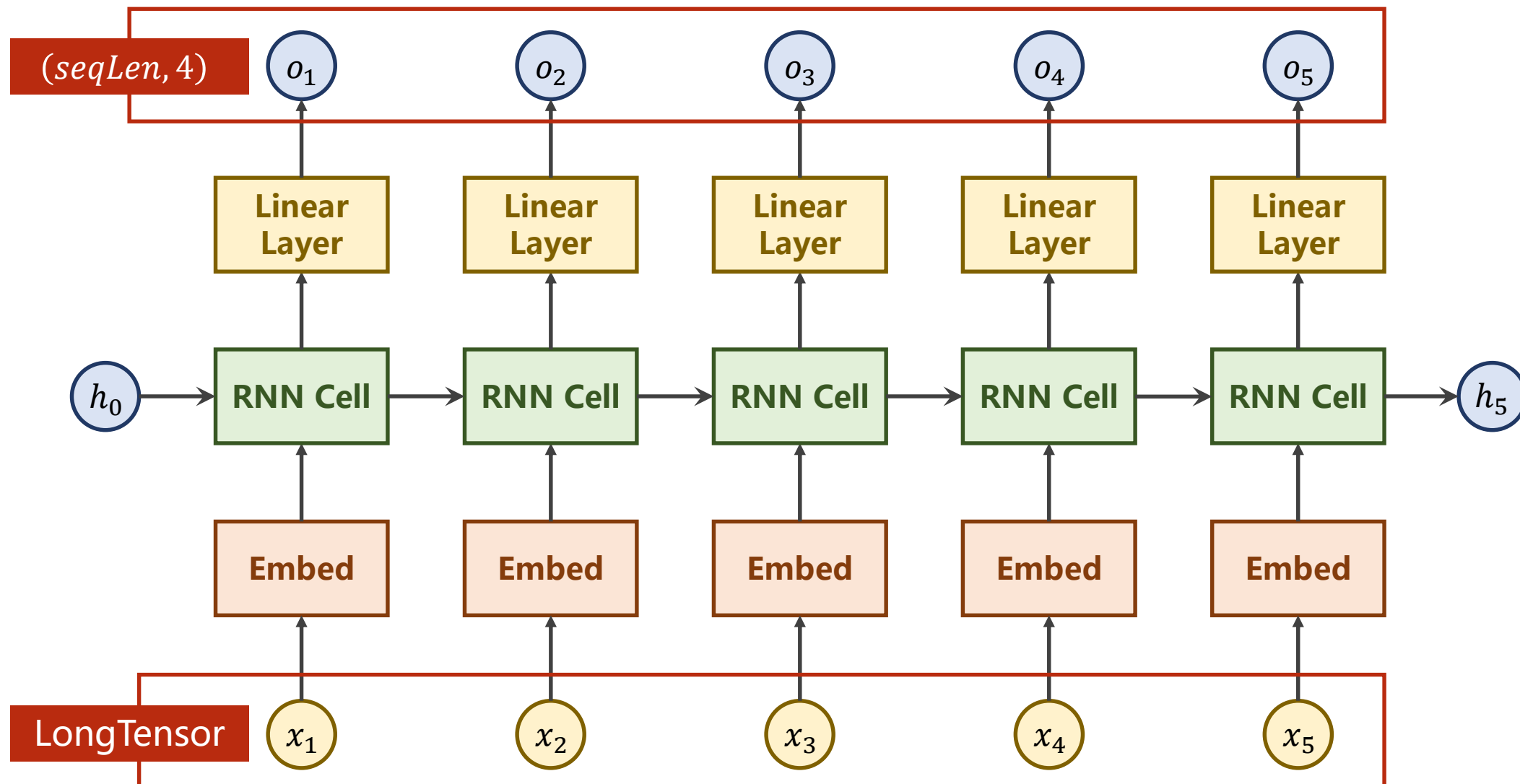
Embedding in PyTorch



Embedding in PyTorch



Example 12-3 Using embedding and linear layer



Example 12-3 Using embedding and linear layer

```
class torch.nn.Embedding(num_embeddings, embedding_dim, padding_idx=None, max_norm=None,
                        norm_type=2, scale_grad_by_freq=False, sparse=False, _weight=None) \[source\]
```

A simple lookup table that stores embeddings of a fixed dictionary and size.

This module is often used to store word embeddings and retrieve them using indices. The input to the module is a list of indices, and the output is the corresponding word embeddings.

Parameters:

- `num_embeddings` (*int*) – size of the dictionary of embeddings
- `embedding_dim` (*int*) – the size of each embedding vector
- `padding_idx` (*int, optional*) – If given, pads the output with the embedding vector at

Shape:

- Input: LongTensor of arbitrary shape containing the indices to extract
- Output: $(*, \text{embedding_dim})$, where $*$ is the input shape

- `sparse` (*bool, optional*) – if `True`, gradient w.r.t. weight matrix will be a sparse tensor. See Notes for more details regarding sparse gradients.

Example 12-3 Using embedding and linear layer

```
class torch.nn.Linear(in_features, out_features, bias=True) \[source\]
```

Applies a linear transformation to the incoming data: $y = Ax + b$

Parameters:

- **in_features** – size of each input sample
- **out_features** – size of each output sample
- **bias** – If set to False, the layer will not learn an additive bias. Default: `True`

Shape:

- Input: $(N, *, in_features)$ where $*$ means any number of additional dimensions
- Output: $(N, *, out_features)$ where all but the last dimension are the same shape as the input.

Example 12-3 Using embedding and linear layer

```
class torch.nn.CrossEntropyLoss (weight=None, size_average=True, ignore_index=-100, reduce=True)  
[source]
```

This criterion combines `nn.LogSoftmax()` and `nn.NLLLoss()` in one single class.

Shape:

- Input: (N, C) where $C = \text{number of classes}$, or $(N, C, d_1, d_2, \dots, d_K)$ with $K \geq 2$ in the case of K -dimensional loss.
- Target: (N) where each value is $0 \leq \text{targets}[i] \leq C - 1$, or $(N, d_1, d_2, \dots, d_K)$ with $K \geq 2$ in the case of K -dimensional loss.
- Output: scalar. If reduce is `False`, then the same size as the target: (N) , or $(N, d_1, d_2, \dots, d_K)$ with $K \geq 2$ in the case of K -dimensional loss.

Example 12-3 Using embedding and linear layer

```
class Model(torch.nn.Module):
    def __init__(self):
        super(Model, self).__init__()
        self.emb = torch.nn.Embedding(input_size, embedding_size)
        self.rnn = torch.nn.RNN(input_size=embedding_size,
                                hidden_size=hidden_size,
                                num_layers=num_layers,
                                batch_first=True)

        self.fc = torch.nn.Linear(hidden_size, num_class)

    def forward(self, x):
        hidden = torch.zeros(num_layers, x.size(0), hidden_size)
        x = self.emb(x) # (batch, seqLen, embeddingSize)
        x, _ = self.rnn(x, hidden)
        x = self.fc(x)
        return x.view(-1, num_class)
```

Lookup matrix of Embedding:
(inputSize, embeddingSize)

embeddingSize

inputSize

-1.1195	-0.3138	-1.4441	-0.4976	1.1591
0.9164	1.2496	0.2717	-0.8645	1.0408
0.3896	1.6515	-0.9640	1.2836	1.2430
2.3852	1.6643	-1.0360	-1.3234	-1.3370

Example 12-3 Using embedding and linear layer

```
class Model(torch.nn.Module):
    def __init__(self):
        super(Model, self).__init__()
        self.emb = torch.nn.Embedding(input_size, embedding_size)
        self.rnn = torch.nn.RNN(input_size=embedding_size,
                                hidden_size=hidden_size,
                                num_layers=num_layers,
                                batch_first=True)
        self.fc = torch.nn.Linear(hidden_size, num_class)

    def forward(self, x):
        hidden = torch.zeros(num_layers, x.size(0), hidden_size)
        x = self.emb(x) # (batch, seqLen, embeddingSize)
        x, _ = self.rnn(x, hidden)
        x = self.fc(x)
        return x.view(-1, num_class)
```

Input should be LongTensor:

(batchSize, seqLen)

Output with shape:

(batchSize, seqLen, embeddingSize)

Notice: batch FIRST

Example 12-3 Using embedding and linear layer

```
class Model(torch.nn.Module):
    def __init__(self):
        super(Model, self).__init__()
        self.emb = torch.nn.Embedding(input_size, embedding_size)
        self.rnn = torch.nn.RNN(input_size=embedding_size,
                                hidden_size=hidden_size,
                                num_layers=num_layers,
                                batch_first=True)
        self.fc = torch.nn.Linear(hidden_size, num_class)

    def forward(self, x):
        hidden = torch.zeros(num_layers, x.size(0), hidden_size)
        x = self.emb(x) # (batch, seqLen, embeddingSize)
        x, _ = self.rnn(x, hidden)
        x = self.fc(x)
        return x.view(-1, num_class)
```

Input of RNN:

(batchSize, seqLen, embeddingSize)

Output of RNN:

(batchSize, seqLen, hiddenSize)

Example 12-3 Using embedding and linear layer

```
class Model(torch.nn.Module):
    def __init__(self):
        super(Model, self).__init__()
        self.emb = torch.nn.Embedding(input_size, embedding_size)
        self.rnn = torch.nn.RNN(input_size=embedding_size,
                                hidden_size=hidden_size,
                                num_layers=num_layers,
                                batch_first=True)
        self.fc = torch.nn.Linear(hidden_size, num_class)

    def forward(self, x):
        hidden = torch.zeros(num_layers, x.size(0), hidden_size)
        x = self.emb(x) # (batch, seqLen, embeddingSize)
        x, _ = self.rnn(x, hidden)
        x = self.fc(x)
        return x.view(-1, num_class)
```

Shape:

- Input: $(N, *, in_features)$ where
- Output: $(N, *, out_features)$ where $out_features$ is the input.

Input of FC Layer:

(batchSize, seqLen, hiddenSize)

Output of FC Layer:

(batchSize, seqLen, numClass)

Example 12-3 Using embedding and linear layer

```
class Model(torch.nn.Module):
    def __init__(self):
        super(Model, self).__init__()
        self.emb = torch.nn.Embedding(input_size, embedding_size)
        self.rnn = torch.nn.RNN(input_size=embedding_size,
                                hidden_size=hidden_size,
                                num_layers=num_layers,
                                batch_first=True)
        self.fc = torch.nn.Linear(hidden_size, num_class)

    def forward(self, x):
        hidden = torch.zeros(num_layers, x.size(0), hidden_size)
        x = self.emb(x) # (batch, seqLen, embeddingSize)
        x, _ = self.rnn(x, hidden)
        x = self.fc(x)
        return x.view(-1, num_class)
```

Shape:

- Input: (N, C) where $C = (N, C, d_1, d_2, \dots)$
- Target: (N) where $N = (N, d_1, d_2, \dots)$

Reshape result to use Cross Entropy

Loss:

$(batchSize \times seqLen, numClass)$

Example 12-3 Using embedding and linear layer

```
# parameters  
num_class = 4  
input_size = 4  
hidden_size = 8  
embedding_size = 10  
num_layers = 2  
batch_size = 1  
seq_len = 5
```


Example 12-3 Using embedding and linear layer

```
idx2char = ['e', 'h', 'l', 'o']  
x_data = [[1, 0, 2, 2, 3]] # (batch, seq_len)  
y_data = [3, 1, 2, 3, 2] # (batch * seq_len)  
  
inputs = torch.LongTensor(x_data)  
labels = torch.LongTensor(y_data)
```

Input should be LongTensor:

(batchSize, seqLen)

Target should be LongTensor:

(batchSize × seqLen)

```
# parameters  
num_class = 4  
input_size = 4  
hidden_size = 8  
embedding_size = 10  
num_layers = 2  
batch_size = 1  
seq_len = 5
```

Example 12-3 Using embedding and linear layer

```
net = Model()  
  
criterion = torch.nn.CrossEntropyLoss()  
optimizer = torch.optim.Adam(net.parameters(), lr=0.05)
```

Example 12-3 Using embedding and linear layer

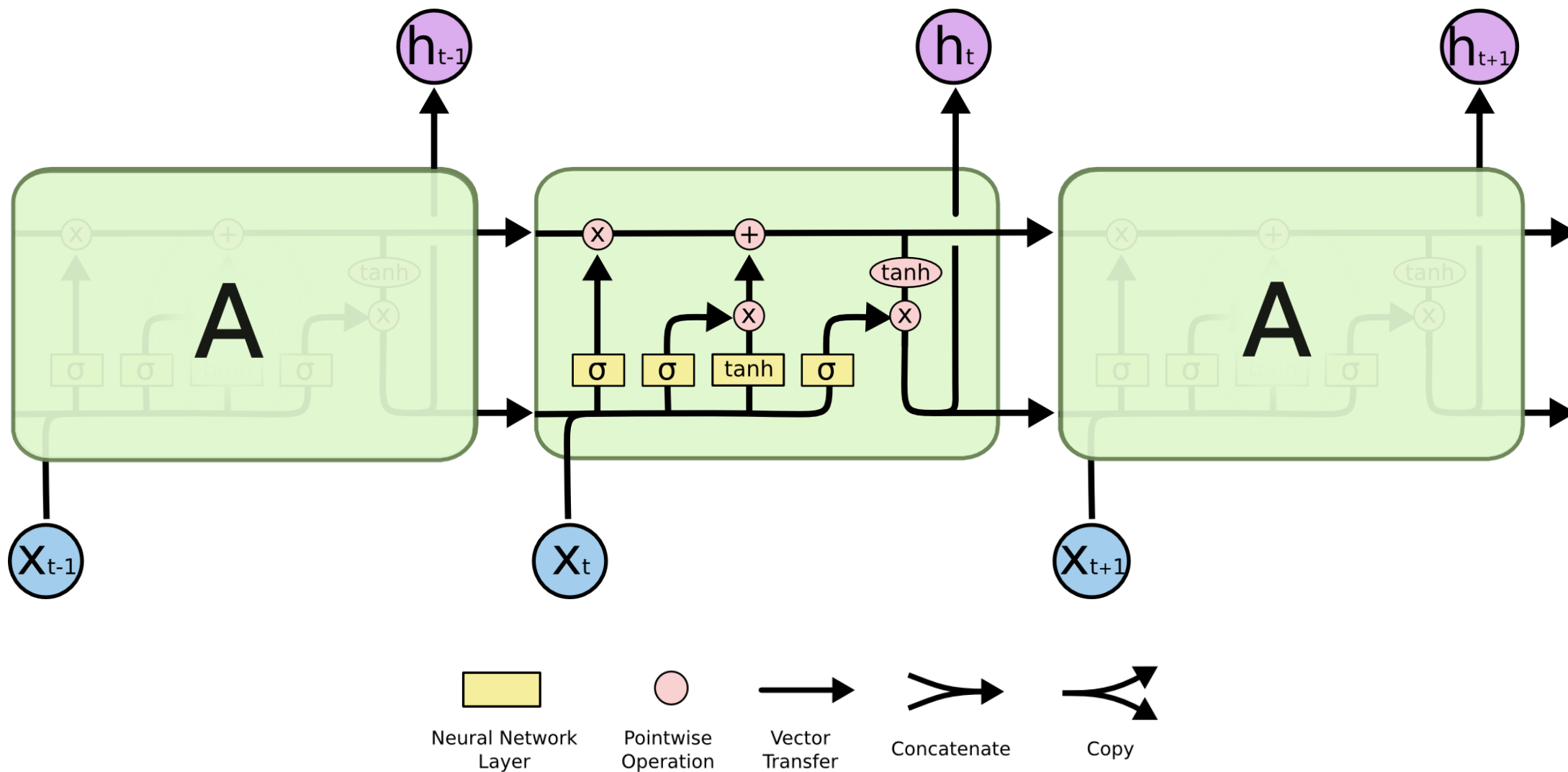
```
for epoch in range(15):
    optimizer.zero_grad()
    outputs = net(inputs)
    loss = criterion(outputs, labels)
    loss.backward()
    optimizer.step()

    _, idx = outputs.max(dim=1)
    idx = idx.data.numpy()
    print('Predicted: ', ''.join([idx2char[x] for x in idx]), end='')
    print(', Epoch [%d/15] loss = %.3f' % (epoch + 1, loss.item()))
```

Example 12-3 Using embedding and linear layer

```
Predicted: llll, Epoch [1/15] loss = 1.412
Predicted: llll, Epoch [2/15] loss = 1.038
Predicted: lhll, Epoch [3/15] loss = 0.799
Predicted: ohlol, Epoch [4/15] loss = 0.652
Predicted: ohloo, Epoch [5/15] loss = 0.548
Predicted: ohlol, Epoch [6/15] loss = 0.459
Predicted: ohlol, Epoch [7/15] loss = 0.381
Predicted: ohlol, Epoch [8/15] loss = 0.313
Predicted: ohlol, Epoch [9/15] loss = 0.248
Predicted: ohlol, Epoch [10/15] loss = 0.188
Predicted: ohlol, Epoch [11/15] loss = 0.136
Predicted: ohlol, Epoch [12/15] loss = 0.098
Predicted: ohlol, Epoch [13/15] loss = 0.072
Predicted: ohlol, Epoch [14/15] loss = 0.055
Predicted: ohlol, Epoch [15/15] loss = 0.043
```

Exercise 12 – 1 Using LSTM



Exercise 12 – 1 Using LSTM

```
class torch.nn.LSTM(*args, **kwargs) [source]
```

Applies a multi-layer long short-term memory (LSTM) RNN to an input sequence.

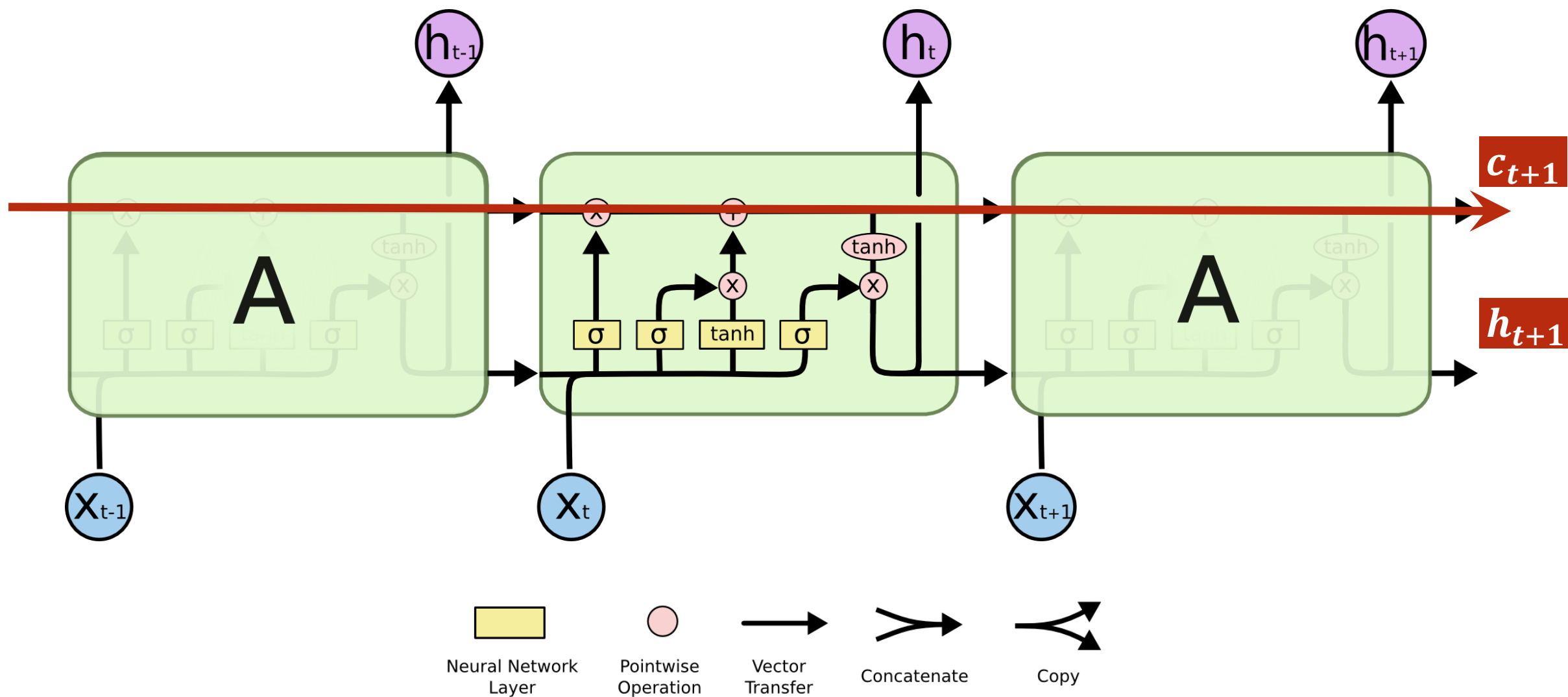
For each element in the input sequence, each layer computes the following function:

$$\begin{aligned}i_t &= \sigma(W_{ii}x_t + b_{ii} + W_{hi}h_{(t-1)} + b_{hi}) \\f_t &= \sigma(W_{if}x_t + b_{if} + W_{hf}h_{(t-1)} + b_{hf}) \\g_t &= \tanh(W_{ig}x_t + b_{ig} + W_{hg}h_{(t-1)} + b_{hg}) \\o_t &= \sigma(W_{io}x_t + b_{io} + W_{ho}h_{(t-1)} + b_{ho}) \\c_t &= f_t c_{(t-1)} + i_t g_t \\h_t &= o_t \tanh(c_t)\end{aligned}$$

where h_t is the hidden state at time t , c_t is the cell state at time t , x_t is the input at time t , $h_{(t-1)}$ is the hidden state of the previous layer at time $t-1$ or the initial hidden state at time 0, and i_t , f_t , g_t , o_t are the input, forget, cell, and output gates, respectively. σ is the sigmoid function.

<https://pytorch.org/docs/stable/nn.html#lstm>

Exercise 12 – 1 Using LSTM



Exercise 12 – 1 Using LSTM

Inputs: input, (h_0, c_0)

- **input** of shape $(seq_len, batch, input_size)$: tensor containing the features of the input sequence. The input can also be a packed variable length sequence. See `torch.nn.utils.rnn.pack_padded_sequence()` OR `torch.nn.utils.rnn.pack_sequence()` for details.
- **h_0** of shape $(num_layers * num_directions, batch, hidden_size)$: tensor containing the initial hidden state for each element in the batch.
- **c_0** of shape $(num_layers * num_directions, batch, hidden_size)$: tensor containing the initial cell state for each element in the batch.

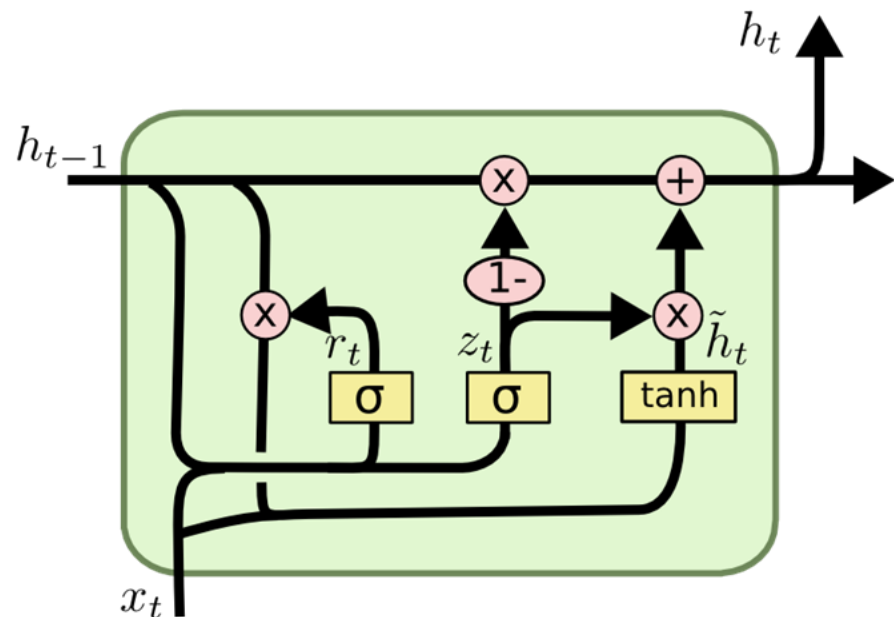
If (h_0, c_0) is not provided, both **h_0** and **c_0** default to zero.

Outputs: output, (h_n, c_n)

- **output** of shape $(seq_len, batch, hidden_size * num_directions)$: tensor containing the output features (h_t) from the last layer of the LSTM, for each t. If a `torch.nn.utils.rnn.PackedSequence` has been given as the input, the output will also be a packed sequence.
- **h_n** of shape $(num_layers * num_directions, batch, hidden_size)$: tensor containing the hidden state for $t = seq_len$
- **c_n** of shape $(num_layers * num_directions, batch, hidden_size)$: tensor containing the cell state for $t = seq_len$

<https://pytorch.org/docs/stable/nn.html#lstm>

Exercise 12 – 2 Using GRU

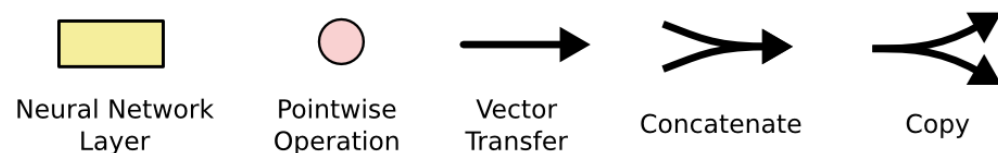


$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$



Exercise 12 – 2 Using GRU

```
class torch.nn.GRU(*args, **kwargs) \[source\]
```

Applies a multi-layer gated recurrent unit (GRU) RNN to an input sequence.

For each element in the input sequence, each layer computes the following function:

$$r_t = \sigma(W_{ir}x_t + b_{ir} + W_{hr}h_{(t-1)} + b_{hr})$$

$$z_t = \sigma(W_{iz}x_t + b_{iz} + W_{hz}h_{(t-1)} + b_{hz})$$

$$n_t = \tanh(W_{in}x_t + b_{in} + r_t(W_{hn}h_{(t-1)} + b_{hn}))$$

$$h_t = (1 - z_t)n_t + z_th_{(t-1)}$$

where h_t is the hidden state at time t , x_t is the input at time t , $h_{(t-1)}$ is the hidden state of the previous layer at time $t-1$ or the initial hidden state at time 0, and r_t, z_t, n_t are the reset, update, and new gates, respectively. σ is the sigmoid function.

<https://pytorch.org/docs/stable/nn.html#gru>

Exercise 12 – 2 Using GRU

Inputs: input, h_0

- **input** of shape $(seq_len, batch, input_size)$: tensor containing the features of the input sequence. The input can also be a packed variable length sequence. See `torch.nn.utils.rnn.pack_padded_sequence()` for details.
- **h_0** of shape $(num_layers * num_directions, batch, hidden_size)$: tensor containing the initial hidden state for each element in the batch. Defaults to zero if not provided.

Outputs: output, h_n

- **output** of shape $(seq_len, batch, hidden_size * num_directions)$: tensor containing the output features h_t from the last layer of the GRU, for each t . If a `torch.nn.utils.rnn.PackedSequence` has been given as the input, the output will also be a packed sequence.
- **h_n** of shape $(num_layers * num_directions, batch, hidden_size)$: tensor containing the hidden state for $t = seq_len$

<https://pytorch.org/docs/stable/nn.html#gru>



PyTorch Tutorial

12. Basic RNN