

Uniswap Arbitrage Analysis

0.Foreword

Uniswap is the most popular dex with more than 11000 trading pairs and 2B dollars liquidity. Where there is a market, there are arbitrage opportunities. On uniswap we can trade coin A for coin D follow a given path, e.g. A->B->C->D, A and D can also be the same coin, which means, you can trade A for A follow a given path, and if you are lucky, you can get more A than the original input amount! So how do we find such a path and determine the optimal input amount for maximum profit? Here we go:

1.Arbitrage problem alalysis

In order to perform an arbitrage, we need to figure out 2 things:

- How to find the best path: from A->?->?->...->A
- How to find the optimal input amount?

1.1 Path finding

Each coin is a vertex of a graph, and each trading pair is an edge in the graph, now the problem is how to find a circle in such a graph? This is a classic graph problem, we can use depth first search(DFS) to solve it, with DFS, we can also control the max path length, which is import for an arbitrage since longer path requires more gas! Here is a sample code:

```
def findArb(pairs, tokenIn, tokenOut, maxHops, currentPairs, path, circles):
    for i in range(len(pairs)):
        newPath = path.copy()
        pair = pairs[i]
        if not pair['token0']['address'] == tokenIn['address'] and not
pair['token1']['address'] == tokenIn['address']:
            continue
        if pair['reserve0']/pow(10, pair['token0']['decimal']) < 1 or
pair['reserve1']/pow(10, pair['token1']['decimal']) < 1:
            continue
        if tokenIn['address'] == pair['token0']['address']:
            tempOut = pair['token1']
        else:
            tempOut = pair['token0']
        newPath.append(tempOut)
        if tempOut['address'] == tokenOut['address'] and len(path) > 2:
            c = { 'route': currentPairs, 'path': newPath }
            circles.append(c)
        elif maxHops > 1 and len(pairs) > 1:
            pairsExcludingThisPair = pairs[:i] + pairs[i+1:]
```

```

        circles = findArb(pairsExcludingThisPair, tempOut, tokenOut,
maxHops-1, currentPairs + [pair], newPath, circles)
    return circles

```

1.2 Optimal input amount

Let's do a little recap on the uniswap constant function market maker(CFMM) model, assume there is a trading pair for coin A and B, reserve for A is R_0 , reserve for B is R_1 , now we use Δ_a amount of A to trade for Δ_b amount of B, assume the fee is $1 - r$, the following equation holds:

$$(R_0 + r\Delta_a)(R_1 - \Delta_b) = R_0 R_1$$

The equation means that the product of the reserves $R_0 R_1$ remains constant during the trade, this is why we call it constant function market maker.

Now assume we have found a circle path: A->B->C->A, how do we find the optimal input amount? This is an optimization problem:

$$\max(\Delta_a' - \Delta_a)$$

s. t.

$$R_n > 0, \Delta_n > 0$$

$$(R_0 + r\Delta_a)(R_1 - \Delta_b) = R_0 R_1 \quad (1)$$

$$(R_1' + r\Delta_b)(R_2 - \Delta_c) = R_1' R_2 \quad (2)$$

$$(R_2' + r\Delta_c)(R_3 - \Delta_a') = R_2' R_1' \quad (3)$$

Equation (1) holds during the trade from A to B, (2) holds during the trade from B to C, and (3) holds during the trade from C to A. It seems pretty simple since we only have 3 equations now, we can get the representation for Δ_a' in Δ_a , then calculate the derivative of $\Delta_a' - \Delta_a$ to find out what the optimal Δ_a is.

What if the path is longer? A->B->C->...->A. We need a general solution for arbitrary length path.

Consider the A->B->C situation, maybe there is not a trading pair directly from A to C, but with B as the bridge, we can trade A for C, we say there is a **virtual** trading pool for A and C, can we get the reserves parameter E_0, E_1 for this virtual pool?

All we need to do is find the representation for E_0, E_1 in R_0, R_1, R_1', R_2 , i.e. the pool parameters of A->B and B->C.

According to equation(1)(2), we have:

$$\Delta_b = \frac{R_1 r \Delta_a}{R_0 + r \Delta_a} \quad (4)$$

$$\Delta_c = \frac{R_2 r \Delta_b}{R_1' + r \Delta_b} \quad (5)$$

Replace Δ_b in (5) using (4), we have:

$$\Delta_c = \frac{\frac{R_0 R_1'}{R_1' + R_1 r} r \Delta_a}{\frac{r R_1 R_2}{R_1' + R_1 r} + r \Delta_a} \quad (6)$$

Comparing the form of (6) and (4) or (6) and (5), we have:

$$E_0 = \frac{R_0 R_1'}{R_1' + R_1 r}$$

$$E_1 = \frac{r R_1 R_2}{R_1' + R_1 r}$$

Now we have the parameters for virtual pool A->C, consider the path A->B->C->A, with the virtual pool, the path is now: A->C->A, we can further calculate the parameters for A->A, say E_a, E_b , if $E_a < E_b$, then there is an arbitrage opportunity. For arbitrary length path, we can calculate E_a, E_b iteratively.

Now we have the parameters E_a, E_b for this virtual pool from A->A constructed from the given path, we have:

$$\Delta_a' = \frac{E_a r \Delta_a}{E_0 + r \Delta_a}$$

$$f = \Delta_a' - \Delta_a$$

Here f is our profit, calculate its derivative, we can find the optimal input amount:

$$\Delta_a = \frac{\sqrt{E_a E_b r} - E_a}{r}$$

Code for path finding with optimal input amount calculation:

```
def findArb(pairs, tokenIn, tokenOut, maxHops, currentPairs, path, bestTrades, count=5):
    for i in range(len(pairs)):
        newPath = path.copy()
        pair = pairs[i]
        if not pair['token0']['address'] == tokenIn['address'] and not pair['token1']['address'] == tokenIn['address']:
            continue
        if pair['reserve0']/pow(10, pair['token0']['decimal']) < 1 or pair['reserve1']/pow(10, pair['token1']['decimal']) < 1:
            continue
        if tokenIn['address'] == pair['token0']['address']:
            tempOut = pair['token1']
        else:
            tempOut = pair['token0']
        newPath.append(tempOut)
        if tempOut['address'] == tokenOut['address'] and len(path) > 2:
            Ea, Eb = getEaEb(tokenOut, currentPairs + [pair])
            newTrade = { 'route': currentPairs + [pair], 'path': newPath, 'Ea': Ea, 'Eb': Eb }
            if Ea and Eb and Ea < Eb:
```

```

        newTrade['optimalAmount'] = getOptimalAmount(Ea, Eb)
        if newTrade['optimalAmount'] > 0:
            newTrade['outputAmount'] =
getAmountOut(newTrade['optimalAmount'], Ea, Eb)
            newTrade['profit'] = newTrade['outputAmount']-
newTrade['optimalAmount']
            newTrade['p'] = int(newTrade['profit']/pow(10,
tokenOut['decimal']))
            else:
                continue

            bestTrades = sortTrades(bestTrades, newTrade)
            bestTrades.reverse()
            bestTrades = bestTrades[:count]
        elif maxHops > 1 and len(pairs) > 1:
            pairsExcludingThisPair = pairs[:i] + pairs[i+1:]
            bestTrades = findArb(pairsExcludingThisPair, tempOut, tokenOut,
maxHops-1, currentPairs + [pair], newPath, bestTrades, count)
    return bestTrades

















```

2. Implementation

Ethereum block interval is 15 seconds, you have to do 3 things in 15 seconds:

- Update the reserves of each trading pair:
 - Small amount of trading pairs: batch request for the states of all trading pairs
 - Large amount of trading pairs: batch request, then parse every new block, if there is a event in (Swap, Sync, Mint, Burn), update the related pair reserves.
- Find the best path and optimal input amount:
 - Optimize DFS, explore other algorithms like bellman-ford, spfa, etc.
- Send the transaction:
 - Call UniswapV2Router02.getAmountsOut before you send your tx, confirm that you can really make a profit.

My test:

- › Swap 0.001837877803868271 Ether For 0.029600841309442325  TRB On  Uniswap
- › Swap 0.029600841309442325  TRB For 0.796430316556100961  DAI On  Uniswap
- › Swap 0.796430316556100961  DAI For 0.346048644105336869  RPL On  Uniswap
- › Swap 0.346048644105336869  RPL For 36.504804784313389539  BUIDL On  Uniswap
- › Swap 36.504804784313389539  BUIDL For 20.691932331434012957  OXT On  Uniswap
- › Swap 20.691932331434012957  OXT For 0.018473813918786526 Ether On  Uniswap

- › From   To Uniswap V2: TRB 3 For 0.001837877803868271 (\$0.65)  Wrapped Ethe... (WETH)
- › From Uniswap V2: TRB 3 To Uniswap V2: TRB-D... For 0.029600841309442325 (\$0.69)  Tellor Tribu... (TRB)
- › From Uniswap V2: TRB-D... To Uniswap V2: DAI-R... For 0.796430316556100961 (\$0.80)  Dai Stableco... (DAI)
- › From Uniswap V2: DAI-R... To Uniswap V2: RPL-B... For 0.346048644105336869 (\$0.74)  Rocket Pool (RPL)
- › From Uniswap V2: RPL-B... To Uniswap V2: OXT-B... For 36.504804784313389539 (\$63.59)  DFOHub (BUIDL)
- › From Uniswap V2: OXT-B... To Uniswap V2: OXT 2 For 20.691932331434012957 (\$6.23)  Orchid (OXT)
- › From Uniswap V2: OXT 2 To   For 0.018473813918786526 (\$6.53)  Wrapped Ethe... (WETH)

Didn't cover the gas fee though :(

3.Finally

Uniswap arbitrage is a competitive area, you may find it hard to make profit, but still, Defi is the haven for arbitraguers, you can also arbitrage between different exchanges like curve.fi, balancer.exchange, with flashloans, you can even borrow money to make arbitrage! Happy hacking :)

Don't ask me for code, my code sucks, but maybe I'll push my code someday.

Contact: ccyanxyz@gmail.com

Donation: 0x0af66d3641640755878F0d72A610FC2EEA856Cd6