

The FORSYDE system which performs the the Fast Fourier Transform can be defined in terms of atoms as:

$$\mathbf{fft}_S \ k \ vs = \mathbf{bitrev}_S((stage \diamond kern) \diamond vs) \quad (1)$$

where the constructors

$$stage \ wdt = \mathbf{concat}_S \circ (segment \diamond twiddles) \circ \mathbf{group}_S \ wdt \quad (2)$$

$$segment \ t = \mathbf{undual}_S \circ (butterfly \ t \diamond) \circ \mathbf{dual}_S \quad (3)$$

$$butterfly \ w = ((\lambda \ x_0 \ x_1 \rightarrow x_0 + wx_1, x_0 - wx_1) \triangle) \oplus \quad (4)$$

are aided by the number generators

$$kern = \mathbf{iterate}_S \ (\times 2) \ 2 \quad (5)$$

$$twiddles = (\mathbf{reverse}_S \circ \mathbf{bitrev}_S \circ \mathbf{take}_S \ (\mathbf{lgth}_S \ vs/2)) (wgen \diamond \langle 1.. \rangle) \quad (6)$$

$$wgen \ x = - \frac{2\pi(x-1)}{\mathbf{lgth}_S \ vs} \quad (7)$$