

Experiment - 5

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ECE1018- Lab

L21+L22

1. Fourier series of a square wave

Period = 2ms

Peak-to-peak value = 2V

Average value = 0V

$$x(t) = \frac{4}{\pi} \sum_{n=0}^{\infty} \frac{1}{2n+1} \sin((2n+1)2\pi f_0 t)$$

2. Fourier series of a sawtooth wave

$$x(t) = \frac{2}{\pi} \sum_{n=0}^{\infty} (-1)^{n+1} (\sin n\omega t / n)$$

3. Fourier series of a triangular wave

$$x(t) = \frac{8}{\pi^2} \sum_{n=0}^{\infty} (-1)^n [\sin((2n+1)\omega t) / (2n+1)^2]$$

4. Find the approximate CFS harmonic function of a periodic signal $x(t)$ where

$$x(t) = \sqrt{1-t^2}, \quad -1 \leq t \leq 1$$

Should not use built-in functions

13/9/19

Experiment - 6

classmate

Date _____

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→ To solve a second order linear differential equation, using laplace transform (13/9/19)

- Laplace transform of a function $f(t)$ is defined as,

$$F(s) = L\{f(t)\} = \int_0^{\infty} e^{-st} f(t) dt, \quad (1)$$

provided the integral exists

- $\text{laplace}(f)$: To find laplace transform of any function f . Return is default in 's'
- $\text{ilaplace}(f)$: To find inverse laplace transform of function f . Return is default in 't'
- $\text{heaviside}(t-a)$: To input heaviside's unit step function $u_n(t) = h(t-a)$
- $\text{dirac}(t-a)$: To input dirac delta function δ
- $\text{laplace}(f,t,w)$: Second and third variables are the input variable and output variable respectively.

1. Find the laplace transform of

$$f(t) = \begin{cases} t^2 & t < 2 \\ t-1 & 2 < t < 3 \\ 7 & t > 3 \end{cases}$$

2. Find the inverse laplace transform of e^{-s}

3 Solve the initial value problem

$$\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + 5y = e^{-t}\sin t$$

where $y(0) = 0$ $y'(0) = 1$

ans

Screenshots 5, 6, 7

1. Answer

Enter function of t :

$$(t^2)^* (\text{heaviside}(t) - \text{heaviside}(t-2)) + \\ (t-1)^* (\text{heaviside}(t-2) - \text{heaviside}(t-3)) + \\ 7^* \text{heaviside}(t-3)$$

$$\begin{aligned} L\{f(t)\} &= (7^* \exp(-3^*s))/s - (4^* \exp(-2^*s))/s - \\ &\quad (4^* \exp(-2^*s))/s^2 - (2^* \exp(-2^*s))/s^3 + \\ &\quad 2/s^3 - (\exp(-3^*s)^* (2^*s - \exp(s) - s^* \exp(s) + 1))/s^2 \\ &= 7e^{-3s}/s - 4e^{-2s}/s - 4e^{-2s}/s^2 \\ &\quad - 2e^{-2s}/s^3 + 2/s^3 - (e^{-3s}[2s - e^s - se^s + 1])/s^2 \\ &= \end{aligned}$$

Experiment – 5

Code:

```
Editor - C:\Users\18BIS0043\Documents\MATLAB\E5.m
E5.m x +
1 -   clc
2 -   clear all
3 -   close all
4 -   syms c1 c2 x m
5 -   Co = input('Enter the coefficients [a,b,c]: ');
6 -   f = input('Enter the RHS function f(x): ');
7 -   a = Co(1);
8 -   b = Co(2);
9 -   c = Co(3);
10 -  aux = a*m^2 + b*m + c;
11 -  m = solve(aux);
12 -  D = b^2 - 4*a*c;
13
```

```
Editor - C:\Users\18BIS0043\Documents\MATLAB\E5.m
E5.m x +
13
14 -   if(D>0)
15 -       % Roots are real and different
16 -       y1 = exp(m(1)*x);
17 -       y2 = exp(m(2)*x);
18 -   elseif(D==0)
19 -       % Roots are real and equal
20 -       y1 = exp(m(1)*x);
21 -       y2 = exp(m(1)*x);
22 -   else
23 -       % Roots are imaginary
24 -       alpha = real(m(1));
25 -       beta = imag(m(1));
26 -       y1 = exp(alpha*x)*cos(beta*x);
27 -       y2 = exp(alpha*x)*sin(beta*x);
28 -   end
```

```

29
30 -   yc = c1*y1 + c2*y2; %CF
31 -   fx = f/a;
32 -   W = y1*diff(y2,x) - y2*diff(y1,x);
33 -   u = int(-y2*fx/W,x);
34 -   v = int(y1*fx/W,x);
35 -   yp = y1*u + y2*v; %PI
36 -   y_g = yc+yp;
37 -   ch = input('Enter "1" if initial conditions, else "2": ');
38
39
38
39 -   if(ch==1)
40 -       cn = input('Enter the initial conditions [x0,y(x),Dy(x)]: ');
41 -       dy_g = diff(y_g);
42 -       eq1 = (subs(y_g,x,cn(1))-cn(2));
43 -       eq2 = (subs(dy_g,x,cn(1))-cn(3));
44 -       [c1 c2] = solve(eq1,eq2);
45 -       y = simplify(subs(y_g));
46 -       disp('The Complete solution is: ');
47 -       disp(y);
48 -       ezplot(y,[cn(1),cn(1)+2]);
49 -       grid on;
50 -   else
51 -       y = simplify(y_g);
52 -       disp('The General solution is: ');
53 -       disp(y);
54 -   end
55

```

Answer - 2:

Command Window

New to MATLAB? See resources for [Getting Started](#).

```

Enter the coefficients [a,b,c]: [1 0 1]
Enter the RHS function f(x): sec(x)*tan(x)
Enter "1" if initial conditions, else "2": 2
The General solution is:
(log(tan(x)^2 + 1)*sin(x))/2 - sin(x) + c1*cos(x) - c2*sin(x) + x*cos(x)

```

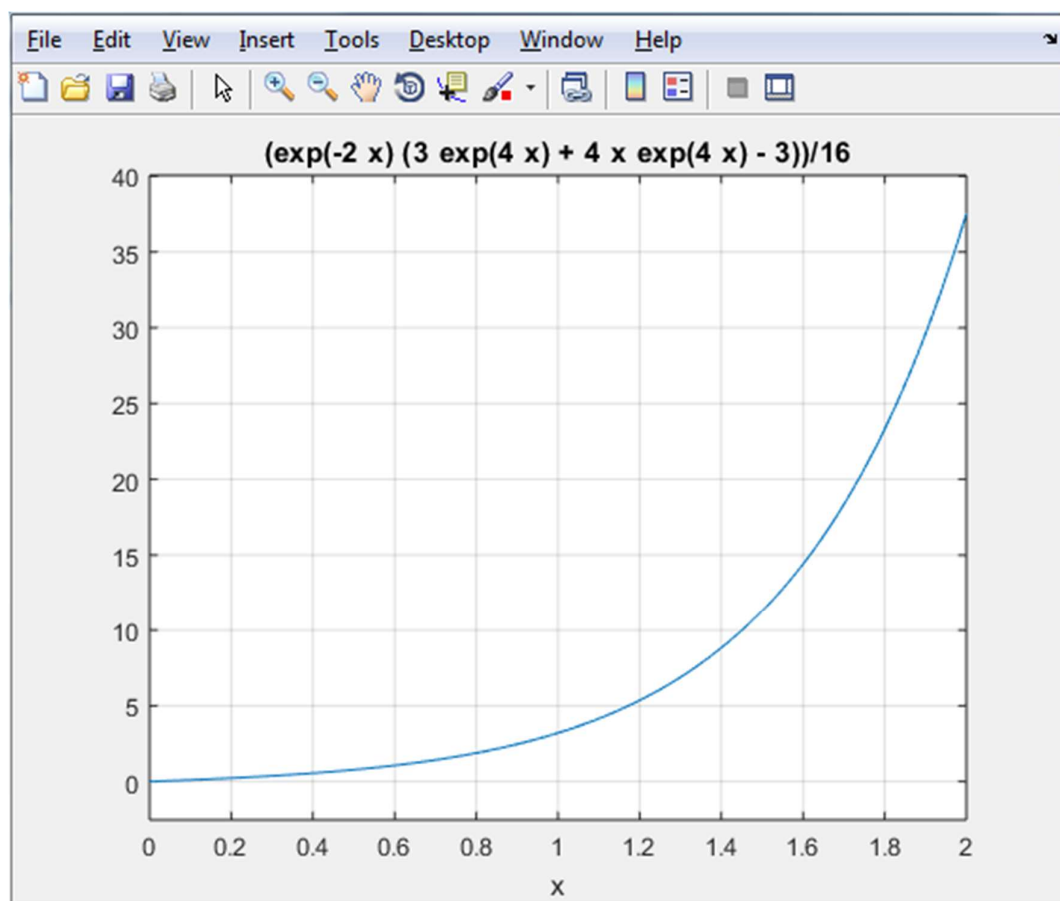
f_x >>

Answer - 1:

Command Window

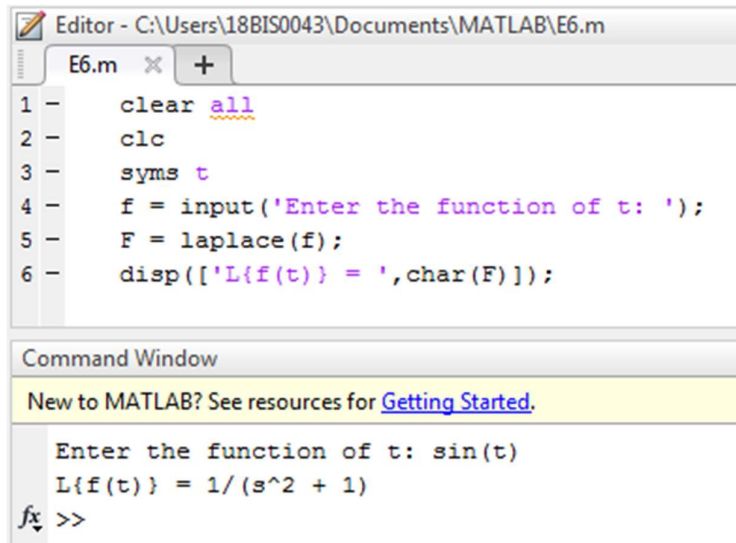
```
Enter the coefficients [a,b,c]: [1 0 -4]
Enter the RHS function f(x): exp(2*x);
Enter "1" if initial conditions, else "2": 1
Enter the initial conditions [x0,y(x),Dy(x)]: [0 0 1]
The Complete solution is:
(exp(-2*x)*(3*exp(4*x) + 4*x*exp(4*x) - 3))/16
```

f_x >>



Experiment – 6

Code – Laplace transform with example:



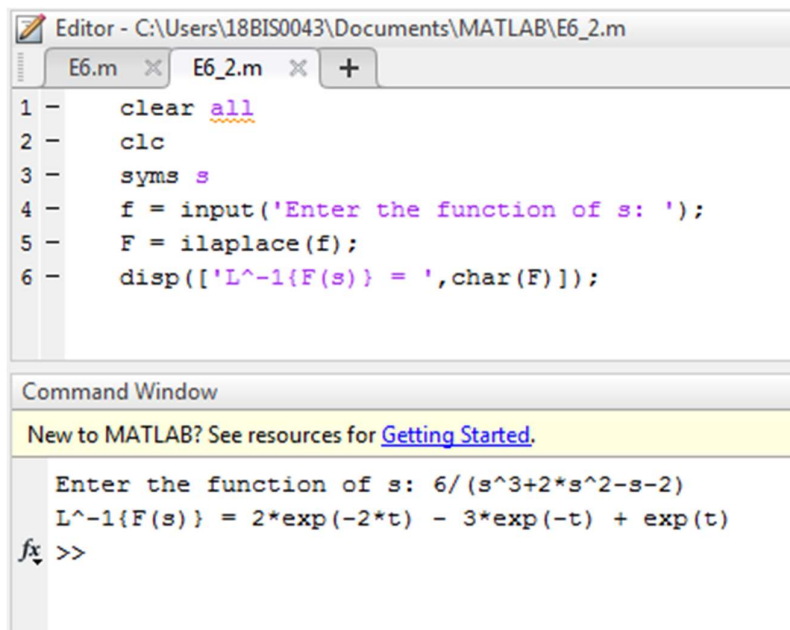
The image shows a MATLAB Editor window titled 'Editor - C:\Users\18BIS0043\Documents\MATLAB\E6.m'. It contains a script with the following code:

```
1 - clear all
2 - clc
3 - syms t
4 - f = input('Enter the function of t: ');
5 - F = laplace(f);
6 - disp(['L{f(t)} = ',char(F)]);
```

Below the editor is the Command Window. It displays a message: 'New to MATLAB? See resources for [Getting Started.](#)'. Below that, it shows the input and output of the script:

```
Enter the function of t: sin(t)
L{f(t)} = 1/(s^2 + 1)
fx >>
```

Code – Inverse Laplace transform with example:



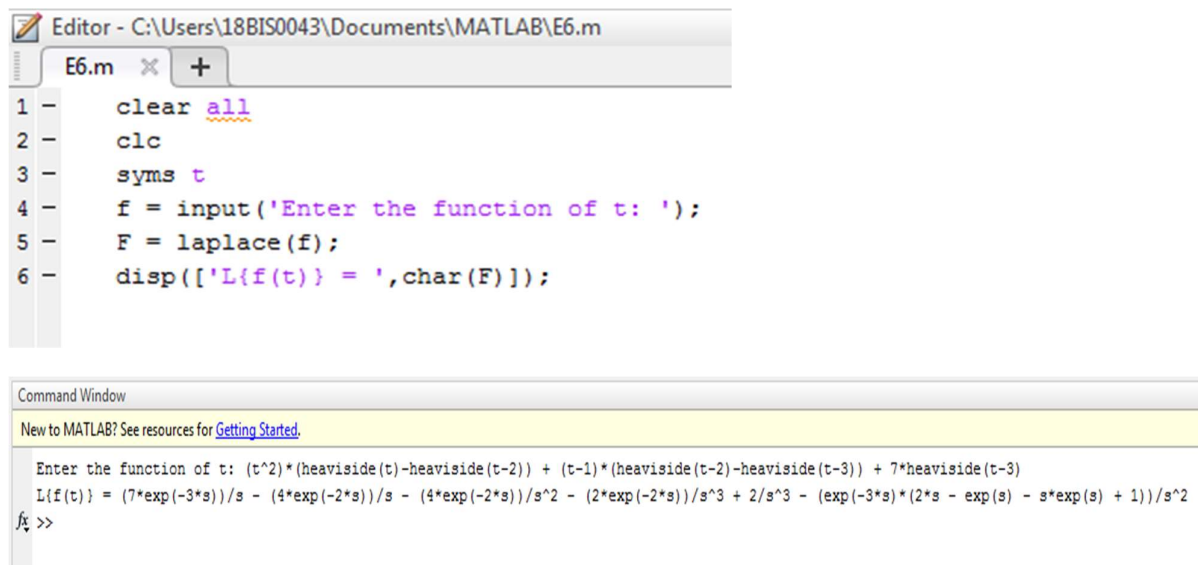
The image shows a MATLAB Editor window titled 'Editor - C:\Users\18BIS0043\Documents\MATLAB\E6_2.m'. It contains a script with the following code:

```
1 - clear all
2 - clc
3 - syms s
4 - f = input('Enter the function of s: ');
5 - F = ilaplace(f);
6 - disp(['L^-1{F(s)} = ',char(F)]);
```

Below the editor is the Command Window. It displays a message: 'New to MATLAB? See resources for [Getting Started.](#)'. Below that, it shows the input and output of the script:

```
Enter the function of s: 6/(s^3+2*s^2-s-2)
L^-1{F(s)} = 2*exp(-2*t) - 3*exp(-t) + exp(t)
fx >>
```

Answer – 1:



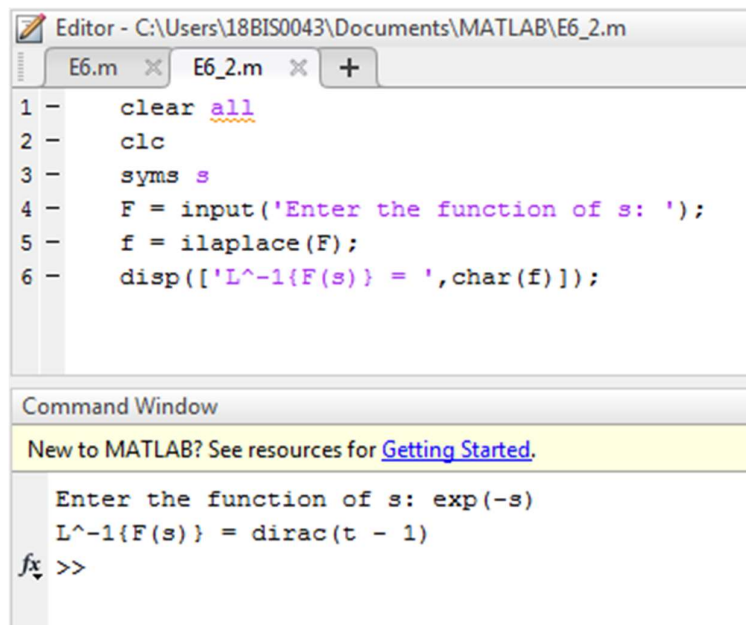
The image shows a MATLAB Editor window titled 'Editor - C:\Users\18BIS0043\Documents\MATLAB\E6.m'. The code in the editor is as follows:

```
1 - clear all
2 - clc
3 - syms t
4 - f = input('Enter the function of t: ');
5 - F = laplace(f);
6 - disp(['L{f(t)} = ',char(F)]);
```

Below the editor is the Command Window. It displays the prompt 'Enter the function of t:' followed by the input: $(t^2)*(heaviside(t)-heaviside(t-2)) + (t-1)*(heaviside(t-2)-heaviside(t-3)) + 7*heaviside(t-3)$. The output shows the Laplace transform: $L\{f(t)\} = (7*\exp(-3*s))/s - (4*\exp(-2*s))/s - (4*\exp(-2*s))/s^2 - (2*\exp(-2*s))/s^3 + 2/s^3 - (\exp(-3*s)*(2*s - \exp(s) - s*\exp(s) + 1))/s^2$. The Command Window prompt is $f_x >>$.

Solution written in notebook also...

Answer – 2:



The image shows a MATLAB Editor window titled 'Editor - C:\Users\18BIS0043\Documents\MATLAB\E6_2.m'. The code in the editor is as follows:

```
1 - clear all
2 - clc
3 - syms s
4 - F = input('Enter the function of s: ');
5 - f = ilaplace(F);
6 - disp(['L^-1{F(s)} = ',char(f)]);
```

Below the editor is the Command Window. It displays the prompt 'Enter the function of s:' followed by the input: $\exp(-s)$. The output shows the inverse Laplace transform: $L^{-1}\{F(s)\} = \text{dirac}(t - 1)$. The Command Window prompt is $f_x >>$.

Answer – 3:

```
Editor - C:\Users\18BIS0043\Documents\MATLAB\E6_3.m
E6.m  E6_2.m  E6_3.m  +
1 - clear all
2 - clc
3 - syms s t y(t) Y
4 - dy(t) = diff(y(t),1);
5 - d2y(t) = diff(y(t),2);
6 - F = input('Enter the coefficients in the form [a,b,c]: ');
7 - A = F(1);
8 - B = F(2);
9 - C = F(3);

10
11 - non = input('Enter the Non-homogenous part f(x): ');
12 - eq1 = A*d2y(t) + B*dy(t) + C*y(t) - non;
13 - LT = laplace(eq1,t,s);
14 - Initial = input('Enter the initial condition in the form [y(0),Dy(0)]: ');
15 - y0 = Initial(1);
16 - dy0 = Initial(2);
17

18 - LT = subs(LT,{'laplace(y(t),t,s)','y(0)','D(y)(0)'},{Y,y0,dy0});
19 - final_eq = collect(LT,Y);
20 - Y = simplify(solve(final_eq,Y));
21 - yt = simplify(ilaplace(Y,s,t));
22 - disp('The solution of the differential equation y(t) = ');
23 - disp(yt);
24 - ezplot(yt,[y0,y0+2]);
25 - grid on;
```

I/O:

Command Window

New to MATLAB? See resources for [Getting Started](#).

Enter the coefficients in the form [a,b,c]: [1 2 5]

Enter the Non-homogenous part f(x): $\exp(-t)*\sin(t)$

Enter the initial condition in the form [y(0),Dy(0)]: [0 1]

The solution of the differential equation y(t) =

$(\exp(-t) * (\sin(2*t) + \sin(t))) / 3$

f_x >>

Graph:

