Quantum++

v1.0-rc3

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Contents

1 Quantum++ **1**

2 Namespace Index **3**

2.1 Namespace List 3

3 Hierarchical Index **5**

3.1 Class Hierarchy 5

4 Class Index **7**

4.1 Class List 7

5 File Index **11**

5.1 File List 11

6 Namespace Documentation **13**

6.1 qpp Namespace Reference 13

6.1.1 Detailed Description 22

6.1.2 Typedef Documentation 22

6.1.2.1 bigint 22

6.1.2.2 bra 22

6.1.2.3 cmat 22

6.1.2.4 cplx 22

6.1.2.5 dmat 22

6.1.2.6 dyn_col_vect 23

6.1.2.7 dyn_mat 23

6.1.2.8 dyn_row_vect 23

6.1.2.9 idx . . . 23
6.1.2.10 ket . . . 24
6.1.2.11 to_void . . . 24
6.1.3 Function Documentation . . . 24
6.1.3.1 apply() [1/5] . . . 24
6.1.3.2 apply() [2/5] . . . 25
6.1.3.3 apply() [3/5] . . . 25
6.1.3.4 apply() [4/5] . . . 26
6.1.3.5 apply() [5/5] . . . 26
6.1.3.6 applyCTRL() [1/2] . . . 27
6.1.3.7 applyCTRL() [2/2] . . . 27
6.1.3.8 avg() . . . 28
6.1.3.9 choi2kraus() . . . 28
6.1.3.10 choi2super() . . . 29
6.1.3.11 compperm() . . . 29
6.1.3.12 concurrence() . . . 30
6.1.3.13 contfrac2x() . . . 30
6.1.3.14 cor() . . . 30
6.1.3.15 cov() . . . 31
6.1.3.16 disp() [1/5] . . . 31
6.1.3.17 disp() [2/5] . . . 32
6.1.3.18 disp() [3/5] . . . 32
6.1.3.19 disp() [4/5] . . . 33
6.1.3.20 disp() [5/5] . . . 33
6.1.3.21 egcd() . . . 34
6.1.3.22 entanglement() [1/2] . . . 34
6.1.3.23 entanglement() [2/2] . . . 35
6.1.3.24 entropy() [1/2] . . . 35
6.1.3.25 entropy() [2/2] . . . 36
6.1.3.26 factors() . . . 36

6.1.3.27 gcd() [1/2] . . . 36
6.1.3.28 gcd() [2/2] . . . 37
6.1.3.29 gconcurrence() . . . 37
6.1.3.30 invperm() . . . 38
6.1.3.31 ip() [1/2] . . . 38
6.1.3.32 ip() [2/2] . . . 39
6.1.3.33 isprime() . . . 39
6.1.3.34 kraus2choi() . . . 39
6.1.3.35 kraus2super() . . . 40
6.1.3.36 lcm() [1/2] . . . 40
6.1.3.37 lcm() [2/2] . . . 41
6.1.3.38 load() . . . 41
6.1.3.39 loadMATLAB() [1/2] . . . 42
6.1.3.40 loadMATLAB() [2/2] . . . 42
6.1.3.41 lognegativity() [1/2] . . . 43
6.1.3.42 lognegativity() [2/2] . . . 44
6.1.3.43 marginalX() . . . 44
6.1.3.44 marginalY() . . . 44
6.1.3.45 measure() [1/9] . . . 45
6.1.3.46 measure() [2/9] . . . 45
6.1.3.47 measure() [3/9] . . . 46
6.1.3.48 measure() [4/9] . . . 46
6.1.3.49 measure() [5/9] . . . 47
6.1.3.50 measure() [6/9] . . . 47
6.1.3.51 measure() [7/9] . . . 48
6.1.3.52 measure() [8/9] . . . 49
6.1.3.53 measure() [9/9] . . . 49
6.1.3.54 measure_seq() [1/2] . . . 50
6.1.3.55 measure_seq() [2/2] . . . 51
6.1.3.56 modinv() . . . 51

6.1.3.57 modmul() . . . 52
6.1.3.58 modpow() . . . 52
6.1.3.59 negativity() [1/2] . . . 53
6.1.3.60 negativity() [2/2] . . . 53
6.1.3.61 omega() . . . 53
6.1.3.62 operator""""" _i() [1/2] . . . 55
6.1.3.63 operator""""" _i() [2/2] . . . 55
6.1.3.64 ptrace() [1/2] . . . 55
6.1.3.65 ptrace() [2/2] . . . 56
6.1.3.66 ptrace1() [1/2] . . . 56
6.1.3.67 ptrace1() [2/2] . . . 57
6.1.3.68 ptrace2() [1/2] . . . 57
6.1.3.69 ptrace2() [2/2] . . . 58
6.1.3.70 ptranspose() [1/2] . . . 58
6.1.3.71 ptranspose() [2/2] . . . 59
6.1.3.72 qmutualinfo() [1/2] . . . 59
6.1.3.73 qmutualinfo() [2/2] . . . 60
6.1.3.74 rand() [1/5] . . . 60
6.1.3.75 rand() [2/5] . . . 61
6.1.3.76 rand() [3/5] . . . 61
6.1.3.77 rand() [4/5] . . . 62
6.1.3.78 rand() [5/5] . . . 62
6.1.3.79 randH() . . . 63
6.1.3.80 randidx() . . . 63
6.1.3.81 randket() . . . 64
6.1.3.82 randkraus() . . . 64
6.1.3.83 randn() [1/4] . . . 64
6.1.3.84 randn() [2/4] . . . 65
6.1.3.85 randn() [3/4] . . . 65
6.1.3.86 randn() [4/4] . . . 66

6.1.3.87 randperm() . . . 66
6.1.3.88 randprime() . . . 67
6.1.3.89 randprob() . . . 67
6.1.3.90 randrho() . . . 67
6.1.3.91 randU() . . . 68
6.1.3.92 randV() . . . 68
6.1.3.93 renyi() [1/2] . . . 69
6.1.3.94 renyi() [2/2] . . . 69
6.1.3.95 save() . . . 70
6.1.3.96 saveMATLAB() [1/2] . . . 70
6.1.3.97 saveMATLAB() [2/2] . . . 71
6.1.3.98 schmidtA() [1/2] . . . 71
6.1.3.99 schmidtA() [2/2] . . . 72
6.1.3.100 schmidtB() [1/2] . . . 72
6.1.3.101 schmidtB() [2/2] . . . 72
6.1.3.102 schmidtcoeffs() [1/2] . . . 73
6.1.3.103 schmidtcoeffs() [2/2] . . . 73
6.1.3.104 schmidtprobs() [1/2] . . . 74
6.1.3.105 schmidtprobs() [2/2] . . . 74
6.1.3.106 sigma() . . . 75
6.1.3.107 super2choi() . . . 75
6.1.3.108 syspermute() [1/2] . . . 77
6.1.3.109 syspermute() [2/2] . . . 77
6.1.3.110 tsallis() [1/2] . . . 78
6.1.3.111 tsallis() [2/2] . . . 78
6.1.3.112 uniform() . . . 79
6.1.3.113 var() . . . 79
6.1.3.114 x2contfrac() . . . 79
6.1.4 Variable Documentation . . . 80
6.1.4.1 chop . . . 80

6.1.4.2 ee . . . 80
6.1.4.3 eps . . . 80
6.1.4.4 infty . . . 81
6.1.4.5 maxn . . . 81
6.1.4.6 pi . . . 81
6.2 qpp::exception Namespace Reference . . . 81
6.2.1 Detailed Description . . . 82
6.3 qpp::experimental Namespace Reference . . . 83
6.3.1 Detailed Description . . . 83
6.4 qpp::internal Namespace Reference . . . 83
6.4.1 Detailed Description . . . 84
6.4.2 Function Documentation . . . 84
6.4.2.1 check_cvector() . . . 84
6.4.2.2 check_dims() . . . 84
6.4.2.3 check_dims_match_cvect() . . . 85
6.4.2.4 check_dims_match_mat() . . . 85
6.4.2.5 check_dims_match_rvect() . . . 85
6.4.2.6 check_eq_dims() . . . 85
6.4.2.7 check_matching_sizes() . . . 85
6.4.2.8 check_nonzero_size() . . . 85
6.4.2.9 check_perm() . . . 86
6.4.2.10 check_qubit_cvector() . . . 86
6.4.2.11 check_qubit_matrix() . . . 86
6.4.2.12 check_qubit_rvector() . . . 86
6.4.2.13 check_qubit_vector() . . . 86
6.4.2.14 check_rvector() . . . 86
6.4.2.15 check_square_mat() . . . 87
6.4.2.16 check_subsys_match_dims() . . . 87
6.4.2.17 check_vector() . . . 87
6.4.2.18 dirsum2() . . . 87
6.4.2.19 get_dim_subsys() . . . 87
6.4.2.20 get_num_subsys() . . . 87
6.4.2.21 kron2() . . . 88
6.4.2.22 multiidx2n() . . . 88
6.4.2.23 n2multiidx() . . . 88
6.4.2.24 variadic_vector_emplace() [1/2] . . . 88
6.4.2.25 variadic_vector_emplace() [2/2] . . . 88

7 Class Documentation 89

7.1 qpp::experimental::Bit_circuit Class Reference . . . 89

7.1.1 Member Function Documentation . . . 90

7.1.1.1 CNOT() . . . 91

7.1.1.2 FRED() . . . 91

7.1.1.3 NOT() . . . 91

7.1.1.4 reset() . . . 91

7.1.1.5 SWAP() . . . 91

7.1.1.6 TOF() . . . 91

7.1.1.7 X() . . . 91

7.1.2 Member Data Documentation . . . 92

7.1.2.1 gate_count . . . 92

7.2 qpp::Bit_circuit Class Reference . . . 92

7.2.1 Detailed Description . . . 92

7.3 qpp::Codes Class Reference . . . 92

7.3.1 Detailed Description . . . 93

7.3.2 Member Enumeration Documentation . . . 93

7.3.2.1 Type . . . 94

7.3.3 Constructor & Destructor Documentation . . . 94

7.3.3.1 Codes() . . . 94

7.3.3.2 ∼Codes() . . . 94

7.3.4 Member Function Documentation . . . 94

7.3.4.1 codeword() . . . 94

7.3.5 Friends And Related Function Documentation . . . 95

7.3.5.1 internal::Singleton< const Codes > . . . 95

7.4 qpp::exception::CustomException Class Reference . . . 95

7.4.1 Detailed Description . . . 96

7.4.2 Constructor & Destructor Documentation . . . 96

7.4.2.1 CustomException() . . . 97

7.4.3 Member Function Documentation . . . 97

7.4.3.1 type_description() . . . 97
7.4.4 Member Data Documentation . . . 97
7.4.4.1 what_ . . . 97
7.5 qpp::exception::DimsInvalid Class Reference . . . 98
7.5.1 Detailed Description . . . 99
7.5.2 Member Function Documentation . . . 99
7.5.2.1 type_description() . . . 99
7.6 qpp::exception::DimsMismatchCvector Class Reference . . . 99
7.6.1 Detailed Description . . . 101
7.6.2 Member Function Documentation . . . 101
7.6.2.1 type_description() . . . 101
7.7 qpp::exception::DimsMismatchMatrix Class Reference . . . 101
7.7.1 Detailed Description . . . 102
7.7.2 Member Function Documentation . . . 102
7.7.2.1 type_description() . . . 103
7.8 qpp::exception::DimsMismatchRvector Class Reference . . . 103
7.8.1 Detailed Description . . . 104
7.8.2 Member Function Documentation . . . 104
7.8.2.1 type_description() . . . 105
7.9 qpp::exception::DimsMismatchVector Class Reference . . . 105
7.9.1 Detailed Description . . . 106
7.9.2 Member Function Documentation . . . 106
7.9.2.1 type_description() . . . 107
7.10 qpp::exception::DimsNotEqual Class Reference . . . 107
7.10.1 Detailed Description . . . 108
7.10.2 Member Function Documentation . . . 108
7.10.2.1 type_description() . . . 108
7.11 qpp::internal::Display_Impl_ Struct Reference . . . 109
7.11.1 Member Function Documentation . . . 109
7.11.1.1 display_impl_() . . . 109

7.12 qpp::experimental::Dynamic_bitset Class Reference . . . 110
7.12.1 Member Typedef Documentation . . . 112
7.12.1.1 storage_type . . . 112
7.12.1.2 value_type . . . 112
7.12.2 Constructor & Destructor Documentation . . . 112
7.12.2.1 Dynamic_bitset() . . . 112
7.12.3 Member Function Documentation . . . 112
7.12.3.1 all() . . . 112
7.12.3.2 any() . . . 113
7.12.3.3 count() . . . 113
7.12.3.4 data() . . . 113
7.12.3.5 flip() [1/2] . . . 113
7.12.3.6 flip() [2/2] . . . 114
7.12.3.7 get() . . . 114
7.12.3.8 index_() . . . 114
7.12.3.9 none() . . . 114
7.12.3.10 offset_() . . . 115
7.12.3.11 operator"!=() . . . 115
7.12.3.12 operator==() . . . 115
7.12.3.13 rand() [1/2] . . . 116
7.12.3.14 rand() [2/2] . . . 116
7.12.3.15 reset() [1/2] . . . 116
7.12.3.16 reset() [2/2] . . . 117
7.12.3.17 set() [1/2] . . . 117
7.12.3.18 set() [2/2] . . . 117
7.12.3.19 size() . . . 117
7.12.3.20 storage_size() . . . 118
7.12.3.21 to_string() . . . 118
7.12.4 Friends And Related Function Documentation . . . 118
7.12.4.1 operator<< . . . 118

7.12.5 Member Data Documentation . . . 119
7.12.5.1 N_ . . . 119
7.12.5.2 storage_size_ . . . 119
7.12.5.3 v_ . . . 119
7.13 qpp::Dynamic_bitset Class Reference . . . 119
7.13.1 Detailed Description . . . 119
7.14 qpp::exception::Exception Class Reference . . . 120
7.14.1 Detailed Description . . . 121
7.14.2 Constructor & Destructor Documentation . . . 122
7.14.2.1 Exception() . . . 122
7.14.3 Member Function Documentation . . . 122
7.14.3.1 type_description() . . . 122
7.14.3.2 what() . . . 122
7.14.4 Member Data Documentation . . . 123
7.14.4.1 where_ . . . 123
7.15 qpp::experimental::Bit_circuit::Gate_count Struct Reference . . . 123
7.15.1 Member Data Documentation . . . 123
7.15.1.1 CNOT . . . 123
7.15.1.2 FRED . . . 123
7.15.1.3 NOT . . . 124
7.15.1.4 SWAP . . . 124
7.15.1.5 TOF . . . 124
7.15.1.6 X . . . 124
7.16 qpp::Gates Class Reference . . . 124
7.16.1 Detailed Description . . . 126
7.16.2 Constructor & Destructor Documentation . . . 126
7.16.2.1 Gates() . . . 127
7.16.2.2 ∼Gates() . . . 127
7.16.3 Member Function Documentation . . . 127
7.16.3.1 CTRL() . . . 127

7.16.3.2 expandout() [1/3] . . . 128
7.16.3.3 expandout() [2/3] . . . 128
7.16.3.4 expandout() [3/3] . . . 129
7.16.3.5 Fd() . . . 129
7.16.3.6 Id() . . . 130
7.16.3.7 Rn() . . . 130
7.16.3.8 Xd() . . . 131
7.16.3.9 Zd() . . . 131
7.16.4 Friends And Related Function Documentation . . . 131
7.16.4.1 internal::Singleton< const Gates > . . . 132
7.16.5 Member Data Documentation . . . 132
7.16.5.1 CNOT . . . 132
7.16.5.2 CNOTba . . . 132
7.16.5.3 CZ . . . 132
7.16.5.4 FRED . . . 132
7.16.5.5 H . . . 132
7.16.5.6 Id2 . . . 133
7.16.5.7 S . . . 133
7.16.5.8 SWAP . . . 133
7.16.5.9 T . . . 133
7.16.5.10 TOF . . . 133
7.16.5.11 X . . . 133
7.16.5.12 Y . . . 134
7.16.5.13 Z . . . 134
7.17 qpp::IDisplay Class Reference . . . 134
7.17.1 Detailed Description . . . 135
7.17.2 Constructor & Destructor Documentation . . . 135
7.17.2.1 IDisplay() [1/3] . . . 135
7.17.2.2 IDisplay() [2/3] . . . 136
7.17.2.3 IDisplay() [3/3] . . . 136

7.17.2.4 ~IDisplay() . . . 136
7.17.3 Member Function Documentation . . . 136
7.17.3.1 display() . . . 136
7.17.3.2 operator=() [1/2] . . . 136
7.17.3.3 operator=() [2/2] . . . 137
7.17.4 Friends And Related Function Documentation . . . 137
7.17.4.1 operator<< . . . 137
7.18 qpp::Init Class Reference . . . 137
7.18.1 Detailed Description . . . 138
7.18.2 Constructor & Destructor Documentation . . . 138
7.18.2.1 Init() . . . 138
7.18.2.2 ~Init() . . . 139
7.18.3 Friends And Related Function Documentation . . . 139
7.18.3.1 internal::Singleton< const Init > . . . 139
7.19 qpp::internal::IOManipEigen Class Reference . . . 139
7.19.1 Constructor & Destructor Documentation . . . 140
7.19.1.1 IOManipEigen() [1/2] . . . 140
7.19.1.2 IOManipEigen() [2/2] . . . 140
7.19.2 Member Function Documentation . . . 140
7.19.2.1 display() . . . 140
7.19.3 Member Data Documentation . . . 141
7.19.3.1 A_ . . . 141
7.19.3.2 chop_ . . . 141
7.20 qpp::internal::IOManipPointer< PointerType > Class Template Reference . . . 141
7.20.1 Constructor & Destructor Documentation . . . 142
7.20.1.1 IOManipPointer() [1/2] . . . 143
7.20.1.2 IOManipPointer() [2/2] . . . 143
7.20.2 Member Function Documentation . . . 143
7.20.2.1 display() . . . 143
7.20.2.2 operator=() . . . 143

7.20.3 Member Data Documentation . . . 143
7.20.3.1 end_ . . . 144
7.20.3.2 N_ . . . 144
7.20.3.3 p_ . . . 144
7.20.3.4 separator_ . . . 144
7.20.3.5 start_ . . . 144
7.21 qpp::internal::IOManipRange< InputIterator > Class Template Reference . . . 145
7.21.1 Constructor & Destructor Documentation . . . 146
7.21.1.1 IOManipRange() [1/2] . . . 146
7.21.1.2 IOManipRange() [2/2] . . . 146
7.21.2 Member Function Documentation . . . 146
7.21.2.1 display() . . . 146
7.21.2.2 operator=() . . . 147
7.21.3 Member Data Documentation . . . 147
7.21.3.1 end_ . . . 147
7.21.3.2 first_ . . . 147
7.21.3.3 last_ . . . 147
7.21.3.4 separator_ . . . 147
7.21.3.5 start_ . . . 147
7.22 qpp::is_complex< T > Struct Template Reference . . . 148
7.22.1 Detailed Description . . . 148
7.23 qpp::is_complex< std::complex< T > > Struct Template Reference . . . 149
7.23.1 Detailed Description . . . 149
7.24 qpp::is_iterable< T, typename > Struct Template Reference . . . 150
7.24.1 Detailed Description . . . 150
7.25 qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > > Struct Template Reference . . . 151
7.25.1 Detailed Description . . . 152
7.26 qpp::is_matrix_expression< Derived > Struct Template Reference . . . 152
7.26.1 Detailed Description . . . 153
7.27 qpp::make_void< Ts > Struct Template Reference . . . 153

7.27.1 Detailed Description . . . 153
7.27.2 Member Typedef Documentation . . . 153
7.27.2.1 type . . . 153
7.28 qpp::exception::MatrixMismatchSubsys Class Reference . . . 154
7.28.1 Detailed Description . . . 155
7.28.2 Member Function Documentation . . . 155
7.28.2.1 type_description() . . . 155
7.29 qpp::exception::MatrixNotCvector Class Reference . . . 155
7.29.1 Detailed Description . . . 157
7.29.2 Member Function Documentation . . . 157
7.29.2.1 type_description() . . . 157
7.30 qpp::exception::MatrixNotRvector Class Reference . . . 157
7.30.1 Detailed Description . . . 158
7.30.2 Member Function Documentation . . . 158
7.30.2.1 type_description() . . . 158
7.31 qpp::exception::MatrixNotSquare Class Reference . . . 159
7.31.1 Detailed Description . . . 160
7.31.2 Member Function Documentation . . . 160
7.31.2.1 type_description() . . . 160
7.32 qpp::exception::MatrixNotSquareNorCvector Class Reference . . . 161
7.32.1 Detailed Description . . . 162
7.32.2 Member Function Documentation . . . 162
7.32.2.1 type_description() . . . 162
7.33 qpp::exception::MatrixNotSquareNorRvector Class Reference . . . 163
7.33.1 Detailed Description . . . 164
7.33.2 Member Function Documentation . . . 164
7.33.2.1 type_description() . . . 164
7.34 qpp::exception::MatrixNotSquareNorVector Class Reference . . . 165
7.34.1 Detailed Description . . . 166
7.34.2 Member Function Documentation . . . 166

7.34.2.1 type_description() . . . 166
7.35 qpp::exception::MatrixNotVector Class Reference . . . 167
7.35.1 Detailed Description . . . 168
7.35.2 Member Function Documentation . . . 168
7.35.2.1 type_description() . . . 168
7.36 qpp::exception::NoCodeword Class Reference . . . 169
7.36.1 Detailed Description . . . 170
7.36.2 Member Function Documentation . . . 170
7.36.2.1 type_description() . . . 170
7.37 qpp::exception::NotBipartite Class Reference . . . 171
7.37.1 Detailed Description . . . 172
7.37.2 Member Function Documentation . . . 172
7.37.2.1 type_description() . . . 172
7.38 qpp::exception::NotQubitCvector Class Reference . . . 172
7.38.1 Detailed Description . . . 174
7.38.2 Member Function Documentation . . . 174
7.38.2.1 type_description() . . . 174
7.39 qpp::exception::NotQubitMatrix Class Reference . . . 174
7.39.1 Detailed Description . . . 175
7.39.2 Member Function Documentation . . . 175
7.39.2.1 type_description() . . . 175
7.40 qpp::exception::NotQubitRvector Class Reference . . . 176
7.40.1 Detailed Description . . . 177
7.40.2 Member Function Documentation . . . 177
7.40.2.1 type_description() . . . 177
7.41 qpp::exception::NotQubitSubsys Class Reference . . . 178
7.41.1 Detailed Description . . . 179
7.41.2 Member Function Documentation . . . 179
7.41.2.1 type_description() . . . 179
7.42 qpp::exception::NotQubitVector Class Reference . . . 180

7.42.1 Detailed Description . . . 181
7.42.2 Member Function Documentation . . . 181
7.42.2.1 type_description() . . . 181
7.43 qpp::exception::OutOfRange Class Reference . . . 182
7.43.1 Detailed Description . . . 183
7.43.2 Member Function Documentation . . . 183
7.43.2.1 type_description() . . . 183
7.44 qpp::exception::PermInvalid Class Reference . . . 184
7.44.1 Detailed Description . . . 185
7.44.2 Member Function Documentation . . . 185
7.44.2.1 type_description() . . . 185
7.45 qpp::exception::PermMismatchDims Class Reference . . . 185
7.45.1 Detailed Description . . . 187
7.45.2 Member Function Documentation . . . 187
7.45.2.1 type_description() . . . 187
7.46 qpp::RandomDevices Class Reference . . . 187
7.46.1 Detailed Description . . . 189
7.46.2 Constructor & Destructor Documentation . . . 189
7.46.2.1 RandomDevices() . . . 189
7.46.2.2 ∼RandomDevices() . . . 189
7.46.3 Member Function Documentation . . . 189
7.46.3.1 get_prng() . . . 189
7.46.3.2 load() . . . 189
7.46.3.3 save() . . . 190
7.46.4 Friends And Related Function Documentation . . . 190
7.46.4.1 internal::Singleton< RandomDevices > . . . 190
7.46.5 Member Data Documentation . . . 190
7.46.5.1 prng_ . . . 190
7.46.5.2 rd_ . . . 191
7.47 qpp::internal::Singleton< T > Class Template Reference . . . 191

7.47.1 Detailed Description . . . 191
7.47.2 Constructor & Destructor Documentation . . . 192
7.47.2.1 Singleton() [1/2] . . . 192
7.47.2.2 Singleton() [2/2] . . . 192
7.47.2.3 ~Singleton() . . . 192
7.47.3 Member Function Documentation . . . 192
7.47.3.1 get_instance() . . . 193
7.47.3.2 get_thread_local_instance() . . . 193
7.47.3.3 operator=() . . . 193
7.48 qpp::exception::SizeMismatch Class Reference . . . 193
7.48.1 Detailed Description . . . 194
7.48.2 Member Function Documentation . . . 194
7.48.2.1 type_description() . . . 194
7.49 qpp::States Class Reference . . . 195
7.49.1 Detailed Description . . . 197
7.49.2 Constructor & Destructor Documentation . . . 197
7.49.2.1 States() . . . 197
7.49.2.2 ~States() . . . 197
7.49.3 Member Function Documentation . . . 197
7.49.3.1 jn() . . . 197
7.49.3.2 mes() . . . 198
7.49.3.3 minus() . . . 198
7.49.3.4 one() . . . 199
7.49.3.5 plus() . . . 199
7.49.3.6 zero() . . . 199
7.49.4 Friends And Related Function Documentation . . . 200
7.49.4.1 internal::Singleton< const States > . . . 200
7.49.5 Member Data Documentation . . . 200
7.49.5.1 b00 . . . 200
7.49.5.2 b01 . . . 200

7.49.5.3 b10 . . . 200
7.49.5.4 b11 . . . 200
7.49.5.5 GHZ . . . 201
7.49.5.6 pb00 . . . 201
7.49.5.7 pb01 . . . 201
7.49.5.8 pb10 . . . 201
7.49.5.9 pb11 . . . 201
7.49.5.10 pGHZ . . . 201
7.49.5.11 pW . . . 202
7.49.5.12 px0 . . . 202
7.49.5.13 px1 . . . 202
7.49.5.14 py0 . . . 202
7.49.5.15 py1 . . . 202
7.49.5.16 pz0 . . . 202
7.49.5.17 pz1 . . . 203
7.49.5.18 W . . . 203
7.49.5.19 x0 . . . 203
7.49.5.20 x1 . . . 203
7.49.5.21 y0 . . . 203
7.49.5.22 y1 . . . 203
7.49.5.23 z0 . . . 204
7.49.5.24 z1 . . . 204
7.50 qpp::exception::SubsysMismatchDims Class Reference . . . 204
7.50.1 Detailed Description . . . 205
7.50.2 Member Function Documentation . . . 205
7.50.2.1 type_description() . . . 205
7.51 qpp::Timer< T, CLOCK_T > Class Template Reference . . . 206
7.51.1 Detailed Description . . . 207
7.51.2 Constructor & Destructor Documentation . . . 208
7.51.2.1 Timer() [1/3] . . . 208

7.51.2.2 Timer() [2/3] . . . 208
7.51.2.3 Timer() [3/3] . . . 208
7.51.2.4 ∼Timer() . . . 208
7.51.3 Member Function Documentation . . . 208
7.51.3.1 display() . . . 208
7.51.3.2 get_duration() . . . 209
7.51.3.3 operator=() [1/2] . . . 209
7.51.3.4 operator=() [2/2] . . . 209
7.51.3.5 tic() . . . 210
7.51.3.6 tics() . . . 210
7.51.3.7 toc() . . . 210
7.51.4 Member Data Documentation . . . 210
7.51.4.1 end_ . . . 210
7.51.4.2 start_ . . . 211
7.52 qpp::exception::TypeMismatch Class Reference . . . 211
7.52.1 Detailed Description . . . 212
7.52.2 Member Function Documentation . . . 212
7.52.2.1 type_description() . . . 212
7.53 qpp::exception::UndefinedType Class Reference . . . 213
7.53.1 Detailed Description . . . 214
7.53.2 Member Function Documentation . . . 214
7.53.2.1 type_description() . . . 214
7.54 qpp::exception::Unknown Class Reference . . . 214
7.54.1 Detailed Description . . . 216
7.54.2 Member Function Documentation . . . 216
7.54.2.1 type_description() . . . 216
7.55 qpp::exception::ZeroSize Class Reference . . . 216
7.55.1 Detailed Description . . . 217
7.55.2 Member Function Documentation . . . 217
7.55.2.1 type_description() . . . 217

8 File Documentation **219**

8.1 classes/codes.h File Reference . . . 219

8.1.1 Detailed Description . . . 219

8.2 classes/exception.h File Reference . . . 219

8.2.1 Detailed Description . . . 221

8.3 classes/gates.h File Reference . . . 221

8.3.1 Detailed Description . . . 221

8.4 classes/idisplay.h File Reference . . . 222

8.4.1 Detailed Description . . . 222

8.5 classes/init.h File Reference . . . 222

8.5.1 Detailed Description . . . 223

8.6 classes/random_devices.h File Reference . . . 223

8.6.1 Detailed Description . . . 223

8.7 classes/states.h File Reference . . . 223

8.7.1 Detailed Description . . . 224

8.8 classes/timer.h File Reference . . . 224

8.8.1 Detailed Description . . . 224

8.9 constants.h File Reference . . . 224

8.9.1 Detailed Description . . . 225

8.10 entanglement.h File Reference . . . 225

8.10.1 Detailed Description . . . 227

8.11 entropies.h File Reference . . . 227

8.11.1 Detailed Description . . . 227

8.12 experimental/experimental.h File Reference . . . 228

8.12.1 Detailed Description . . . 228

8.12.2 Typedef Documentation . . . 228

8.12.2.1 idx . . . 228

8.13 functions.h File Reference . . . 229

8.13.1 Detailed Description . . . 229

8.14 input_output.h File Reference . . . 229

8.14.1 Detailed Description . . . 230
8.15 instruments.h File Reference . . . 230
8.15.1 Detailed Description . . . 232
8.16 internal/classes/iomanip.h File Reference . . . 232
8.16.1 Detailed Description . . . 232
8.17 internal/classes/singleton.h File Reference . . . 233
8.17.1 Detailed Description . . . 233
8.18 internal/util.h File Reference . . . 233
8.18.1 Detailed Description . . . 235
8.19 MATLAB/matlab.h File Reference . . . 235
8.19.1 Detailed Description . . . 236
8.20 number_theory.h File Reference . . . 236
8.20.1 Detailed Description . . . 237
8.21 operations.h File Reference . . . 237
8.21.1 Detailed Description . . . 239
8.22 qpp.h File Reference . . . 239
8.22.1 Detailed Description . . . 240
8.22.2 Macro Definition Documentation . . . 240
8.22.2.1 QPP_UNUSED_ . . . 240
8.23 random.h File Reference . . . 240
8.23.1 Detailed Description . . . 241
8.24 statistics.h File Reference . . . 242
8.24.1 Detailed Description . . . 242
8.25 traits.h File Reference . . . 243
8.25.1 Detailed Description . . . 243
8.26 types.h File Reference . . . 244
8.26.1 Detailed Description . . . 245
8.27 /Users/vlad/Dropbox/programming/cpp/qpp/README.md File Reference . . . 245

Index **247**

Chapter 1

Quantum++

Version 1.0-rc2 - 6 September 2017

Build status:

Chat (questions/issues)

About

Quantum++ is a modern C++11 general purpose quantum computing library, composed solely of template header files. Quantum++ is written in standard C++11 and has very low external dependencies, using only the `Eigen 3` linear algebra header-only template library and, if available, the `OpenMP` multi-processing library.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance. The library's simulation capabilities are only restricted by the amount of available physical memory. On a typical machine (Intel i5 8Gb RAM) Quantum++ can successfully simulate the evolution of 25 qubits in a pure state or of 12 qubits in a mixed state reasonably fast.

To report any bugs or ask for additional features/enhancements, please `submit an issue` with an appropriate label.

If you are interesting in contributing to this project, feel free to contact me. Alternatively, create a custom branch, add your contribution, then finally create a pull request. If I accept the pull request, I will merge your custom branch with the latest development branch. The latter will eventually be merged into a future release version. To contribute, you need to have a solid knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and working experience with `Eigen 3`.

For additional `Eigen 3` documentation see `http://eigen.tuxfamily.org/dox/`. For a simple `Eigen 3` quick ASCII reference see `http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt`.

License

`Quantum++` is distributed under the MIT license. Please see the `LICENSE` file for more details.

Installation instructions and further documentation

Please see the installation guide https://github.com/vsoftco/qpp/blob/master/INSTALL.md "‘INSTALL.md‘" and the comprehensive `Wiki` for further documentation and detailed examples.

The official API documentation is available in PDF and HTML formats in the `doc` folder.

Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp
Quantum++ main namespace 13
qpp::exception
Quantum++ exception hierarchy namespace 81
qpp::experimental
Experimental/test functions/classes, do not use or modify 83
qpp::internal
Internal utility functions, do not use them directly or modify them 83

Chapter 3

Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::Bit_circuit . . . 92
qpp::internal::Display_Impl_ . . . 109
  qpp::internal::IOManipEigen . . . 139
qpp::experimental::Dynamic_bitset . . . 110
  qpp::experimental::Bit_circuit . . . 89
qpp::Dynamic_bitset . . . 119
std::exception
  qpp::exception::Exception . . . 120
    qpp::exception::CustomException . . . 95
    qpp::exception::DimsInvalid . . . 98
    qpp::exception::DimsMismatchCvector . . . 99
    qpp::exception::DimsMismatchMatrix . . . 101
    qpp::exception::DimsMismatchRvector . . . 103
    qpp::exception::DimsMismatchVector . . . 105
    qpp::exception::DimsNotEqual . . . 107
    qpp::exception::MatrixMismatchSubsys . . . 154
    qpp::exception::MatrixNotCvector . . . 155
    qpp::exception::MatrixNotRvector . . . 157
    qpp::exception::MatrixNotSquare . . . 159
    qpp::exception::MatrixNotSquareNorCvector . . . 161
    qpp::exception::MatrixNotSquareNorRvector . . . 163
    qpp::exception::MatrixNotSquareNorVector . . . 165
    qpp::exception::MatrixNotVector . . . 167
    qpp::exception::NoCodeword . . . 169
    qpp::exception::NotBipartite . . . 171
    qpp::exception::NotQubitCvector . . . 172
    qpp::exception::NotQubitMatrix . . . 174
    qpp::exception::NotQubitRvector . . . 176
    qpp::exception::NotQubitSubsys . . . 178
    qpp::exception::NotQubitVector . . . 180
    qpp::exception::OutOfRange . . . 182
    qpp::exception::PermInvalid . . . 184
    qpp::exception::PermMismatchDims . . . 185
    qpp::exception::SizeMismatch . . . 193
    qpp::exception::SubsysMismatchDims . . . 204

qpp::exception::TypeMismatch . . . 211
qpp::exception::UndefinedType . . . 213
qpp::exception::Unknown . . . 214
qpp::exception::ZeroSize . . . 216
false_type
qpp::is_complex< T > . . . 148
qpp::is_iterable< T, typename > . . . 150
qpp::experimental::Bit_circuit::Gate_count . . . 123
qpp::IDisplay . . . 134
qpp::internal::IOManipEigen . . . 139
qpp::internal::IOManipPointer< PointerType > . . . 141
qpp::internal::IOManipRange< InputIterator > . . . 145
qpp::Timer< T, CLOCK_T > . . . 206
is_base_of
qpp::is_matrix_expression< Derived > . . . 152
qpp::make_void< Ts > . . . 153
qpp::internal::Singleton< T > . . . 191
qpp::internal::Singleton< const Codes > . . . 191
qpp::Codes . . . 92
qpp::internal::Singleton< const Gates > . . . 191
qpp::Gates . . . 124
qpp::internal::Singleton< const Init > . . . 191
qpp::Init . . . 137
qpp::internal::Singleton< const States > . . . 191
qpp::States . . . 195
qpp::internal::Singleton< RandomDevices > . . . 191
qpp::RandomDevices . . . 187
true_type
qpp::is_complex< std::complex< T > > . . . 149
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > > . . . 151

Chapter 4

Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

qpp::experimental::Bit_circuit . . . 89
qpp::Bit_circuit
Classical reversible circuit simulator . . . 92
qpp::Codes
Const Singleton class that defines quantum error correcting codes . . . 92
qpp::exception::CustomException
Custom exception . . . 95
qpp::exception::DimsInvalid
Invalid dimension(s) exception . . . 98
qpp::exception::DimsMismatchCvector
Dimension(s) mismatch column vector size exception . . . 99
qpp::exception::DimsMismatchMatrix
Dimension(s) mismatch matrix size exception . . . 101
qpp::exception::DimsMismatchRvector
Dimension(s) mismatch row vector size exception . . . 103
qpp::exception::DimsMismatchVector
Dimension(s) mismatch vector size exception . . . 105
qpp::exception::DimsNotEqual
Dimensions not equal exception . . . 107
qpp::internal::Display_Impl_ . . . 109
qpp::experimental::Dynamic_bitset . . . 110
qpp::Dynamic_bitset
Dynamic bitset class, allows the specification of the number of bits at runtime (unlike std::bitset<N>) . . . 119
qpp::exception::Exception
Base class for generating Quantum++ custom exceptions . . . 120
qpp::experimental::Bit_circuit::Gate_count . . . 123
qpp::Gates
Const Singleton class that implements most commonly used gates . . . 124
qpp::IDisplay
Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const . . . 134
qpp::Init
Const Singleton class that performs additional initializations/cleanups . . . 137
qpp::internal::IOManipEigen . . . 139

qpp::internal::IOManipPointer< PointerType > . . . 141
qpp::internal::IOManipRange< InputIterator > . . . 145
qpp::is_complex< T >
Checks whether the type is a complex type . . . 148
qpp::is_complex< std::complex< T > >
Checks whether the type is a complex number type, specialization for complex types . . . 149
qpp::is_iterable< T, typename >
Checks whether *T* is compatible with an STL-like iterable container . . . 150
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >
Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers . . . 151
qpp::is_matrix_expression< Derived >
Checks whether the type is an Eigen matrix expression . . . 152
qpp::make_void< Ts >
Helper for qpp::to_void<> alias template . . . 153
qpp::exception::MatrixMismatchSubsys
Matrix mismatch subsystems exception . . . 154
qpp::exception::MatrixNotCvector
Matrix is not a column vector exception . . . 155
qpp::exception::MatrixNotRvector
Matrix is not a row vector exception . . . 157
qpp::exception::MatrixNotSquare
Matrix is not square exception . . . 159
qpp::exception::MatrixNotSquareNorCvector
Matrix is not square nor column vector exception . . . 161
qpp::exception::MatrixNotSquareNorRvector
Matrix is not square nor row vector exception . . . 163
qpp::exception::MatrixNotSquareNorVector
Matrix is not square nor vector exception . . . 165
qpp::exception::MatrixNotVector
Matrix is not a vector exception . . . 167
qpp::exception::NoCodeword
Codeword does not exist exception . . . 169
qpp::exception::NotBipartite
Not bi-partite exception . . . 171
qpp::exception::NotQubitCvector
Column vector is not 2 x 1 exception . . . 172
qpp::exception::NotQubitMatrix
Matrix is not 2 x 2 exception . . . 174
qpp::exception::NotQubitRvector
Row vector is not 1 x 2 exception . . . 176
qpp::exception::NotQubitSubsys
Subsystems are not qubits exception . . . 178
qpp::exception::NotQubitVector
Vector is not 2 x 1 nor 1 x 2 exception . . . 180
qpp::exception::OutOfRange
Parameter out of range exception . . . 182
qpp::exception::PermInvalid
Invalid permutation exception . . . 184
qpp::exception::PermMismatchDims
Permutation mismatch dimensions exception . . . 185
qpp::RandomDevices
Singleton class that manages the source of randomness in the library . . . 187
qpp::internal::Singleton< T >
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern) . . . 191

qpp::exception::SizeMismatch
Size mismatch exception . . . 193
qpp::States
Const Singleton class that implements most commonly used states . . . 195
qpp::exception::SubsysMismatchDims
Subsystems mismatch dimensions exception . . . 204
qpp::Timer< T, CLOCK_T >
Chronometer . . . 206
qpp::exception::TypeMismatch
Type mismatch exception . . . 211
qpp::exception::UndefinedType
Not defined for this type exception . . . 213
qpp::exception::Unknown
Unknown exception . . . 214
qpp::exception::ZeroSize
Object has zero size exception . . . 216

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

constants.h
: Constants . . . 224

entanglement.h
: Entanglement functions . . . 225

entropies.h
: Entropy functions . . . 227

functions.h
: Generic quantum computing functions . . . 229

input_output.h
: Input/output functions . . . 229

instruments.h
: Measurement functions . . . 230

number_theory.h
: Number theory functions . . . 236

operations.h
: Quantum operation functions . . . 237

qpp.h
: Quantum++ main header file, includes all other necessary headers . . . 239

random.h
: Randomness-related functions . . . 240

statistics.h
: Statistics functions . . . 242

traits.h
: Type traits . . . 243

types.h
: Type aliases . . . 244

classes/codes.h
: Quantum error correcting codes . . . 219

classes/exception.h
: Exceptions . . . 219

classes/gates.h
: Quantum gates . . . 221

classes/idisplay.h
: Display interface via the non-virtual interface (NVI) . . . 222

classes/init.h
: Initialization . . . 222

classes/random_devices.h
Random devices 223
classes/states.h
Quantum states 223
classes/timer.h
Timing 224
experimental/experimental.h
Experimental/test functions/classes 228
internal/util.h
Internal utility functions 233
internal/classes/iomanip.h
Input/output manipulators 232
internal/classes/singleton.h
Singleton pattern via CRTP 233
MATLAB/matlab.h
Input/output interfacing with MATLAB 235

Chapter 6

Namespace Documentation

6.1 qpp Namespace Reference

Quantum++ main namespace.

Namespaces

- exception

  Quantum++ exception hierarchy namespace.
- experimental

  Experimental/test functions/classes, do not use or modify.
- internal

  Internal utility functions, do not use them directly or modify them.

Classes

- class Bit_circuit

  Classical reversible circuit simulator.
- class Codes

  const Singleton class that defines quantum error correcting codes
- class Dynamic_bitset

  Dynamic bitset class, allows the specification of the number of bits at runtime (unlike std::bitset<N>)
- class Gates

  const Singleton class that implements most commonly used gates
- class IDisplay

  Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.
- class Init

  const Singleton class that performs additional initializations/cleanups
- struct is_complex

  Checks whether the type is a complex type.
- struct is_complex< std::complex< T > >

  Checks whether the type is a complex number type, specialization for complex types.
- struct is_iterable

  Checks whether T is compatible with an STL-like iterable container.

- struct is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >

  Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

- struct is_matrix_expression

  Checks whether the type is an Eigen matrix expression.

- struct make_void

  Helper for qpp::to_void<> alias template.

- class RandomDevices

  Singleton class that manages the source of randomness in the library.

- class States

  const Singleton class that implements most commonly used states

- class Timer

  Chronometer.

Typedefs

- template<typename... Ts>
  using to_void = typename make_void< Ts... >::type

  Alias template that implements the proposal for void_t.

- using idx = std::size_t

  Non-negative integer index.

- using bigint = long long int

  Big integer.

- using cplx = std::complex< double >

  Complex number in double precision.

- using ket = Eigen::VectorXcd

  Complex (double precision) dynamic Eigen column vector.

- using bra = Eigen::RowVectorXcd

  Complex (double precision) dynamic Eigen row vector.

- using cmat = Eigen::MatrixXcd

  Complex (double precision) dynamic Eigen matrix.

- using dmat = Eigen::MatrixXd

  Real (double precision) dynamic Eigen matrix.

- template<typename Scalar >
  using dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

  Dynamic Eigen matrix over the field specified by Scalar.

- template<typename Scalar >
  using dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >

  Dynamic Eigen column vector over the field specified by Scalar.

- template<typename Scalar >
  using dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >

  Dynamic Eigen row vector over the field specified by Scalar.

Functions

- constexpr cplx operator"" _i (unsigned long long int x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr cplx operator"" _i (long double x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- cplx omega (idx D)

  D-th root of unity.
- template<typename Derived >
  dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt coefficients of the bi-partite pure state A.
- template<typename Derived >
  dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt coefficients of the bi-partite pure state A.
- template<typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Alice side.
- template<typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Alice side.
- template<typename Derived >
  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Bob side.
- template<typename Derived >
  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Bob side.
- template<typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double gconcurrence (const Eigen::MatrixBase< Derived > &A)

  G-concurrence of the bi-partite pure state A.
- template<typename Derived >
  double negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Logarithmic negativity of the bi-partite mixed state A.

- template<typename Derived >
  double lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double concurrence (const Eigen::MatrixBase< Derived > &A)

  Wootters concurrence of the bi-partite qubit mixed state A.
- template<typename Derived >
  double entropy (const Eigen::MatrixBase< Derived > &A)

  von-Neumann entropy of the density matrix A
- double entropy (const std::vector< double > &prob)

  Shannon entropy of the probability distribution prob.
- template<typename Derived >
  double renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

  Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- double renyi (const std::vector< double > &prob, double alpha)

  Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template<typename Derived >
  double tsallis (const Eigen::MatrixBase< Derived > &A, double q)

  Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- double tsallis (const std::vector< double > &prob, double q)

  Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template<typename Derived >
  double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

  Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived >
  double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)

  Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived >
  internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

  Eigen expression ostream manipulator.
- internal::IOManipEigen disp (cplx z, double chop=qpp::chop)

  Complex number ostream manipulator.
- template<typename InputIterator >
  internal::IOManipRange< InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

  Range ostream manipulator.
- template<typename Container >
  internal::IOManipRange< typename Container::const_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="]", typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template<typename PointerType >
  internal::IOManipPointer< PointerType > disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")

  C-style pointer ostream manipulator.
- template<typename Derived >
  void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

  Saves Eigen expression to a binary file (internal format) in double precision.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > load (const std::string &fname)

  Loads Eigen matrix from a binary file (internal format) in double precision.

- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::↩
  MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Generalized inner product.
- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::↩
  MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)

  Generalized inner product.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Measures the state A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)

  Measures the state A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

  Measures the state A in the orthonormal basis specified by the unitary matrix U.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::Scalar > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< !std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.
- std::vector< int > x2contfrac (double x, idx N, idx cut=1e5)

  Simple continued fraction expansion.
- double contfrac2x (const std::vector< int > &cf, idx N=idx(-1))

  Real representation of a simple continued fraction.
- bigint gcd (bigint a, bigint b)

  Greatest common divisor of two integers.
- bigint gcd (const std::vector< bigint > &as)

  Greatest common divisor of a list of integers.
- bigint lcm (bigint a, bigint b)

  Least common multiple of two integers.
- bigint lcm (const std::vector< bigint > &as)

  Least common multiple of a list of integers.
- std::vector< idx > invperm (const std::vector< idx > &perm)

  Inverse permutation.
- std::vector< idx > compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

  Compose permutations.
- std::vector< bigint > factors (bigint a)

  Prime factor decomposition.
- bigint modmul (bigint a, bigint b, bigint p)

  Modular multiplication without overflow.
- bigint modpow (bigint a, bigint n, bigint p)

  Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.
- std::tuple< bigint, bigint, bigint > egcd (bigint a, bigint b)

  Extended greatest common divisor of two integers.
- bigint modinv (bigint a, bigint p)

  Modular inverse of a mod p.
- bool isprime (bigint p, idx k=80)

  Primality test based on the Miller-Rabin's algorithm.
- bigint randprime (bigint a, bigint b, idx N=1000)

  Generates a random big prime uniformly distributed in the interval [a, b].
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Applies the channel specified by the set of Kraus operators Ks to the density matrix A.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- cmat kraus2super (const std::vector< cmat > &Ks)

  Superoperator matrix.
- cmat kraus2choi (const std::vector< cmat > &Ks)

  Choi matrix.
- std::vector< cmat > choi2kraus (const cmat &A)

  Orthogonal Kraus operators from Choi matrix.
- cmat choi2super (const cmat &A)

  Converts Choi matrix to superoperator matrix.
- cmat super2choi (const cmat &A)

  Converts superoperator matrix to Choi matrix.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Partial trace.

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &subsys, const std::vector< idx > &dims)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &subsys, idx d=2)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &perm, const std::vector< idx > &dims)

  Subsystem permutation.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &perm, idx d=2)

  Subsystem permutation.
- double rand (double a, double b)

  Generates a random real number uniformly distributed in the interval [a, b)
- bigint rand (bigint a, bigint b)

  Generates a random big integer uniformly distributed in the interval [a, b].
- idx randidx (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

  Generates a random index (idx) uniformly distributed in the interval [a, b].
- template<typename Derived >
  Derived rand (idx rows, idx cols, double a=0, double b=1)

  Generates a random matrix with entries uniformly distributed in the interval [a, b)
- template<>
  dmat rand (idx rows, idx cols, double a, double b)

  Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
- template<>
  cmat rand (idx rows, idx cols, double a, double b)

  Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
- template<typename Derived >
  Derived randn (idx rows, idx cols, double mean=0, double sigma=1)

  Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>
  dmat randn (idx rows, idx cols, double mean, double sigma)

  Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)
- template<>
  cmat randn (idx rows, idx cols, double mean, double sigma)

  Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)
- double randn (double mean=0, double sigma=1)

  Generates a random real number (double) normally distributed in N(mean, sigma)
- cmat randU (idx D=2)

  Generates a random unitary matrix.
- cmat randV (idx Din, idx Dout)

Generates a random isometry matrix.

- std::vector< cmat > randkraus (idx N, idx D=2)

  Generates a set of random Kraus operators.
- cmat randH (idx D=2)

  Generates a random Hermitian matrix.
- ket randket (idx D=2)

  Generates a random normalized ket (pure state vector)
- cmat randrho (idx D=2)

  Generates a random density matrix.
- std::vector< idx > randperm (idx N)

  Generates a random uniformly distributed permutation.
- std::vector< double > randprob (idx N)

  Generates a random probability vector uniformly distributed over the probability simplex.
- std::vector< double > uniform (idx N)

  Uniform probability distribution vector.
- std::vector< double > marginalX (const dmat &probXY)

  Marginal distribution.
- std::vector< double > marginalY (const dmat &probXY)

  Marginal distribution.
- template<typename Container >
  double avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Average.
- template<typename Container >
  double cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Covariance.
- template<typename Container >
  double var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Variance.
- template<typename Container >
  double sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Standard deviation.
- template<typename Container >
  double cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Correlation.

Variables

- constexpr double chop = 1e-10

  Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.
- constexpr double eps = 1e-12

  Used to decide whether a number or expression in double precision is zero or not.
- constexpr idx maxn = 64

  Maximum number of allowed qubits/qudits (subsystems)
- constexpr double pi = 3.14159265358979323846264338327950288 4

  π
- constexpr double ee = 2.71828182845904523536028747135266249 7

  Base of natural logarithm, e.
- constexpr double infty = std::numeric_limits<double>::max()

  Used to denote infinity in double precision.

6.1.1 Detailed Description

Quantum++ main namespace.

6.1.2 Typedef Documentation

6.1.2.1 bigint

```
using qpp::bigint = typedef long long int
```

Big integer.

6.1.2.2 bra

```
using qpp::bra = typedef Eigen::RowVectorXcd
```

Complex (double precision) dynamic Eigen row vector.

6.1.2.3 cmat

```
using qpp::cmat = typedef Eigen::MatrixXcd
```

Complex (double precision) dynamic Eigen matrix.

6.1.2.4 cplx

```
using qpp::cplx = typedef std::complex<double>
```

Complex number in double precision.

6.1.2.5 dmat

```
using qpp::dmat = typedef Eigen::MatrixXd
```

Real (double precision) dynamic Eigen matrix.

6.1.2.6 dyn_col_vect

```
template<typename Scalar >
using qpp::dyn_col_vect = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, 1>
```

Dynamic Eigen column vector over the field specified by *Scalar*.

Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
dyn_col_vect<float> colvect(2);
```

6.1.2.7 dyn_mat

```
template<typename Scalar >
using qpp::dyn_mat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>
```

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
dyn_mat<float> mat(2, 3);
```

6.1.2.8 dyn_row_vect

```
template<typename Scalar >
using qpp::dyn_row_vect = typedef Eigen::Matrix<Scalar, 1, Eigen::Dynamic>
```

Dynamic Eigen row vector over the field specified by *Scalar*.

Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
dyn_row_vect<float> rowvect(3);
```

6.1.2.9 idx

```
using qpp::idx = typedef std::size_t
```

Non-negative integer index.

6.1.2.10 ket

```
using qpp::ket = typedef Eigen::VectorXcd
```

Complex (double precision) dynamic Eigen column vector.

6.1.2.11 to_void

```
template<typename...  Ts>
using qpp::to_void = typedef typename make_void<Ts...>::type
```

Alias template that implements the proposal for void_t.

See also

http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911

6.1.3 Function Documentation

6.1.3.1 apply() [1/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
             const Eigen::MatrixBase< Derived1 > & state,
             const Eigen::MatrixBase< Derived2 > & A,
             const std::vector< idx > & subsys,
             const std::vector< idx > & dims )
```

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

state	Eigen expression
A	Eigen expression
subsys	Subsystem indexes where the gate *A* is applied
dims	Dimensions of the multi-partite system

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.2 apply() [2/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
             const Eigen::MatrixBase< Derived1 > & state,
             const Eigen::MatrixBase< Derived2 > & A,
             const std::vector< idx > & subsys,
             idx d = 2 )
```

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

state	Eigen expression
A	Eigen expression
subsys	Subsystem indexes where the gate *A* is applied
d	Subsystem dimensions

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.3 apply() [3/5]

```
template<typename Derived >
cmat qpp::apply (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< cmat > & Ks )
```

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Output density matrix after the action of the channel

6.1.3.4 apply() [4/5]

```
template<typename Derived >
cmat qpp::apply (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< cmat > & Ks,
             const std::vector< idx > & subsys,
             const std::vector< idx > & dims )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes where the Kraus operators *Ks* are applied
dims	Dimensions of the multi-partite system

Returns

Output density matrix after the action of the channel

6.1.3.5 apply() [5/5]

```
template<typename Derived >
cmat qpp::apply (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< cmat > & Ks,
             const std::vector< idx > & subsys,
             idx d = 2 )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes where the Kraus operators *Ks* are applied
d	Subsystem dimensions

Returns

Output density matrix after the action of the channel

6.1.3.6 applyCTRL() [1/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

qpp::Gates::CTRL()

Note

The dimension of the gate *A* must match the dimension of *subsys*. Also, all control subsystems in *ctrl* must have the same dimension.

Parameters

state	Eigen expression
A	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate *A* is applied
dims	Dimensions of the multi-partite system

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.7 applyCTRL() [2/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

qpp::Gates::CTRL()

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

state	Eigen expression
A	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate *A* is applied
d	Subsystem dimensions

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.8 avg()

```
template<typename Container >
double qpp::avg (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Average.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Average of *X*

6.1.3.9 choi2kraus()

```
std::vector<cmat> qpp::choi2kraus (
            const cmat & A )  [inline]
```

Orthogonal Kraus operators from Choi matrix.

See also

qpp::kraus2choi()

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix *A*

Note

The Kraus operators satisfy $Tr(K_i^\dagger K_j) = \delta_{ij}$ for all $i \neq j$

Parameters

A	Choi matrix

Returns

Set of orthogonal Kraus operators

6.1.3.10 choi2super()

```
cmat qpp::choi2super (
            const cmat & A )  [inline]
```

Converts Choi matrix to superoperator matrix.

See also

qpp::super2choi()

Parameters

A	Choi matrix

Returns

Superoperator matrix

6.1.3.11 compperm()

```
std::vector<idx> qpp::compperm (
            const std::vector< idx > & perm,
            const std::vector< idx > & sigma )  [inline]
```

Compose permutations.

Parameters

perm	Permutation
sigma	Permutation

Returns

Composition of the permutations *perm* ∘ *sigma* = perm(sigma)

6.1.3.12 concurrence()

```
template<typename Derived >
double qpp::concurrence (
             const Eigen::MatrixBase< Derived > & A )
```

Wootters concurrence of the bi-partite qubit mixed state *A*.

Parameters

A	Eigen expression

Returns

Wootters concurrence

6.1.3.13 contfrac2x()

```
double qpp::contfrac2x (
             const std::vector< int > & cf,
             idx N = idx(-1) )  [inline]
```

Real representation of a simple continued fraction.

See also

qpp::x2contfrac()

Note

If *N* is greater than the size of *cf* (by default it is), then all terms in *cf* are considered.

Parameters

cf	Integer vector containing the simple continued fraction expansion
N	Number of terms considered in the continued fraction expansion.

Returns

Real representation of the simple continued fraction

6.1.3.14 cor()

```
template<typename Container >
double qpp::cor (
```

```
            const dmat & probXY,
            const Container & X,
            const Container & Y,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Correlation.

Parameters

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
X	Real random variable values represented by an STL-like container
Y	Real random variable values represented by an STL-like container

Returns

Correlation of X and Y

6.1.3.15 cov()

```
template<typename Container >
double qpp::cov (
            const dmat & probXY,
            const Container & X,
            const Container & Y,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Covariance.

Parameters

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
X	Real random variable values represented by an STL-like container
Y	Real random variable values represented by an STL-like container

Returns

Covariance of X and Y

6.1.3.16 disp() [1/5]

```
template<typename Derived >
internal::IOManipEigen qpp::disp (
            const Eigen::MatrixBase< Derived > & A,
            double chop = qpp::chop )
```

Eigen expression ostream manipulator.

Parameters

A	Eigen expression
chop	Set to zero the elements smaller in absolute value than *chop*

Returns

Instance of qpp::internal::IOManipEigen

6.1.3.17 disp() [2/5]

```
internal::IOManipEigen qpp::disp (
            cplx z,
            double chop = qpp::chop )  [inline]
```

Complex number ostream manipulator.

Parameters

z	Complex number (or any other type implicitly cast-able to std::complex<double>)
chop	Set to zero the elements smaller in absolute value than *chop*

Returns

Instance of qpp::internal::IOManipEigen

6.1.3.18 disp() [3/5]

```
template<typename InputIterator >
internal::IOManipRange<InputIterator> qpp::disp (
            InputIterator first,
            InputIterator last,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )
```

Range ostream manipulator.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipRange

6.1.3.19 disp() [4/5]

```
template<typename Container >
internal::IOManipRange<typename Container::const_iterator> qpp::disp (
            const Container & c,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]",
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

Parameters

c	Container
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipRange

6.1.3.20 disp() [5/5]

```
template<typename PointerType >
internal::IOManipPointer<PointerType> qpp::disp (
            const PointerType * p,
            idx N,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )
```

C-style pointer ostream manipulator.

Parameters

p	Pointer to the first element
N	Number of elements to be displayed
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipPointer

6.1.3.21 egcd()

```
std::tuple<bigint, bigint, bigint> qpp::egcd (
            bigint a,
            bigint b )  [inline]
```

Extended greatest common divisor of two integers.

See also

qpp::gcd()

Parameters

a	Integer
b	Integer

Returns

Tuple of: 1. Integer m, 2. Integer n, and 3. Non-negative integer $gcd(a, b)$ such that $ma + nb = gcd(a, b)$

6.1.3.22 entanglement() [1/2]

```
template<typename Derived >
double qpp::entanglement (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

qpp::entropy()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Entanglement, with the logarithm in base 2

6.1.3.23 entanglement() [2/2]

```
template<typename Derived >
double qpp::entanglement (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

qpp::entropy()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Entanglement, with the logarithm in base 2

6.1.3.24 entropy() [1/2]

```
template<typename Derived >
double qpp::entropy (
            const Eigen::MatrixBase< Derived > & A )
```

von-Neumann entropy of the density matrix *A*

Parameters

A	Eigen expression

Returns

von-Neumann entropy, with the logarithm in base 2

6.1.3.25 entropy() [2/2]

```
double qpp::entropy (
            const std::vector< double > & prob ) [inline]
```

Shannon entropy of the probability distribution *prob*.

Parameters

prob	Real probability vector

Returns

Shannon entropy, with the logarithm in base 2

6.1.3.26 factors()

```
std::vector<bigint> qpp::factors (
            bigint a ) [inline]
```

Prime factor decomposition.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

a	Integer different from 0, 1 or -1

Returns

Integer vector containing the factors

6.1.3.27 gcd() [1/2]

```
bigint qpp::gcd (
            bigint a,
            bigint b ) [inline]
```

Greatest common divisor of two integers.

See also

qpp::lcm()

Parameters

a	Integer
b	Integer

Returns

Greatest common divisor of *a* and *b*

6.1.3.28 gcd() [2/2]

```
bigint qpp::gcd (
            const std::vector< bigint > & as )  [inline]
```

Greatest common divisor of a list of integers.

See also

qpp::lcm()

Parameters

as	List of integers

Returns

Greatest common divisor of all numbers in *as*

6.1.3.29 gconcurrence()

```
template<typename Derived >
double qpp::gconcurrence (
            const Eigen::MatrixBase< Derived > & A )
```

G-concurrence of the bi-partite pure state *A*.

Note

Both local dimensions must be equal

Uses qpp::logdet() to avoid overflows

See also

qpp::logdet()

Parameters

A	Eigen expression

Returns

G-concurrence

6.1.3.30 invperm()

```
std::vector<idx> qpp::invperm (
            const std::vector< idx > & perm )  [inline]
```

Inverse permutation.

Parameters

perm	Permutation

Returns

Inverse of the permutation *perm*

6.1.3.31 ip() [1/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
            const Eigen::MatrixBase< Derived > & phi,
            const Eigen::MatrixBase< Derived > & psi,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
subsys	Subsystem indexes over which *phi* is defined
dims	Dimensions of the multi-partite system

Returns

Inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.32 ip() [2/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
            const Eigen::MatrixBase< Derived > & phi,
            const Eigen::MatrixBase< Derived > & psi,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
subsys	Subsystem indexes over which *phi* is defined
d	Subsystem dimensions

Returns

Inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.33 isprime()

```
bool qpp::isprime (
            bigint p,
            idx k = 80 )  [inline]
```

Primality test based on the Miller-Rabin's algorithm.

Parameters

p	Integer different from 0, 1 or -1
k	Number of iterations. The probability of a false positive is 2^{-k}.

Returns

True if the number is (most-likely) prime, false otherwise

6.1.3.34 kraus2choi()

```
cmat qpp::kraus2choi (
            const std::vector< cmat > & Ks )  [inline]
```

Choi matrix.

See also

qpp::choi2kraus()

Constructs the Choi matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Note

The superoperator matrix S and the Choi matrix C are related by $S_{ab,mn} = C_{ma,nb}$

Parameters

Ks	Set of Kraus operators

Returns

Choi matrix

6.1.3.35 kraus2super()

```
cmat qpp::kraus2super (
            const std::vector< cmat > & Ks )  [inline]
```

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Parameters

Ks	Set of Kraus operators

Returns

Superoperator matrix

6.1.3.36 lcm() [1/2]

```
bigint qpp::lcm (
            bigint a,
            bigint b )  [inline]
```

Least common multiple of two integers.

See also

qpp::gcd()

Parameters

a	Integer
b	Integer

Returns

Least common multiple of *a* and *b*

6.1.3.37 lcm() [2/2]

```
bigint qpp::lcm (
            const std::vector< bigint > & as )  [inline]
```

Least common multiple of a list of integers.

See also

qpp::gcd()

Parameters

as	List of integers

Returns

Least common multiple of all numbers in *as*

6.1.3.38 load()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::load (
            const std::string & fname )
```

Loads Eigen matrix from a binary file (internal format) in double precision.

See also

qpp::save()

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
cmat mat = load<cmat>("input.bin");
```

Parameters

fname	Output file name

6.1.3.39 loadMATLAB() [1/2]

```
template<typename Derived >
std::enable_if<std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat<cplx> >::type
qpp::loadMATLAB (
            const std::string & mat_file,
            const std::string & var_name )
```

Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

qpp::saveMATLAB()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen ket
// from the MATLAB file "input.mat"
ket psi = loadMATLAB<ket>("input.mat");
```

Template Parameters

Derived	Complex Eigen type

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen dynamic matrix

6.1.3.40 loadMATLAB() [2/2]

```
template<typename Derived >
std::enable_if<!std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat<typename Derived↩
::Scalar> >::type qpp::loadMATLAB (
            const std::string & mat_file,
            const std::string & var_name )
```

Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

qpp::saveMATLAB()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
dmat mat = loadMATLAB<dmat>("input.mat");
```

Template Parameters

Derived	Non-complex Eigen type

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen dynamic matrix

6.1.3.41 lognegativity() [1/2]

```
template<typename Derived >
double qpp::lognegativity (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Logarithmic negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.42 lognegativity() [2/2]

```
template<typename Derived >
double qpp::lognegativity (
             const Eigen::MatrixBase< Derived > & A,
             idx d = 2 )
```

Logarithmic negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.43 marginalX()

```
std::vector<double> qpp::marginalX (
             const dmat & probXY )  [inline]
```

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)

Returns

Real vector consisting of the marginal distribution of *X*

6.1.3.44 marginalY()

```
std::vector<double> qpp::marginalY (
             const dmat & probXY )  [inline]
```

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)

Returns

Real vector consisting of the marginal distribution of *Y*

6.1.3.45 measure() [1/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks )
```

Measures the state *A* using the set of Kraus operators *Ks*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.46 measure() [2/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks )
```

Measures the state *A* using the set of Kraus operators *Ks*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.47 measure() [3/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & U )
```

Measures the state *A* in the orthonormal basis specified by the unitary matrix *U*.

Parameters

A	Eigen expression
U	Unitary matrix whose columns represent the measurement basis vectors

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.48 measure() [4/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.49 measure() [5/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.50 measure() [6/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.51 measure() [7/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.52 measure() [8/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & V,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

qpp::measure_seq()

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
V	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.53 measure() [9/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & V,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

qpp::measure_seq()

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
V	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.54 measure_seq() [1/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
            const Eigen::MatrixBase< Derived > & A,
            std::vector< idx > subsys,
            std::vector< idx > dims )
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

qpp::measure()

Parameters

A	Eigen expression
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.55 measure_seq() [2/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
            const Eigen::MatrixBase< Derived > & A,
            std::vector< idx > subsys,
            idx d = 2 )
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

qpp::measure()

Parameters

A	Eigen expression
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.56 modinv()

```
bigint qpp::modinv (
            bigint a,
            bigint p )  [inline]
```

Modular inverse of *a* mod *p*.

See also

qpp::egcd()

Note

a and *p* must be co-prime

Parameters

a	Non-negative integer
p	Non-negative integer

Returns

Modular inverse $a^{-1} \mod p$

6.1.3.57 modmul()

```
bigint qpp::modmul (
            bigint a,
            bigint b,
            bigint p )  [inline]
```

Modular multiplication without overflow.

Computes $ab \mod p$ without overflow

Parameters

a	Integer
b	Integer
p	Positive integer

Returns

$ab \mod p$ avoiding overflow

6.1.3.58 modpow()

```
bigint qpp::modpow (
            bigint a,
            bigint n,
            bigint p )  [inline]
```

Fast integer power modulo *p* based on the SQUARE-AND-MULTIPLY algorithm.

Note

Uses qpp::modmul() that avoids overflows

Computes $a^n \mod p$

Parameters

a	Non-negative integer
n	Non-negative integer
p	Strictly positive integer

Returns

$a^n \bmod p$

6.1.3.59 negativity() [1/2]

```
template<typename Derived >
double qpp::negativity (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Negativity

6.1.3.60 negativity() [2/2]

```
template<typename Derived >
double qpp::negativity (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Negativity

6.1.3.61 omega()

```
cplx qpp::omega (
            idx D )  [inline]
```

D-th root of unity.

Parameters

D	Non-negative integer

Returns

D-th root of unity $\exp(2\pi i/D)$

6.1.3.62 operator"""" _i() [1/2]

```
constexpr cplx qpp::operator"" _i (
            unsigned long long int x )  [inline], [noexcept]
```

User-defined literal for complex $i = \sqrt{-1}$ (integer overload)

Example:

```
cplx z = 4_i; // type of z is std::complex<double>
```

6.1.3.63 operator"""" _i() [2/2]

```
constexpr cplx qpp::operator"" _i (
            long double x )  [inline], [noexcept]
```

User-defined literal for complex $i = \sqrt{-1}$ (real overload)

Example:

```
cplx z = 4.5_i; // type of z is std::complex<double>
```

6.1.3.64 ptrace() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.65 ptrace() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
d	Subsystem dimensions

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.66 ptrace1() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Partial trace $Tr_A(\cdot)$ over the first subsytem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.67 ptrace1() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Partial trace $Tr_A(\cdot)$ over the first subsytem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.68 ptrace2() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Partial trace $Tr_B(\cdot)$ over the second subsytem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.69 ptrace2() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
             const Eigen::MatrixBase< Derived > & A,
             idx d = 2 )
```

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Partial trace $Tr_B(\cdot)$ over the second subsytem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.70 ptranspose() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
```

```
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.71 ptranspose() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
d	Subsystem dimensions

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.72 qmutualinfo() [1/2]

```
template<typename Derived >
double qpp::qmutualinfo (
```

```
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsysA,
            const std::vector< idx > & subsysB,
            const std::vector< idx > & dims )
```

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
dims	Dimensions of the multi-partite system

Returns

Mutual information between the 2 subsystems

6.1.3.73 qmutualinfo() [2/2]

```
template<typename Derived >
double qpp::qmutualinfo (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsysA,
            const std::vector< idx > & subsysB,
            idx d = 2 )
```

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
d	Subsystem dimensions

Returns

Mutual information between the 2 subsystems

6.1.3.74 rand() [1/5]

```
double qpp::rand (
            double a,
            double b )  [inline]
```

Generates a random real number uniformly distributed in the interval [a, b)

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real number (double) uniformly distributed in the interval [a, b)

6.1.3.75 rand() [2/5]

```
bigint qpp::rand (
              bigint a,
              bigint b )  [inline]
```

Generates a random big integer uniformly distributed in the interval [a, b].

Note

To avoid ambiguity with double qpp::rand(double, double) cast at least one of the arguments to qpp::bigint

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.76 rand() [3/5]

```
template<typename Derived >
Derived qpp::rand (
              idx rows,
              idx cols,
              double a = 0,
              double b = 1 )
```

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED_TYPE. It is specialized only for qpp::dmat and qpp::cmat

6.1.3.77 rand() [4/5]

```
template<>
dmat qpp::rand (
              idx rows,
              idx cols,
              double a,
              double b )  [inline]
```

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries uniformly distributed in [-1,1)
dmat mat = rand<dmat>(3, 3, -1, 1);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real matrix

6.1.3.78 rand() [5/5]

```
template<>
cmat qpp::rand (
              idx rows,
              idx cols,
              double a,
              double b )  [inline]
```

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) uniformly distributed in [-1,1)
cmat mat = rand<cmat>(3, 3, -1, 1);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random complex matrix

6.1.3.79 randH()

```
cmat qpp::randH (
            idx D = 2 )  [inline]
```

Generates a random Hermitian matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random Hermitian matrix

6.1.3.80 randidx()

```
idx qpp::randidx (
            idx a = std::numeric_limits<idx>::min(),
            idx b = std::numeric_limits<idx>::max() )  [inline]
```

Generates a random index (idx) uniformly distributed in the interval [a, b].

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

Returns

Random index (idx) uniformly distributed in the interval [a, b]

6.1.3.81 randket()

```
ket qpp::randket (
            idx D = 2 )  [inline]
```

Generates a random normalized ket (pure state vector)

Parameters

D	Dimension of the Hilbert space

Returns

Random normalized ket

6.1.3.82 randkraus()

```
std::vector<cmat> qpp::randkraus (
            idx N,
            idx D = 2 )  [inline]
```

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition $\sum_i K_i^\dagger K_i = I$

Parameters

N	Number of Kraus operators
D	Dimension of the Hilbert space

Returns

Set of *N* Kraus operators satisfying the closure condition

6.1.3.83 randn() [1/4]

```
template<typename Derived >
Derived qpp::randn (
            idx rows,
            idx cols,
            double mean = 0,
            double sigma = 1 )
```

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED_TYPE. It is specialized only for qpp::dmat and qpp::cmat

6.1.3.84 randn() [2/4]

```
template<>
dmat qpp::randn (
              idx rows,
              idx cols,
              double mean,
              double sigma )  [inline]
```

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries normally distributed in N(0,2)
dmat mat = randn<dmat>(3, 3, 0, 2);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Returns

Random real matrix

6.1.3.85 randn() [3/4]

```
template<>
cmat qpp::randn (
              idx rows,
              idx cols,
              double mean,
              double sigma )  [inline]
```

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) normally distributed in N(0,2)
cmat mat = randn<cmat>(3, 3, 0, 2);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Returns

Random complex matrix

6.1.3.86 randn() [4/4]

```
double qpp::randn (
            double mean = 0,
            double sigma = 1 )  [inline]
```

Generates a random real number (double) normally distributed in N(mean, sigma)

Parameters

mean	Mean
sigma	Standard deviation

Returns

Random real number normally distributed in N(mean, sigma)

6.1.3.87 randperm()

```
std::vector<idx> qpp::randperm (
            idx N )  [inline]
```

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by std::shuffle), so that all permutations are equally probable

Parameters

N	Size of the permutation

Returns

Random permutation of size *N*

6.1.3.88 randprime()

```
bigint qpp::randprime (
            bigint a,
            bigint b,
            idx N = 1000 )  [inline]
```

Generates a random big prime uniformly distributed in the interval [a, b].

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it
N	Maximum number of candidates

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.89 randprob()

```
std::vector<double> qpp::randprob (
            idx N )  [inline]
```

Generates a random probability vector uniformly distributed over the probability simplex.

Parameters

N	Size of the probability vector

Returns

Random probability vector

6.1.3.90 randrho()

```
cmat qpp::randrho (
            idx D = 2 )  [inline]
```

Generates a random density matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random density matrix

6.1.3.91 randU()

```
cmat qpp::randU (
              idx D = 2 )  [inline]
```

Generates a random unitary matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random unitary

6.1.3.92 randV()

```
cmat qpp::randV (
              idx Din,
              idx Dout )  [inline]
```

Generates a random isometry matrix.

Parameters

Din	Size of the input Hilbert space
Dout	Size of the output Hilbert space

Returns

Random isometry matrix

6.1.3.93 renyi() [1/2]

```
template<typename Derived >
double qpp::renyi (
             const Eigen::MatrixBase< Derived > & A,
             double alpha )
```

Renyi- α entropy of the density matrix *A*, for $\alpha \geq 0$.

Note

When $\alpha \to 1$ the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

Parameters

A	Eigen expression
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.94 renyi() [2/2]

```
double qpp::renyi (
             const std::vector< double > & prob,
             double alpha )  [inline]
```

Renyi- α entropy of the probability distribution *prob*, for $\alpha \geq 0$.

Note

When $\alpha \to 1$ the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

Parameters

prob	Real probability vector
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.95 save()

```
template<typename Derived >
void qpp::save (
             const Eigen::MatrixBase< Derived > & A,
             const std::string & fname )
```

Saves Eigen expression to a binary file (internal format) in double precision.

See also

qpp::load()

Parameters

A	Eigen expression
fname	Output file name

6.1.3.96 saveMATLAB() [1/2]

```
template<typename Derived >
std::enable_if< std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
             const Eigen::MatrixBase< Derived > & A,
             const std::string & mat_file,
             const std::string & var_name,
             const std::string & mode )
```

Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

qpp::loadMATLAB()

Template Parameters

Complex	Eigen type

Parameters

A	Eigen expression over the complex field
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB *matOpen()* documentation for details

6.1.3.97 saveMATLAB() [2/2]

```
template<typename Derived >
std::enable_if< !std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
            const Eigen::MatrixBase< Derived > & A,
            const std::string & mat_file,
            const std::string & var_name,
            const std::string & mode )
```

Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

qpp::loadMATLAB()

Template Parameters

Npn-complex	Eigen type

Parameters

A	Non-complex Eigen expression
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB *matOpen()* documentation for details

6.1.3.98 schmidtA() [1/2]

```
template<typename Derived >
cmat qpp::schmidtA (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt basis on Alice side.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.99 schmidtA() [2/2]

```
template<typename Derived >
cmat qpp::schmidtA (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt basis on Alice side.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.100 schmidtB() [1/2]

```
template<typename Derived >
cmat qpp::schmidtB (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt basis on Bob side.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.101 schmidtB() [2/2]

```
template<typename Derived >
cmat qpp::schmidtB (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt basis on Bob side.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.102 schmidtcoeffs() [1/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< idx > & dims )
```

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

qpp::schmidtprobs()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Schmidt coefficients of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.103 schmidtcoeffs() [2/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
             const Eigen::MatrixBase< Derived > & A,
             idx d = 2 )
```

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

qpp::schmidtprobs()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Schmidt coefficients of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.104 schmidtprobs() [1/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

qpp::schmidtcoeffs()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Real vector consisting of the Schmidt probabilites of *A*, ordered in decreasing order

6.1.3.105 schmidtprobs() [2/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
```

```
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

qpp::schmidtcoeffs()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Real vector consisting of the Schmidt probabilites of *A*, ordered in decreasing order

6.1.3.106 sigma()

```
template<typename Container >
double qpp::sigma (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Standard deviation.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Standard deviation of *X*

6.1.3.107 super2choi()

```
cmat qpp::super2choi (
            const cmat & A )  [inline]
```

Converts superoperator matrix to Choi matrix.

See also

qpp::choi2super()

Parameters

A	Superoperator matrix

Returns

Choi matrix

6.1.3.108 syspermute() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & perm,
            const std::vector< idx > & dims )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

Parameters

A	Eigen expression
perm	Permutation
dims	Dimensions of the multi-partite system

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.109 syspermute() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & perm,
            idx d = 2 )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

Parameters

A	Eigen expression
perm	Permutation
d	Subsystem dimensions

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.110 tsallis() [1/2]

```
template<typename Derived >
double qpp::tsallis (
            const Eigen::MatrixBase< Derived > & A,
            double q )
```

Tsallis- q entropy of the density matrix *A*, for $q \geq 0$.

Note

When $q \to 1$ the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base e

Parameters

A	Eigen expression
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.111 tsallis() [2/2]

```
double qpp::tsallis (
            const std::vector< double > & prob,
            double q )  [inline]
```

Tsallis- q entropy of the probability distribution *prob*, for $q \geq 0$.

Note

When $q \to 1$ the Tsallis entropy converges to the Shannon entropy, with the logarithm in base e

Parameters

prob	Real probability vector
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.112 uniform()

```
std::vector<double> qpp::uniform (
            idx N )  [inline]
```

Uniform probability distribution vector.

Parameters

N	Size of the alphabet

Returns

Real vector consisting of a uniform distribution of size *N*

6.1.3.113 var()

```
template<typename Container >
double qpp::var (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Variance.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Variance of *X*

6.1.3.114 x2contfrac()

```
std::vector<int> qpp::x2contfrac (
            double x,
            idx N,
            idx cut = 1e5 )  [inline]
```

Simple continued fraction expansion.

See also

qpp::contfrac2x()

Parameters

x	Real number
N	Maximum number of terms in the expansion
cut	Stop the expansion when the next term is greater than *cut*

Returns

Integer vector containing the simple continued fraction expansion of *x*. If there are *M* less than *N* terms in the expansion, a shorter vector with *M* components is returned.

6.1.4 Variable Documentation

6.1.4.1 chop

```
constexpr double qpp::chop = 1e-10
```

Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.

6.1.4.2 ee

```
constexpr double qpp::ee = 2.71828182845904523536028747135266249 7
```

Base of natural logarithm, e.

6.1.4.3 eps

```
constexpr double qpp::eps = 1e-12
```

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::eps) // x is zero
```

6.1.4.4 infty

```
constexpr double qpp::infty = std::numeric_limits<double>::max()
```

Used to denote infinity in double precision.

6.1.4.5 maxn

```
constexpr idx qpp::maxn = 64
```

Maximum number of allowed qubits/qudits (subsystems)

Used internally to allocate arrays on the stack (for performance reasons):

6.1.4.6 pi

```
constexpr double qpp::pi = 3.14159265358979323846264338327950288 4
```

π

6.2 qpp::exception Namespace Reference

Quantum++ exception hierarchy namespace.

Classes

- class CustomException
  Custom exception.
- class DimsInvalid
  Invalid dimension(s) exception.
- class DimsMismatchCvector
  Dimension(s) mismatch column vector size exception.
- class DimsMismatchMatrix
  Dimension(s) mismatch matrix size exception.
- class DimsMismatchRvector
  Dimension(s) mismatch row vector size exception.
- class DimsMismatchVector
  Dimension(s) mismatch vector size exception.
- class DimsNotEqual
  Dimensions not equal exception.
- class Exception
  Base class for generating Quantum++ custom exceptions.
- class MatrixMismatchSubsys
  Matrix mismatch subsystems exception.
- class MatrixNotCvector

Matrix is not a column vector exception.

- class MatrixNotRvector

  Matrix is not a row vector exception.
- class MatrixNotSquare

  Matrix is not square exception.
- class MatrixNotSquareNorCvector

  Matrix is not square nor column vector exception.
- class MatrixNotSquareNorRvector

  Matrix is not square nor row vector exception.
- class MatrixNotSquareNorVector

  Matrix is not square nor vector exception.
- class MatrixNotVector

  Matrix is not a vector exception.
- class NoCodeword

  Codeword does not exist exception.
- class NotBipartite

  Not bi-partite exception.
- class NotQubitCvector

  Column vector is not 2 x 1 exception.
- class NotQubitMatrix

  Matrix is not 2 x 2 exception.
- class NotQubitRvector

  Row vector is not 1 x 2 exception.
- class NotQubitSubsys

  Subsystems are not qubits exception.
- class NotQubitVector

  Vector is not 2 x 1 nor 1 x 2 exception.
- class OutOfRange

  Parameter out of range exception.
- class PermInvalid

  Invalid permutation exception.
- class PermMismatchDims

  Permutation mismatch dimensions exception.
- class SizeMismatch

  Size mismatch exception.
- class SubsysMismatchDims

  Subsystems mismatch dimensions exception.
- class TypeMismatch

  Type mismatch exception.
- class UndefinedType

  Not defined for this type exception.
- class Unknown

  Unknown exception.
- class ZeroSize

  Object has zero size exception.

6.2.1 Detailed Description

Quantum++ exception hierarchy namespace.

6.3 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

Classes

- class Bit_circuit
- class Dynamic_bitset

6.3.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

6.4 qpp::internal Namespace Reference

Internal utility functions, do not use them directly or modify them.

Classes

- struct Display_Impl_
- class IOManipEigen
- class IOManipPointer
- class IOManipRange
- class Singleton

  Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Functions

- void n2multiidx (idx n, idx numdims, const idx *const dims, idx *result) noexcept
- idx multiidx2n (const idx *const midx, idx numdims, const idx *const dims) noexcept
- template<typename Derived >
  bool check_square_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool check_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool check_rvector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool check_cvector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
  bool check_nonzero_size (const T &x) noexcept
- template<typename T1 , typename T2 >
  bool check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept
- bool check_dims (const std::vector< idx > &dims)
- template<typename Derived >
  bool check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)

- template<typename Derived >
  bool check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- bool check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept
- bool check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template<typename Derived >
  bool check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept
- bool check_perm (const std::vector< idx > &perm)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::↩
  MatrixBase< Derived2 > &B)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen↩
  ::MatrixBase< Derived2 > &B)
- template<typename T >
  void variadic_vector_emplace (std::vector< T > &)
- template<typename T , typename First , typename... Args>
  void variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)
- idx get_num_subsys (idx sz, idx d)
- idx get_dim_subsys (idx sz, idx N)

6.4.1 Detailed Description

Internal utility functions, do not use them directly or modify them.

6.4.2 Function Documentation

6.4.2.1 check_cvector()

```
template<typename Derived >
bool qpp::internal::check_cvector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.2 check_dims()

```
bool qpp::internal::check_dims (
            const std::vector< idx > & dims )  [inline]
```

6.4.2.3 check_dims_match_cvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_cvect (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.4 check_dims_match_mat()

```
template<typename Derived >
bool qpp::internal::check_dims_match_mat (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.5 check_dims_match_rvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_rvect (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.6 check_eq_dims()

```
bool qpp::internal::check_eq_dims (
            const std::vector< idx > & dims,
            idx dim )  [inline], [noexcept]
```

6.4.2.7 check_matching_sizes()

```
template<typename T1 , typename T2 >
bool qpp::internal::check_matching_sizes (
            const T1 & lhs,
            const T2 & rhs )  [noexcept]
```

6.4.2.8 check_nonzero_size()

```
template<typename T >
bool qpp::internal::check_nonzero_size (
            const T & x )  [noexcept]
```

6.4.2.9 check_perm()

```
bool qpp::internal::check_perm (
            const std::vector< idx > & perm )  [inline]
```

6.4.2.10 check_qubit_cvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_cvector (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.11 check_qubit_matrix()

```
template<typename Derived >
bool qpp::internal::check_qubit_matrix (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.12 check_qubit_rvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_rvector (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.13 check_qubit_vector()

```
template<typename Derived >
bool qpp::internal::check_qubit_vector (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.14 check_rvector()

```
template<typename Derived >
bool qpp::internal::check_rvector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.15 check_square_mat()

```
template<typename Derived >
bool qpp::internal::check_square_mat (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.16 check_subsys_match_dims()

```
bool qpp::internal::check_subsys_match_dims (
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )  [inline]
```

6.4.2.17 check_vector()

```
template<typename Derived >
bool qpp::internal::check_vector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.18 dirsum2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::dirsum2 (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

6.4.2.19 get_dim_subsys()

```
idx qpp::internal::get_dim_subsys (
            idx sz,
            idx N )  [inline]
```

6.4.2.20 get_num_subsys()

```
idx qpp::internal::get_num_subsys (
            idx sz,
            idx d )  [inline]
```

6.4.2.21 kron2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::kron2 (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

6.4.2.22 multiidx2n()

```
idx qpp::internal::multiidx2n (
            const idx *const midx,
            idx numdims,
            const idx *const dims )  [inline], [noexcept]
```

6.4.2.23 n2multiidx()

```
void qpp::internal::n2multiidx (
            idx n,
            idx numdims,
            const idx *const dims,
            idx * result )  [inline], [noexcept]
```

6.4.2.24 variadic_vector_emplace() [1/2]

```
template<typename T >
void qpp::internal::variadic_vector_emplace (
            std::vector< T > &  )
```

6.4.2.25 variadic_vector_emplace() [2/2]

```
template<typename T , typename First , typename...  Args>
void qpp::internal::variadic_vector_emplace (
            std::vector< T > & v,
            First && first,
            Args &&...  args )
```

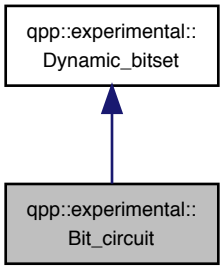
Chapter 7

Class Documentation

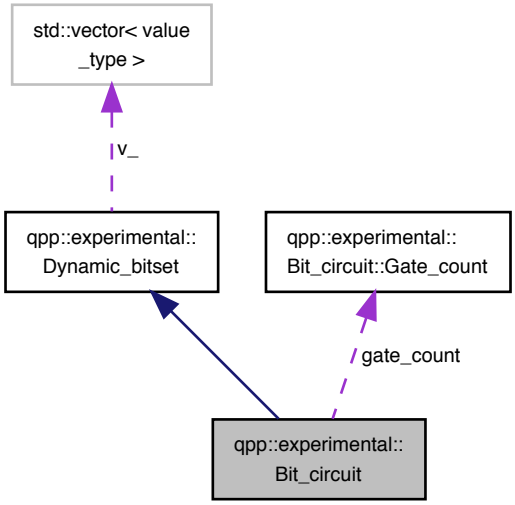
7.1 qpp::experimental::Bit_circuit Class Reference

```
#include <experimental/experimental.h>
```

Inheritance diagram for qpp::experimental::Bit_circuit:



Collaboration diagram for qpp::experimental::Bit_circuit:



Classes

- struct Gate_count

Public Member Functions

- Bit_circuit & X (idx pos)
- Bit_circuit & NOT (idx pos)
- Bit_circuit & CNOT (const std::vector< idx > &pos)
- Bit_circuit & TOF (const std::vector< idx > &pos)
- Bit_circuit & SWAP (const std::vector< idx > &pos)
- Bit_circuit & FRED (const std::vector< idx > &pos)
- Bit_circuit & reset () noexcept

Public Attributes

- struct qpp::experimental::Bit_circuit::Gate_count gate_count

Additional Inherited Members

7.1.1 Member Function Documentation

7.1.1.1 CNOT()

```
Bit_circuit& qpp::experimental::Bit_circuit::CNOT (
             const std::vector< idx > & pos )  [inline]
```

7.1.1.2 FRED()

```
Bit_circuit& qpp::experimental::Bit_circuit::FRED (
             const std::vector< idx > & pos )  [inline]
```

7.1.1.3 NOT()

```
Bit_circuit& qpp::experimental::Bit_circuit::NOT (
             idx pos )  [inline]
```

7.1.1.4 reset()

```
Bit_circuit& qpp::experimental::Bit_circuit::reset ( )  [inline], [noexcept]
```

7.1.1.5 SWAP()

```
Bit_circuit& qpp::experimental::Bit_circuit::SWAP (
             const std::vector< idx > & pos )  [inline]
```

7.1.1.6 TOF()

```
Bit_circuit& qpp::experimental::Bit_circuit::TOF (
             const std::vector< idx > & pos )  [inline]
```

7.1.1.7 X()

```
Bit_circuit& qpp::experimental::Bit_circuit::X (
             idx pos )  [inline]
```

7.1.2 Member Data Documentation

7.1.2.1 gate_count

```
struct qpp::experimental::Bit_circuit::Gate_count qpp::experimental::Bit_circuit::gate_count
```

The documentation for this class was generated from the following file:

- experimental/experimental.h

7.2 qpp::Bit_circuit Class Reference

Classical reversible circuit simulator.

```
#include <experimental/experimental.h>
```

7.2.1 Detailed Description

Classical reversible circuit simulator.

The documentation for this class was generated from the following file:

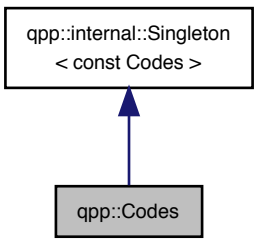
- experimental/experimental.h

7.3 qpp::Codes Class Reference

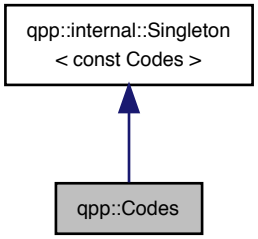
const Singleton class that defines quantum error correcting codes

```
#include <classes/codes.h>
```

Inheritance diagram for qpp::Codes:



Collaboration diagram for qpp::Codes:



Public Types

- enum Type { Type::FIVE_QUBIT = 1, Type::SEVEN_QUBIT_STEANE, Type::NINE_QUBIT_SHOR }

  Code types, add more codes here if needed.

Public Member Functions

- ket codeword (Type type, idx i) const

  Returns the codeword of the specified code type.

Private Member Functions

- Codes ()

  Default constructor.
- ∼Codes ()=default

  Default destructor.

Friends

- class internal::Singleton< const Codes >

Additional Inherited Members

7.3.1 Detailed Description

const Singleton class that defines quantum error correcting codes

7.3.2 Member Enumeration Documentation

7.3.2.1 Type

```
enum qpp::Codes::Type  [strong]
```

Code types, add more codes here if needed.

See also

qpp::Codes::codeword()

Enumerator

FIVE_QUBIT	[[5,1,3]] qubit code
SEVEN_QUBIT_STEANE	[[7,1,3]] Steane qubit code
NINE_QUBIT_SHOR	[[9,1,3]] Shor qubit code

7.3.3 Constructor & Destructor Documentation

7.3.3.1 Codes()

```
qpp::Codes::Codes ( )  [inline], [private]
```

Default constructor.

7.3.3.2 ~Codes()

```
qpp::Codes::~Codes ( )  [private], [default]
```

Default destructor.

7.3.4 Member Function Documentation

7.3.4.1 codeword()

```
ket qpp::Codes::codeword (
            Type type,
            idx i ) const  [inline]
```

Returns the codeword of the specified code type.

See also

qpp::Codes::Type

Parameters

type	Code type
i	Codeword index

Returns

i-th codeword of the code *type*

7.3.5 Friends And Related Function Documentation

7.3.5.1 internal::Singleton< const Codes >

```
friend class internal::Singleton< const Codes > [friend]
```

The documentation for this class was generated from the following file:

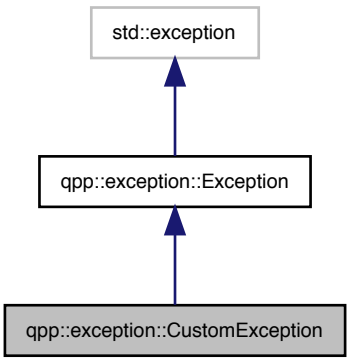
- classes/codes.h

7.4 qpp::exception::CustomException Class Reference

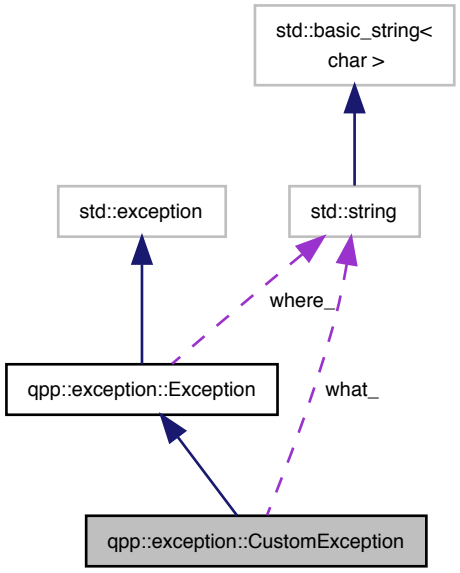
Custom exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::CustomException:



Collaboration diagram for qpp::exception::CustomException:



Public Member Functions

- CustomException (const std::string &where, const std::string &what)

Private Member Functions

- std::string type_description () const override

  Exception type description.

Private Attributes

- std::string what_ {}

7.4.1 Detailed Description

Custom exception.

Custom exception, the user must provide a custom message

7.4.2 Constructor & Destructor Documentation

7.4.2.1 CustomException()

```
qpp::exception::CustomException::CustomException (
            const std::string & where,
            const std::string & what )  [inline]
```

7.4.3 Member Function Documentation

7.4.3.1 type_description()

```
std::string qpp::exception::CustomException::type_description ( ) const  [inline], [override],
[private], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

7.4.4 Member Data Documentation

7.4.4.1 what_

```
std::string qpp::exception::CustomException::what_ {}  [private]
```

The documentation for this class was generated from the following file:

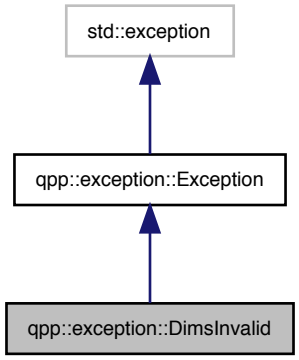
- classes/exception.h

7.5 qpp::exception::DimsInvalid Class Reference

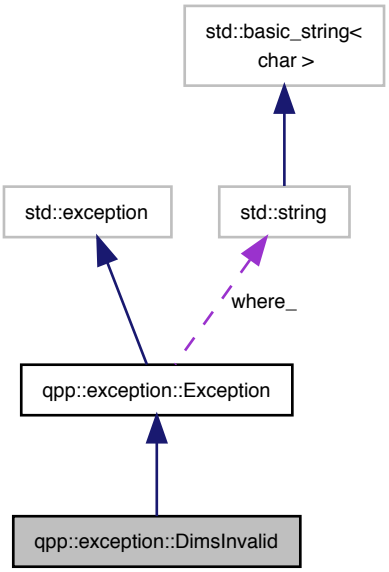
Invalid dimension(s) exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsInvalid:



Collaboration diagram for qpp::exception::DimsInvalid:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.5.1 Detailed Description

Invalid dimension(s) exception.

std::vector<idx> of dimensions has zero size or contains zeros

7.5.2 Member Function Documentation

7.5.2.1 type_description()

```
std::string qpp::exception::DimsInvalid::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

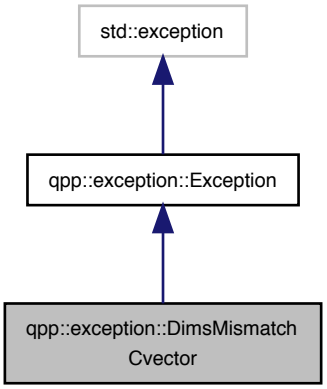
- classes/exception.h

7.6 qpp::exception::DimsMismatchCvector Class Reference

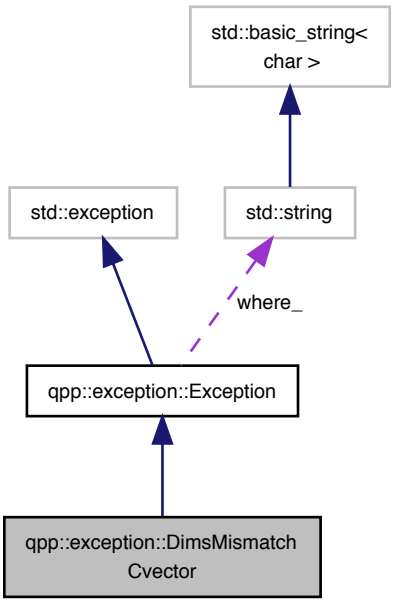
Dimension(s) mismatch column vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchCvector:



Collaboration diagram for qpp::exception::DimsMismatchCvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.6.1 Detailed Description

Dimension(s) mismatch column vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩ Matrix (assumed to be a column vector)

7.6.2 Member Function Documentation

7.6.2.1 type_description()

```
std::string qpp::exception::DimsMismatchCvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

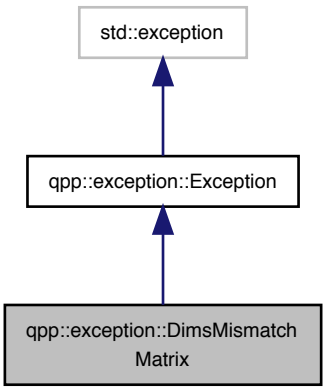
- classes/exception.h

7.7 qpp::exception::DimsMismatchMatrix Class Reference

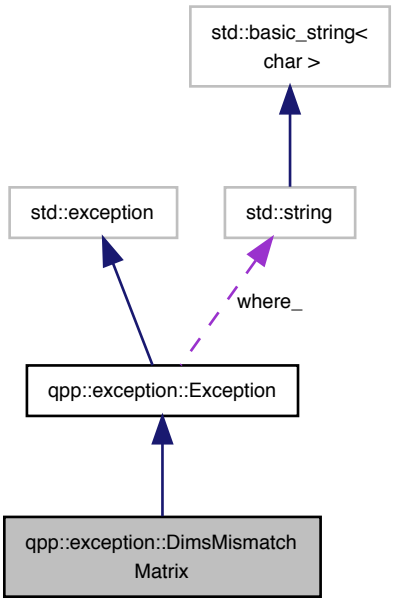
Dimension(s) mismatch matrix size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchMatrix:



Collaboration diagram for qpp::exception::DimsMismatchMatrix:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.7.1 Detailed Description

Dimension(s) mismatch matrix size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of rows of the Eigen::Matrix (assumed to be a square matrix)

7.7.2 Member Function Documentation

7.7.2.1 type_description()

```
std::string qpp::exception::DimsMismatchMatrix::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

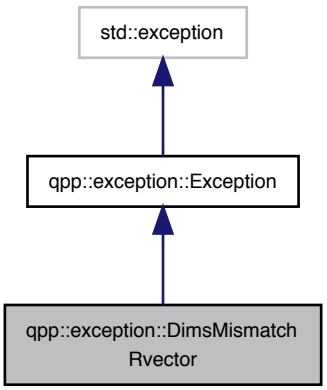
- classes/exception.h

7.8 qpp::exception::DimsMismatchRvector Class Reference

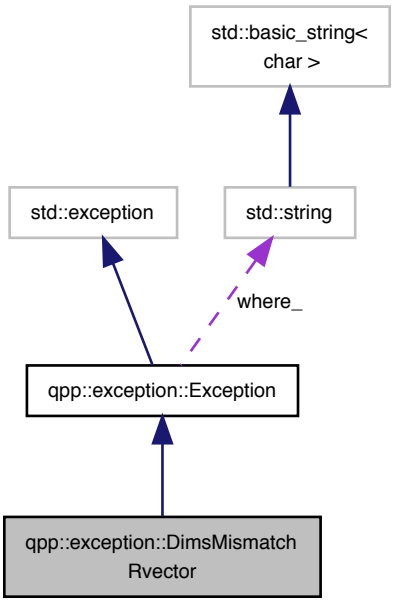
Dimension(s) mismatch row vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchRvector:



Collaboration diagram for qpp::exception::DimsMismatchRvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.8.1 Detailed Description

Dimension(s) mismatch row vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩
Matrix (assumed to be a row vector)

7.8.2 Member Function Documentation

7.8.2.1 type_description()

```
std::string qpp::exception::DimsMismatchRvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

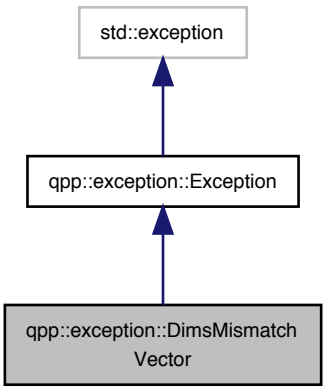
- classes/exception.h

7.9 qpp::exception::DimsMismatchVector Class Reference

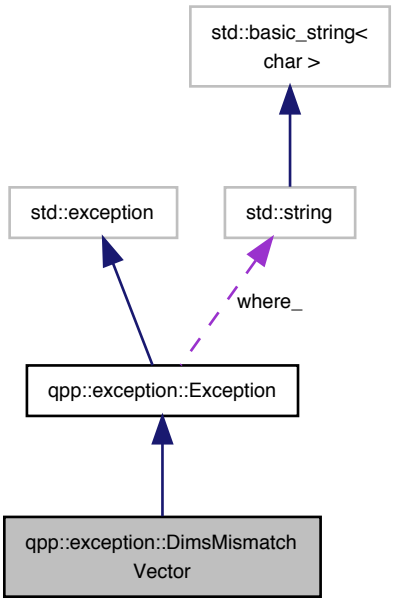
Dimension(s) mismatch vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchVector:



Collaboration diagram for qpp::exception::DimsMismatchVector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.9.1 Detailed Description

Dimension(s) mismatch vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩
Matrix (assumed to be a row/column vector)

7.9.2 Member Function Documentation

7.9.2.1 type_description()

```
std::string qpp::exception::DimsMismatchVector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

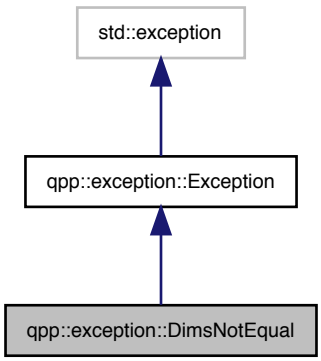
- classes/exception.h

7.10 qpp::exception::DimsNotEqual Class Reference

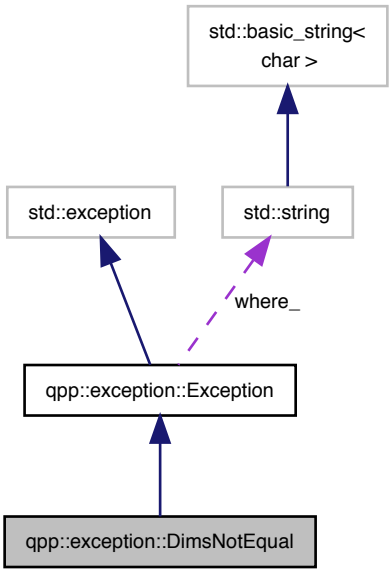
Dimensions not equal exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsNotEqual:



Collaboration diagram for qpp::exception::DimsNotEqual:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.10.1 Detailed Description

Dimensions not equal exception.

Local/global dimensions are not equal

7.10.2 Member Function Documentation

7.10.2.1 type_description()

```
std::string qpp::exception::DimsNotEqual::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

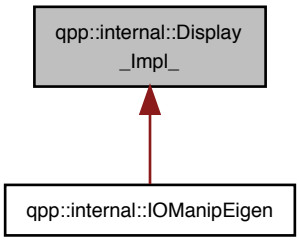
The documentation for this class was generated from the following file:

- classes/exception.h

7.11 qpp::internal::Display_Impl_ Struct Reference

`#include <internal/util.h>`

Inheritance diagram for qpp::internal::Display_Impl_:



Public Member Functions

- template<typename T >
  std::ostream & display_impl_ (const T &A, std::ostream &os, double chop=qpp::chop) const

7.11.1 Member Function Documentation

7.11.1.1 display_impl_()

```
template<typename T >
std::ostream& qpp::internal::Display_Impl_::display_impl_ (
             const T & A,
             std::ostream & os,
             double chop = qpp::chop ) const  [inline]
```

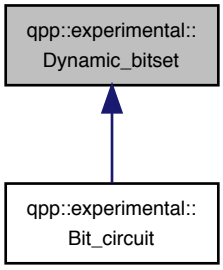
The documentation for this struct was generated from the following file:

- internal/util.h

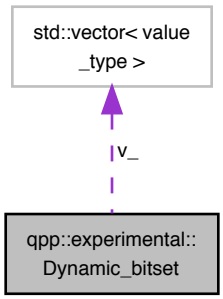
7.12 qpp::experimental::Dynamic_bitset Class Reference

`#include <experimental/experimental.h>`

Inheritance diagram for qpp::experimental::Dynamic_bitset:



Collaboration diagram for qpp::experimental::Dynamic_bitset:



Public Types

- using value_type = unsigned int

  Type of the storage elements.
- using storage_type = std::vector< value_type >

  Type of the storage.

Public Member Functions

- Dynamic_bitset (idx N)

  Constructor, initializes all bits to false (zero)
- const storage_type & data () const

  Raw storage space of the bitset.
- idx size () const

  Number of bits stored in the bitset.
- idx storage_size () const

  Size of the underlying storage space (in units of value_type, unsigned int by default)
- idx count () const noexcept
- bool get (idx pos) const
- bool none () const noexcept
- bool all () const noexcept
- bool any () const noexcept
- Dynamic_bitset & set (idx pos, bool value=true)
- Dynamic_bitset & set () noexcept
- Dynamic_bitset & rand (idx pos, double p=0.5)
- Dynamic_bitset & rand (double p=0.5)
- Dynamic_bitset & reset (idx pos)
- Dynamic_bitset & reset () noexcept
- Dynamic_bitset & flip (idx pos)
- Dynamic_bitset & flip () noexcept
- bool operator== (const Dynamic_bitset &rhs) const noexcept
- bool operator!= (const Dynamic_bitset &rhs) const noexcept
- template<class CharT = char, class Traits = std::char_traits<CharT>, class Allocator = std::allocator<CharT>>
  std::basic_string< CharT, Traits, Allocator > to_string (CharT zero=CharT('0'), CharT one=CharT('1')) const

Protected Member Functions

- idx index_ (idx pos) const

  Index of the pos bit in the storage space.
- idx offset_ (idx pos) const

  Offset of the pos bit in the storage space relative to its index.

Protected Attributes

- idx storage_size_

  Storage size.
- idx N_

  Number of bits.
- std::vector< value_type > v_

  Storage space.

Friends

- std::ostream & operator<< (std::ostream &os, const Dynamic_bitset &rhs)

7.12.1 Member Typedef Documentation

7.12.1.1 storage_type

```
using qpp::experimental::Dynamic_bitset::storage_type = std::vector<value_type>
```

Type of the storage.

7.12.1.2 value_type

```
using qpp::experimental::Dynamic_bitset::value_type = unsigned int
```

Type of the storage elements.

7.12.2 Constructor & Destructor Documentation

7.12.2.1 Dynamic_bitset()

```
qpp::experimental::Dynamic_bitset::Dynamic_bitset (
            idx N )  [inline]
```

Constructor, initializes all bits to false (zero)

Parameters

N	Number of bits in the bitset

7.12.3 Member Function Documentation

7.12.3.1 all()

```
bool qpp::experimental::Dynamic_bitset::all ( ) const  [inline], [noexcept]
```

Returns

7.12.3.2 any()

```
bool qpp::experimental::Dynamic_bitset::any ( ) const  [inline], [noexcept]
```

Returns

7.12.3.3 count()

```
idx qpp::experimental::Dynamic_bitset::count ( ) const  [inline], [noexcept]
```

Returns

7.12.3.4 data()

```
const storage_type& qpp::experimental::Dynamic_bitset::data ( ) const  [inline]
```

Raw storage space of the bitset.

Returns

Const reference to the underlying storage space

7.12.3.5 flip() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::flip (
            idx pos )  [inline]
```

Parameters

pos	

Returns

7.12.3.6 flip() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::flip ( )  [inline], [noexcept]
```

Returns

7.12.3.7 get()

```
bool qpp::experimental::Dynamic_bitset::get (
            idx pos ) const  [inline]
```

Parameters

pos	

Returns

7.12.3.8 index_()

```
idx qpp::experimental::Dynamic_bitset::index_ (
            idx pos ) const  [inline], [protected]
```

Index of the *pos* bit in the storage space.

Parameters

pos	Bit location

Returns

Index of the *pos* bit in the storage space

7.12.3.9 none()

```
bool qpp::experimental::Dynamic_bitset::none ( ) const  [inline], [noexcept]
```

Returns

7.12.3.10 offset_()

```
idx qpp::experimental::Dynamic_bitset::offset_ (
            idx pos ) const  [inline], [protected]
```

Offset of the *pos* bit in the storage space relative to its index.

Parameters

pos	Bit location

Returns

Offset of the *pos* bit in the storage space relative to its index

7.12.3.11 operator"!=()

```
bool qpp::experimental::Dynamic_bitset::operator!= (
            const Dynamic_bitset & rhs ) const  [inline], [noexcept]
```

Parameters

rhs	

Returns

7.12.3.12 operator==()

```
bool qpp::experimental::Dynamic_bitset::operator== (
            const Dynamic_bitset & rhs ) const  [inline], [noexcept]
```

Parameters

rhs	

Returns

7.12.3.13 rand() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::rand (
            idx pos,
            double p = 0.5 )  [inline]
```

Parameters

pos	
p	

Returns

7.12.3.14 rand() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::rand (
            double p = 0.5 )  [inline]
```

Parameters

p	

Returns

7.12.3.15 reset() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::reset (
            idx pos )  [inline]
```

Parameters

pos	

Returns

7.12.3.16 reset() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::reset ( )  [inline], [noexcept]
```

Returns

7.12.3.17 set() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::set (
            idx pos,
            bool value = true )  [inline]
```

Parameters

pos	
value	

Returns

7.12.3.18 set() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::set ( )  [inline], [noexcept]
```

Returns

7.12.3.19 size()

```
idx qpp::experimental::Dynamic_bitset::size ( ) const  [inline]
```

Number of bits stored in the bitset.

Returns

Number of bits

7.12.3.20 storage_size()

```
idx qpp::experimental::Dynamic_bitset::storage_size ( ) const  [inline]
```

Size of the underlying storage space (in units of value_type, unsigned int by default)

Returns

Size of the underlying storage space

7.12.3.21 to_string()

```
template<class CharT = char, class Traits = std::char_traits<CharT>, class Allocator = std↩
::allocator<CharT>>
std::basic_string<CharT, Traits, Allocator> qpp::experimental::Dynamic_bitset::to_string (
            CharT zero = CharT('0'),
            CharT one = CharT('1') ) const  [inline]
```

Template Parameters

CharT	
Traits	
Allocator	

Parameters

zero	
one	

Returns

7.12.4 Friends And Related Function Documentation

7.12.4.1 operator<<

```
std::ostream& operator<< (
            std::ostream & os,
            const Dynamic_bitset & rhs )  [friend]
```

Parameters

os	
rhs	

Returns

7.12.5 Member Data Documentation

7.12.5.1 N_

```
idx qpp::experimental::Dynamic_bitset::N_  [protected]
```

Number of bits.

7.12.5.2 storage_size_

```
idx qpp::experimental::Dynamic_bitset::storage_size_  [protected]
```

Storage size.

7.12.5.3 v_

```
std::vector<value_type> qpp::experimental::Dynamic_bitset::v_  [protected]
```

Storage space.

The documentation for this class was generated from the following file:

- experimental/experimental.h

7.13 qpp::Dynamic_bitset Class Reference

Dynamic bitset class, allows the specification of the number of bits at runtime (unlike std::bitset<N>)

```
#include <experimental/experimental.h>
```

7.13.1 Detailed Description

Dynamic bitset class, allows the specification of the number of bits at runtime (unlike std::bitset<N>)

The documentation for this class was generated from the following file:

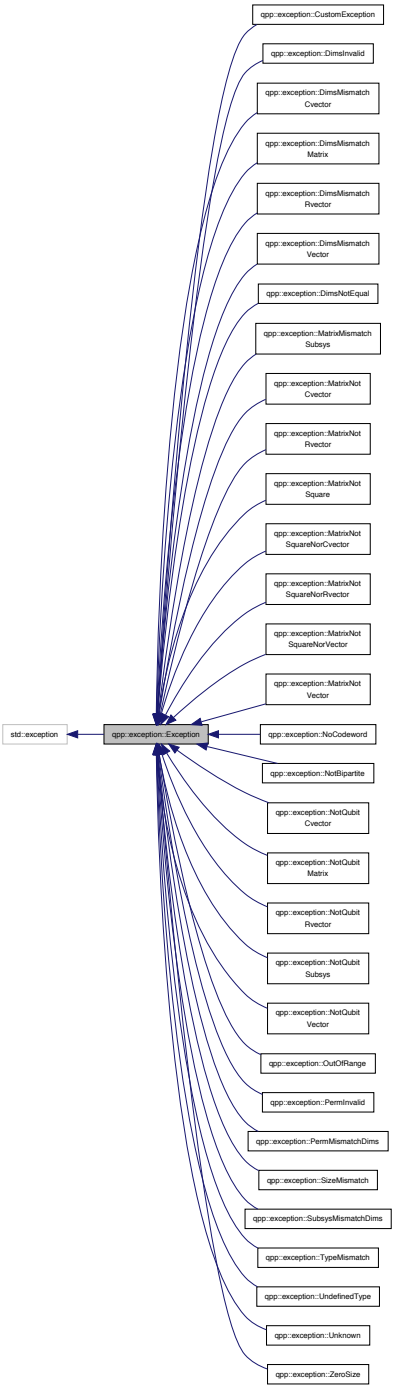
- experimental/experimental.h

7.14 qpp::exception::Exception Class Reference

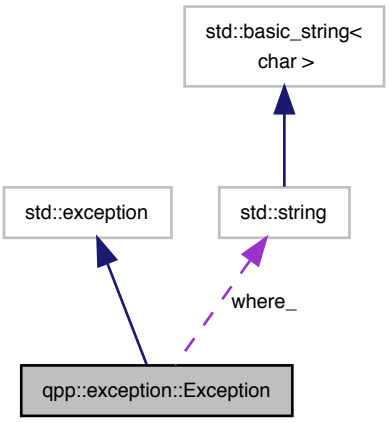
Base class for generating Quantum++ custom exceptions.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::Exception:



Collaboration diagram for qpp::exception::Exception:



Public Member Functions

- Exception (const std::string &where)

  Constructs an exception.
- virtual const char * what () const noexcept override

  Overrides std::exception::what()
- virtual std::string type_description () const =0

  Exception type description.

Private Attributes

- std::string where_

7.14.1 Detailed Description

Base class for generating Quantum++ custom exceptions.

Derive from this class if more exceptions are needed, making sure to override qpp::exception::Exception::type_description() in the derived class and to inherit the constructor qpp::exception::Exception::Exception(). Preferably keep your newly defined exception classes in the namespace qpp::exception.

Example:

```
namespace qpp
{
namespace exception
{
    class ZeroSize : public Exception
    {
    public:
        std::string type_description() const override
        {
            return "Object has zero size";
        }

        // inherit the base class' qpp::exception::Exception constructor
        using Exception::Exception;
    };
} // namespace exception
} // namespace qpp
```

7.14.2 Constructor & Destructor Documentation

7.14.2.1 Exception()

```
qpp::exception::Exception::Exception (
            const std::string & where )  [inline]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

7.14.3 Member Function Documentation

7.14.3.1 type_description()

```
std::string qpp::exception::Exception::type_description ( ) const  [inline], [pure virtual]
```

Exception type description.

Returns

Exception type description

Implemented in qpp::exception::CustomException, qpp::exception::UndefinedType, qpp::exception::SizeMismatch, qpp::exception::TypeMismatch, qpp::exception::OutOfRange, qpp::exception::NoCodeword, qpp::exception::NotBipartite, qpp::exception::NotQubitSubsys, qpp::exception::NotQubitVector, qpp::exception::NotQubitRvector, qpp::exception::NotQubitCvector, qpp::exception::NotQubitMatrix, qpp::exception::PermMismatchDims, qpp::exception::PermInvalid, qpp::exception::SubsysMismatchDims, qpp::exception::DimsMismatchVector, qpp::exception::DimsMismatchRvector, qpp::exception::DimsMismatchCvector, qpp::exception::DimsMismatchMatrix, qpp::exception::DimsNotEqual, qpp::exception::DimsInvalid, qpp::exception::MatrixMismatchSubsys, qpp::exception::MatrixNotSquareNorVector, qpp::exception::MatrixNotSquareNorRvector, qpp::exception::MatrixNotSquareNorCvector, qpp::exception::MatrixNotVector, qpp::exception::MatrixNotRvector, qpp::exception::MatrixNotCvector, qpp::exception::MatrixNotSquare, qpp::exception::ZeroSize, and qpp::exception::Unknown.

7.14.3.2 what()

```
virtual const char* qpp::exception::Exception::what ( ) const  [inline], [override], [virtual],
[noexcept]
```

Overrides std::exception::what()

Returns

Exception description

7.14.4 Member Data Documentation

7.14.4.1 where_

```
std::string qpp::exception::Exception::where_  [private]
```

The documentation for this class was generated from the following file:

- classes/exception.h

7.15 qpp::experimental::Bit_circuit::Gate_count Struct Reference

```
#include <experimental/experimental.h>
```

Public Attributes

- idx NOT = 0
- idx & X = NOT
- idx CNOT = 0
- idx SWAP = 0
- idx FRED = 0
- idx TOF = 0

7.15.1 Member Data Documentation

7.15.1.1 CNOT

```
idx qpp::experimental::Bit_circuit::Gate_count::CNOT = 0
```

7.15.1.2 FRED

```
idx qpp::experimental::Bit_circuit::Gate_count::FRED = 0
```

7.15.1.3 NOT

```
idx qpp::experimental::Bit_circuit::Gate_count::NOT = 0
```

7.15.1.4 SWAP

```
idx qpp::experimental::Bit_circuit::Gate_count::SWAP = 0
```

7.15.1.5 TOF

```
idx qpp::experimental::Bit_circuit::Gate_count::TOF = 0
```

7.15.1.6 X

```
idx& qpp::experimental::Bit_circuit::Gate_count::X = NOT
```

The documentation for this struct was generated from the following file:

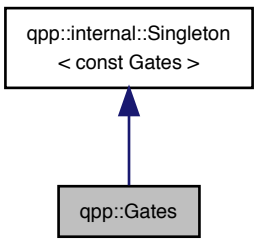
- experimental/experimental.h

7.16 qpp::Gates Class Reference

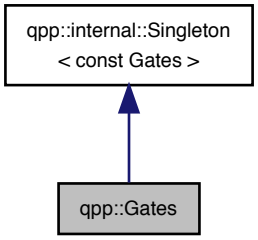
const Singleton class that implements most commonly used gates

```
#include <classes/gates.h>
```

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



Public Member Functions

- cmat Rn (double theta, const std::vector< double > &n) const

  Qubit rotation of theta about the 3-dimensional real (unit) vector n.
- cmat Zd (idx D=2) const

  Generalized Z gate for qudits.
- cmat Fd (idx D=2) const

  Fourier transform gate for qudits.
- cmat Xd (idx D=2) const

  Generalized X gate for qudits.
- template<typename Derived = Eigen::MatrixXcd>
  Derived Id (idx D=2) const

  Identity gate.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx N, idx d=2) const

  Generates the multi-partite multiple-controlled-A gate in matrix form.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::vector< idx > &dims) const

  Expands out.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::initializer_list< idx > &dims) const

  Expands out.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, idx N, idx d=2) const

  Expands out.

Public Attributes

- cmat Id2 {cmat::Identity(2, 2)}

  Identity gate.
- cmat H {cmat::Zero(2, 2)}

Hadamard gate.

- cmat X {cmat::Zero(2, 2)}

  Pauli Sigma-X gate.
- cmat Y {cmat::Zero(2, 2)}

  Pauli Sigma-Y gate.
- cmat Z {cmat::Zero(2, 2)}

  Pauli Sigma-Z gate.
- cmat S {cmat::Zero(2, 2)}

  S gate.
- cmat T {cmat::Zero(2, 2)}

  T gate.
- cmat CNOT {cmat::Identity(4, 4)}

  Controlled-NOT control target gate.
- cmat CZ {cmat::Identity(4, 4)}

  Controlled-Phase gate.
- cmat CNOTba {cmat::Zero(4, 4)}

  Controlled-NOT target control gate.
- cmat SWAP {cmat::Identity(4, 4)}

  SWAP gate.
- cmat TOF {cmat::Identity(8, 8)}

  Toffoli gate.
- cmat FRED {cmat::Identity(8, 8)}

  Fredkin gate.

Private Member Functions

- Gates ()

  Initializes the gates.
- ∼Gates ()=default

  Default destructor.

Friends

- class internal::Singleton< const Gates >

Additional Inherited Members

7.16.1 Detailed Description

const Singleton class that implements most commonly used gates

7.16.2 Constructor & Destructor Documentation

7.16.2.1 Gates()

```
qpp::Gates::Gates ( )  [inline], [private]
```

Initializes the gates.

7.16.2.2 ~Gates()

```
qpp::Gates::~Gates ( )  [private], [default]
```

Default destructor.

7.16.3 Member Function Documentation

7.16.3.1 CTRL()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::CTRL (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & subsys,
            idx N,
            idx d = 2 ) const  [inline]
```

Generates the multi-partite multiple-controlled-*A* gate in matrix form.

See also

qpp::applyCTRL()

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

A	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate *A* is applied
N	Total number of subsystems
d	Subsystem dimensions

Returns

CTRL-A gate, as a matrix over the same scalar field as *A*

7.16.3.2 expandout() [1/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            const std::vector< idx > & dims ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Parameters

A	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.16.3.3 expandout() [2/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            const std::initializer_list< idx > & dims ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Note

The std::initializer_list overload exists because otherwise, in the degenerate case when *dims* has only one element, the one element list is implicitly converted to the element's underlying type, i.e. qpp::idx, which has the net effect of picking the wrong (non-vector) qpp::expandout() overload

Parameters

A	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.16.3.4 expandout() [3/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
             const Eigen::MatrixBase< Derived > & A,
             idx pos,
             idx N,
             idx d = 2 ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Parameters

A	Eigen expression
pos	Position
N	Number of subsystems
d	Subsystem dimension

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.16.3.5 Fd()

```
cmat qpp::Gates::Fd (
             idx D = 2 ) const  [inline]
```

Fourier transform gate for qudits.

Note

Defined as $F = \sum_{j,k=0}^{D-1} \exp(2\pi \mathrm{i} jk/D)|j\rangle\langle k|$

Parameters

D	Dimension of the Hilbert space

Returns

Fourier transform gate for qudits

7.16.3.6 Id()

```
template<typename Derived = Eigen::MatrixXcd>
Derived qpp::Gates::Id (
            idx D = 2 ) const  [inline]
```

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

Parameters

D	Dimension of the Hilbert space

Returns

Identity gate on a Hilbert space of dimension *D*

7.16.3.7 Rn()

```
cmat qpp::Gates::Rn (
            double theta,
            const std::vector< double > & n ) const  [inline]
```

Qubit rotation of *theta* about the 3-dimensional real (unit) vector *n*.

Parameters

theta	Rotation angle
n	3-dimensional real (unit) vector

Returns

Rotation gate

7.16.3.8 Xd()

```
cmat qpp::Gates::Xd (
            idx D = 2 ) const  [inline]
```

Generalized X gate for qudits.

Note

Defined as $X = \sum_{j=0}^{D-1} |j \oplus 1\rangle\langle j|$, i.e. raising operator $X|j\rangle = |j \oplus 1\rangle$

Parameters

D	Dimension of the Hilbert space

Returns

Generalized X gate for qudits

7.16.3.9 Zd()

```
cmat qpp::Gates::Zd (
            idx D = 2 ) const  [inline]
```

Generalized Z gate for qudits.

Note

Defined as $Z = \sum_{j=0}^{D-1} \exp(2\pi \mathrm{i} j/D)|j\rangle\langle j|$

Parameters

D	Dimension of the Hilbert space

Returns

Generalized Z gate for qudits

7.16.4 Friends And Related Function Documentation

7.16.4.1 internal::Singleton< const Gates >

```
friend class internal::Singleton< const Gates >  [friend]
```

7.16.5 Member Data Documentation

7.16.5.1 CNOT

```
cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}
```

Controlled-NOT control target gate.

7.16.5.2 CNOTba

```
cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}
```

Controlled-NOT target control gate.

7.16.5.3 CZ

```
cmat qpp::Gates::CZ {cmat::Identity(4, 4)}
```

Controlled-Phase gate.

7.16.5.4 FRED

```
cmat qpp::Gates::FRED {cmat::Identity(8, 8)}
```

Fredkin gate.

7.16.5.5 H

```
cmat qpp::Gates::H {cmat::Zero(2, 2)}
```

Hadamard gate.

7.16.5.6 Id2

```
cmat qpp::Gates::Id2 {cmat::Identity(2, 2)}
```

Identity gate.

7.16.5.7 S

```
cmat qpp::Gates::S {cmat::Zero(2, 2)}
```

S gate.

7.16.5.8 SWAP

```
cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}
```

SWAP gate.

7.16.5.9 T

```
cmat qpp::Gates::T {cmat::Zero(2, 2)}
```

T gate.

7.16.5.10 TOF

```
cmat qpp::Gates::TOF {cmat::Identity(8, 8)}
```

Toffoli gate.

7.16.5.11 X

```
cmat qpp::Gates::X {cmat::Zero(2, 2)}
```

Pauli Sigma-X gate.

7.16.5.12 Y

```
cmat qpp::Gates::Y {cmat::Zero(2, 2)}
```

Pauli Sigma-Y gate.

7.16.5.13 Z

```
cmat qpp::Gates::Z {cmat::Zero(2, 2)}
```

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

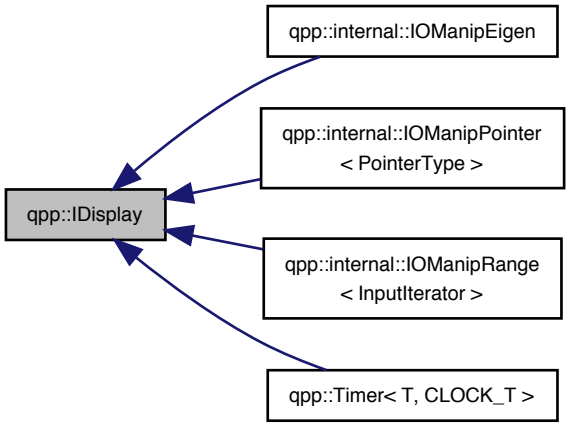
- classes/gates.h

7.17 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

```
#include <classes/idisplay.h>
```

Inheritance diagram for qpp::IDisplay:



Public Member Functions

- IDisplay ()=default

  Default constructor.
- IDisplay (const IDisplay &)=default

  Default copy constructor.
- IDisplay (IDisplay &&)=default

  Default move constructor.
- IDisplay & operator= (const IDisplay &)=default

  Default copy assignment operator.
- IDisplay & operator= (IDisplay &&)=default

  Default move assignment operator.
- virtual ~IDisplay ()=default

  Default virtual destructor.

Private Member Functions

- virtual std::ostream & display (std::ostream &os) const =0

  Must be overridden by all derived classes.

Friends

- std::ostream & operator<< (std::ostream &os, const IDisplay &rhs)

  Overloads the extraction operator.

7.17.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

This class defines friend inline std::ostream& operator<< (std::ostream& os, const qpp::IDisplay& rhs). The latter delegates the work to the pure private virtual function qpp::IDisplay::display() which has to be overridden by all derived classes.

7.17.2 Constructor & Destructor Documentation

7.17.2.1 IDisplay() [1/3]

```
qpp::IDisplay::IDisplay ( )  [default]
```

Default constructor.

7.17.2.2 IDisplay() [2/3]

```
qpp::IDisplay::IDisplay (
            const IDisplay &  )  [default]
```

Default copy constructor.

7.17.2.3 IDisplay() [3/3]

```
qpp::IDisplay::IDisplay (
            IDisplay &&  )  [default]
```

Default move constructor.

7.17.2.4 ~IDisplay()

```
virtual qpp::IDisplay::~IDisplay ( )  [virtual], [default]
```

Default virtual destructor.

7.17.3 Member Function Documentation

7.17.3.1 display()

```
virtual std::ostream& qpp::IDisplay::display (
            std::ostream & os ) const  [private], [pure virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implemented in qpp::internal::IOManipEigen, qpp::Timer< T, CLOCK_T >, qpp::internal::IOManipPointer< PointerType >, and qpp::internal::IOManipRange< InputIterator >.

7.17.3.2 operator=() [1/2]

```
IDisplay& qpp::IDisplay::operator= (
            const IDisplay &  )  [default]
```

Default copy assignment operator.

7.17.3.3 operator=() [2/2]

```
IDisplay& qpp::IDisplay::operator= (
            IDisplay &&  )  [default]
```

Default move assignment operator.

7.17.4 Friends And Related Function Documentation

7.17.4.1 operator<<

```
std::ostream& operator<< (
            std::ostream & os,
            const IDisplay & rhs )  [friend]
```

Overloads the extraction operator.

Delegates the work to the virtual function qpp::IDisplay::display()

The documentation for this class was generated from the following file:

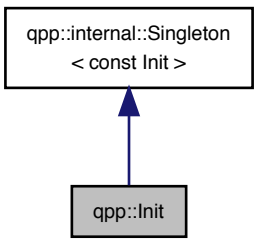
- classes/idisplay.h

7.18 qpp::Init Class Reference

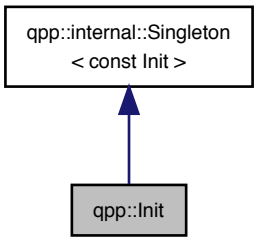
const Singleton class that performs additional initializations/cleanups

```
#include <classes/init.h>
```

Inheritance diagram for qpp::Init:



Collaboration diagram for qpp::Init:



Private Member Functions

- Init ()

  Additional initializations.
- ∼Init ()

  Cleanups.

Friends

- class internal::Singleton< const Init >

Additional Inherited Members

7.18.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

7.18.2 Constructor & Destructor Documentation

7.18.2.1 Init()

```
qpp::Init::Init ( )  [inline], [private]
```

Additional initializations.

7.18.2.2 ~Init()

```
qpp::Init::~Init ( )  [inline], [private]
```

Cleanups.

7.18.3 Friends And Related Function Documentation

7.18.3.1 internal::Singleton< const Init >

```
friend class internal::Singleton< const Init >  [friend]
```

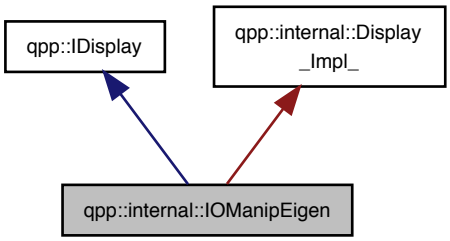
The documentation for this class was generated from the following file:

- classes/init.h

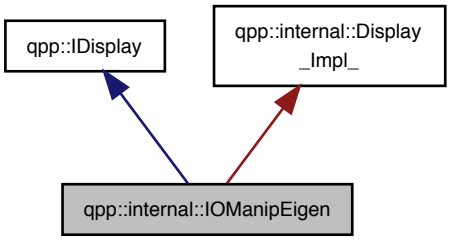
7.19 qpp::internal::IOManipEigen Class Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipEigen:



Collaboration diagram for qpp::internal::IOManipEigen:



Public Member Functions

- template<typename Derived >
  IOManipEigen (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)
- IOManipEigen (const cplx z, double chop=qpp::chop)

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- cmat A_
- double chop_

7.19.1 Constructor & Destructor Documentation

7.19.1.1 IOManipEigen() [1/2]

```
template<typename Derived >
qpp::internal::IOManipEigen::IOManipEigen (
            const Eigen::MatrixBase< Derived > & A,
            double chop = qpp::chop )  [inline], [explicit]
```

7.19.1.2 IOManipEigen() [2/2]

```
qpp::internal::IOManipEigen::IOManipEigen (
            const cplx z,
            double chop = qpp::chop )  [inline], [explicit]
```

7.19.2 Member Function Documentation

7.19.2.1 display()

```
std::ostream& qpp::internal::IOManipEigen::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.19.3 Member Data Documentation

7.19.3.1 A_

```
cmat qpp::internal::IOManipEigen::A_  [private]
```

7.19.3.2 chop_

```
double qpp::internal::IOManipEigen::chop_  [private]
```

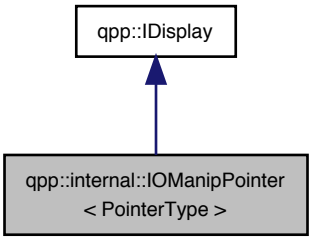
The documentation for this class was generated from the following file:

- internal/classes/iomanip.h

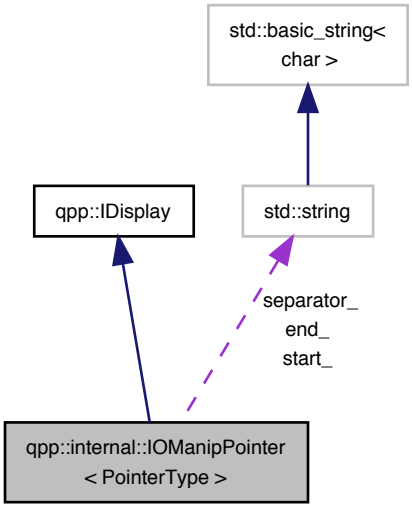
7.20 qpp::internal::IOManipPointer< PointerType > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipPointer< PointerType >:



Collaboration diagram for qpp::internal::IOManipPointer< PointerType >:



Public Member Functions

- IOManipPointer (const PointerType *p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipPointer (const IOManipPointer &)=default
- IOManipPointer & operator= (const IOManipPointer &)=default

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- const PointerType * p_
- idx N_
- std::string separator_
- std::string start_
- std::string end_

7.20.1 Constructor & Destructor Documentation

7.20.1.1 IOManipPointer() [1/2]

```
template<typename PointerType>
qpp::internal::IOManipPointer< PointerType >::IOManipPointer (
            const PointerType * p,
            idx N,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )  [inline], [explicit]
```

7.20.1.2 IOManipPointer() [2/2]

```
template<typename PointerType>
qpp::internal::IOManipPointer< PointerType >::IOManipPointer (
            const IOManipPointer< PointerType > &  )  [default]
```

7.20.2 Member Function Documentation

7.20.2.1 display()

```
template<typename PointerType>
std::ostream& qpp::internal::IOManipPointer< PointerType >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.20.2.2 operator=()

```
template<typename PointerType>
IOManipPointer& qpp::internal::IOManipPointer< PointerType >::operator= (
            const IOManipPointer< PointerType > &  )  [default]
```

7.20.3 Member Data Documentation

7.20.3.1 end_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::end_  [private]
```

7.20.3.2 N_

```
template<typename PointerType>
idx qpp::internal::IOManipPointer< PointerType >::N_  [private]
```

7.20.3.3 p_

```
template<typename PointerType>
const PointerType* qpp::internal::IOManipPointer< PointerType >::p_  [private]
```

7.20.3.4 separator_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::separator_  [private]
```

7.20.3.5 start_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::start_  [private]
```

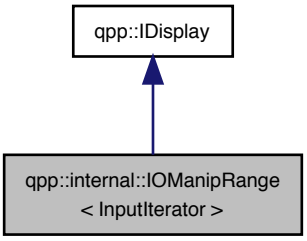
The documentation for this class was generated from the following file:

- internal/classes/iomanip.h

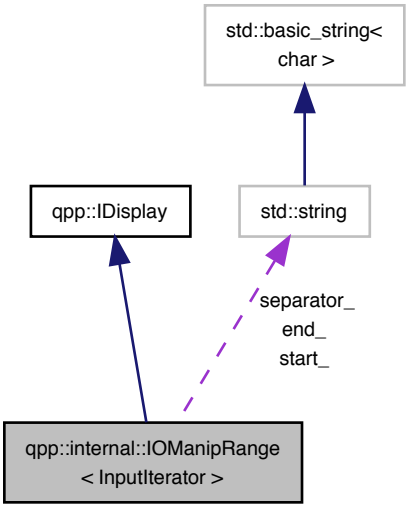
7.21 qpp::internal::IOManipRange< InputIterator > Class Template Reference

`#include <internal/classes/iomanip.h>`

Inheritance diagram for qpp::internal::IOManipRange< InputIterator >:



Collaboration diagram for qpp::internal::IOManipRange< InputIterator >:



Public Member Functions

- IOManipRange (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipRange (const IOManipRange &)=default
- IOManipRange & operator= (const IOManipRange &)=default

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- InputIterator first_
- InputIterator last_
- std::string separator_
- std::string start_
- std::string end_

7.21.1 Constructor & Destructor Documentation

7.21.1.1 IOManipRange() [1/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
            InputIterator first,
            InputIterator last,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )  [inline], [explicit]
```

7.21.1.2 IOManipRange() [2/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
            const IOManipRange< InputIterator > &  )  [default]
```

7.21.2 Member Function Documentation

7.21.2.1 display()

```
template<typename InputIterator>
std::ostream& qpp::internal::IOManipRange< InputIterator >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.21.2.2 operator=()

```
template<typename InputIterator>
IOManipRange& qpp::internal::IOManipRange< InputIterator >::operator= (
            const IOManipRange< InputIterator > &  )  [default]
```

7.21.3 Member Data Documentation

7.21.3.1 end_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::end_  [private]
```

7.21.3.2 first_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::first_  [private]
```

7.21.3.3 last_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::last_  [private]
```

7.21.3.4 separator_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::separator_  [private]
```

7.21.3.5 start_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::start_  [private]
```

The documentation for this class was generated from the following file:

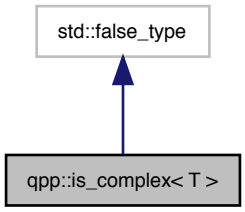
- internal/classes/iomanip.h

7.22 qpp::is_complex< T > Struct Template Reference

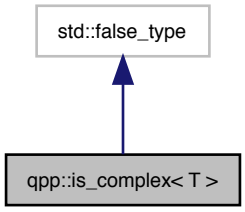
Checks whether the type is a complex type.

`#include <traits.h>`

Inheritance diagram for qpp::is_complex< T >:



Collaboration diagram for qpp::is_complex< T >:



7.22.1 Detailed Description

template<typename T>
struct qpp::is_complex< T >

Checks whether the type is a complex type.

Provides the constant member *value* which is equal to *true*, if the type is a complex type, i.e. *std::complex<T>*

The documentation for this struct was generated from the following file:

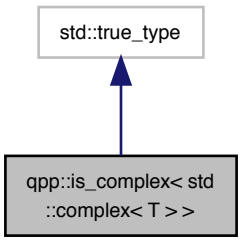
- traits.h

7.23 qpp::is_complex< std::complex< T > > Struct Template Reference

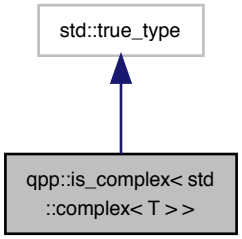
Checks whether the type is a complex number type, specialization for complex types.

`#include <traits.h>`

Inheritance diagram for qpp::is_complex< std::complex< T > >:



Collaboration diagram for qpp::is_complex< std::complex< T > >:



7.23.1 Detailed Description

template<typename T>
struct qpp::is_complex< std::complex< T > >

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

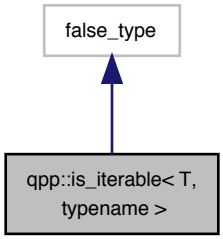
- traits.h

7.24 qpp::is_iterable< T, typename > Struct Template Reference

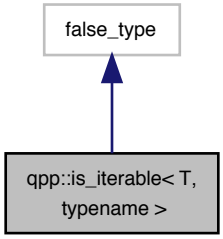
Checks whether *T* is compatible with an STL-like iterable container.

`#include <traits.h>`

Inheritance diagram for qpp::is_iterable< T, typename >:



Collaboration diagram for qpp::is_iterable< T, typename >:



7.24.1 Detailed Description

template<typename T, typename = void>
struct qpp::is_iterable< T, typename >

Checks whether *T* is compatible with an STL-like iterable container.

Provides the constant member *value* which is equal to *true*, if *T* is compatible with an iterable container, i.e. provides at least *begin()* and *end()* member functions. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

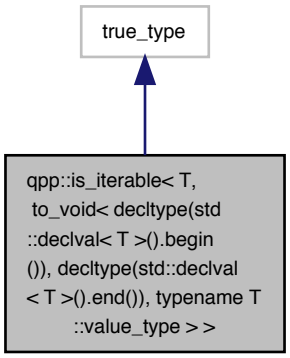
- traits.h

7.25 qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > > Struct Template Reference

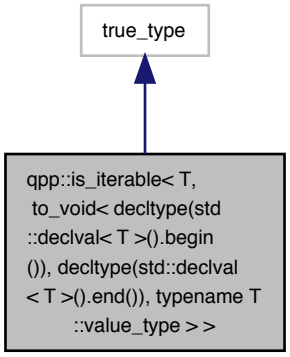
Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >:



Collaboration diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >:



7.25.1 Detailed Description

template<typename T>
struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T↩ ::value_type > >

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

The documentation for this struct was generated from the following file:

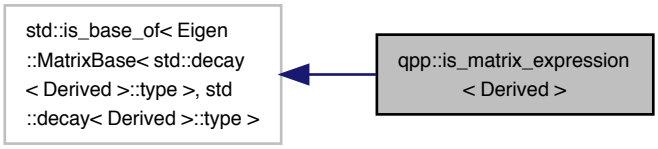
- traits.h

7.26 qpp::is_matrix_expression< Derived > Struct Template Reference

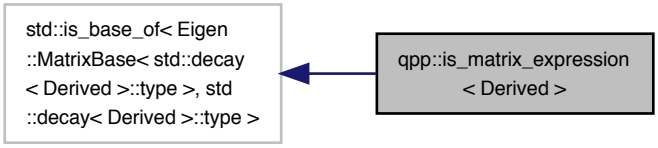
Checks whether the type is an Eigen matrix expression.

`#include <traits.h>`

Inheritance diagram for qpp::is_matrix_expression< Derived >:



Collaboration diagram for qpp::is_matrix_expression< Derived >:



7.26.1 Detailed Description

template<typename Derived>
struct qpp::is_matrix_expression< Derived >

Checks whether the type is an Eigen matrix expression.

Provides the constant member *value* which is equal to *true*, if the type is an Eigen matrix expression of type *Eigen::MatrixBase<Derived>*. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

- traits.h

7.27 qpp::make_void< Ts > Struct Template Reference

Helper for qpp::to_void<> alias template.

```
#include <traits.h>
```

Public Types

- typedef void type

7.27.1 Detailed Description

template<typename... Ts>
struct qpp::make_void< Ts >

Helper for qpp::to_void<> alias template.

See also

qpp::to_void<>

7.27.2 Member Typedef Documentation

7.27.2.1 type

```
template<typename...  Ts>
typedef void qpp::make_void< Ts >::type
```

The documentation for this struct was generated from the following file:

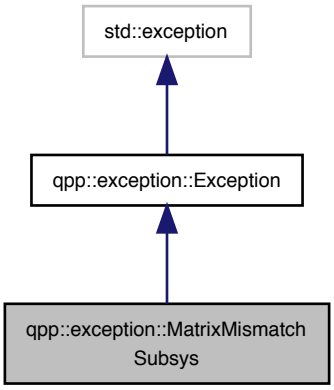
- traits.h

7.28 qpp::exception::MatrixMismatchSubsys Class Reference

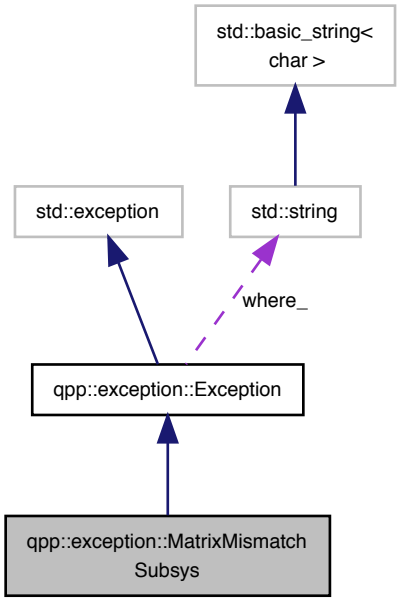
Matrix mismatch subsystems exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::MatrixMismatchSubsys:



Collaboration diagram for qpp::exception::MatrixMismatchSubsys:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.28.1 Detailed Description

Matrix mismatch subsystems exception.

Matrix size mismatch subsystem sizes (e.g. in qpp::apply())

7.28.2 Member Function Documentation

7.28.2.1 type_description()

```
std::string qpp::exception::MatrixMismatchSubsys::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

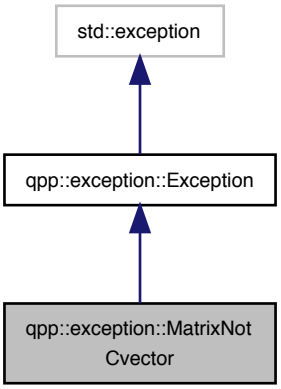
- classes/exception.h

7.29 qpp::exception::MatrixNotCvector Class Reference

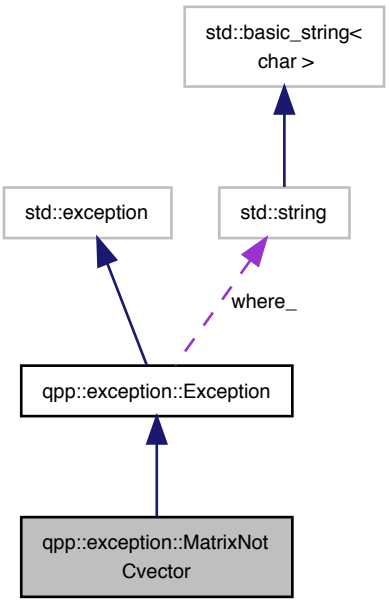
Matrix is not a column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotCvector:



Collaboration diagram for qpp::exception::MatrixNotCvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.29.1 Detailed Description

Matrix is not a column vector exception.

Eigen::Matrix is not a column vector

7.29.2 Member Function Documentation

7.29.2.1 type_description()

```
std::string qpp::exception::MatrixNotCvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

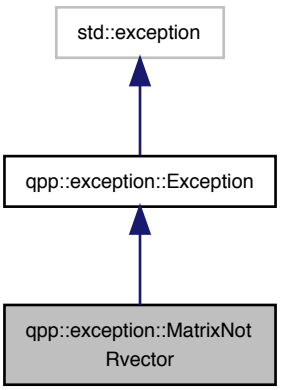
- classes/exception.h

7.30 qpp::exception::MatrixNotRvector Class Reference

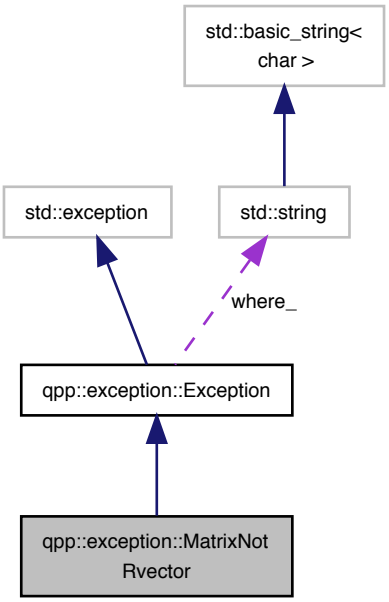
Matrix is not a row vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotRvector:



Collaboration diagram for qpp::exception::MatrixNotRvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.30.1 Detailed Description

Matrix is not a row vector exception.

Eigen::Matrix is not a row vector

7.30.2 Member Function Documentation

7.30.2.1 type_description()

```
std::string qpp::exception::MatrixNotRvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

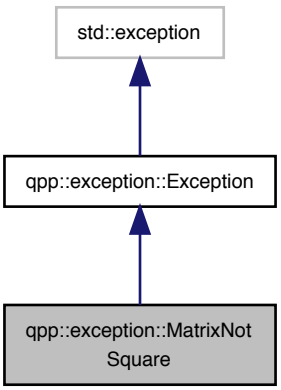
- classes/exception.h

7.31 qpp::exception::MatrixNotSquare Class Reference

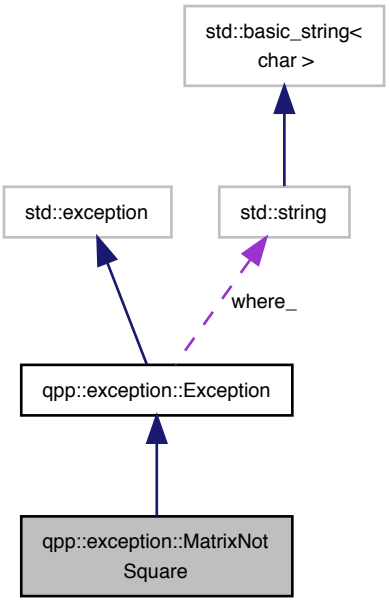
Matrix is not square exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquare:



Collaboration diagram for qpp::exception::MatrixNotSquare:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.31.1 Detailed Description

Matrix is not square exception.

Eigen::Matrix is not a square matrix

7.31.2 Member Function Documentation

7.31.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquare::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

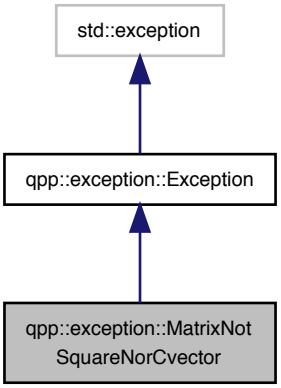
- classes/exception.h

7.32 qpp::exception::MatrixNotSquareNorCvector Class Reference

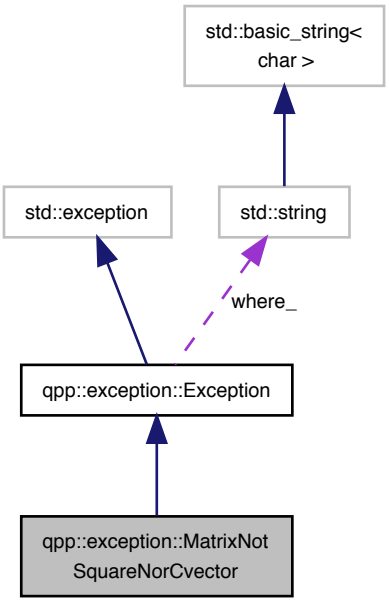
Matrix is not square nor column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorCvector:



Collaboration diagram for qpp::exception::MatrixNotSquareNorCvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.32.1 Detailed Description

Matrix is not square nor column vector exception.

Eigen::Matrix is not a square matrix nor a column vector

7.32.2 Member Function Documentation

7.32.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquareNorCvector::type_description ( ) const  [inline],
[override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

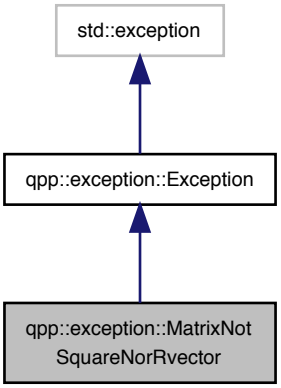
- classes/exception.h

7.33 qpp::exception::MatrixNotSquareNorRvector Class Reference

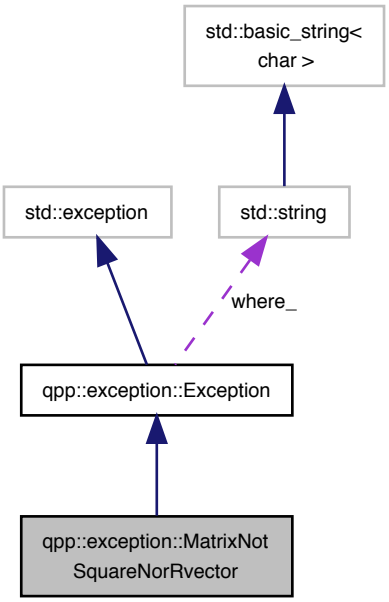
Matrix is not square nor row vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorRvector:



Collaboration diagram for qpp::exception::MatrixNotSquareNorRvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.33.1 Detailed Description

Matrix is not square nor row vector exception.

Eigen::Matrix is not a square matrix nor a row vector

7.33.2 Member Function Documentation

7.33.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquareNorRvector::type_description ( ) const  [inline],
[override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

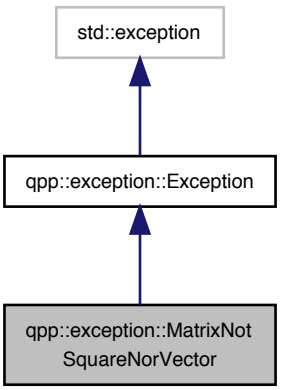
- classes/exception.h

7.34 qpp::exception::MatrixNotSquareNorVector Class Reference

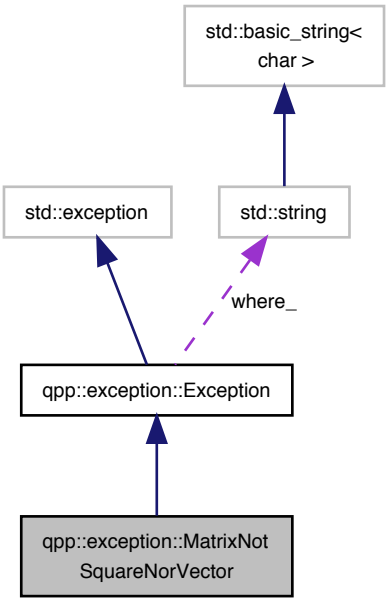
Matrix is not square nor vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorVector:



Collaboration diagram for qpp::exception::MatrixNotSquareNorVector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.34.1 Detailed Description

Matrix is not square nor vector exception.

Eigen::Matrix is not a square matrix nor a row/column vector

7.34.2 Member Function Documentation

7.34.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquareNorVector::type_description ( ) const  [inline],
[override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

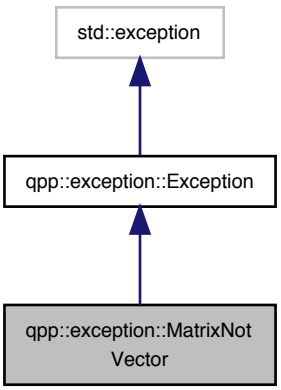
- classes/exception.h

7.35 qpp::exception::MatrixNotVector Class Reference

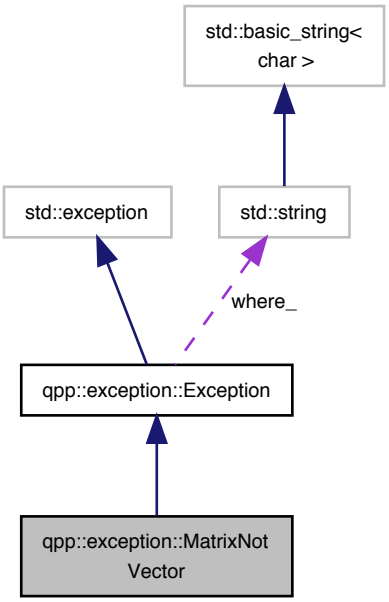
Matrix is not a vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotVector:



Collaboration diagram for qpp::exception::MatrixNotVector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.35.1 Detailed Description

Matrix is not a vector exception.

Eigen::Matrix is not a row or column vector

7.35.2 Member Function Documentation

7.35.2.1 type_description()

```
std::string qpp::exception::MatrixNotVector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

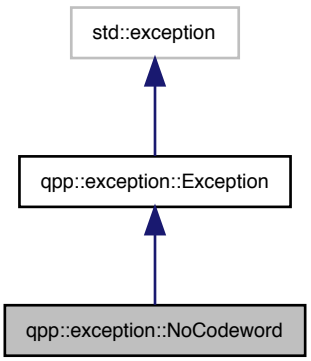
- classes/exception.h

7.36 qpp::exception::NoCodeword Class Reference

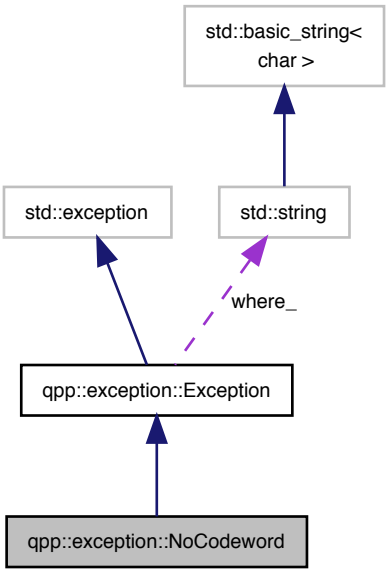
Codeword does not exist exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NoCodeword:



Collaboration diagram for qpp::exception::NoCodeword:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.36.1 Detailed Description

Codeword does not exist exception.

Codeword does not exist, thrown when calling qpp::Codes::codeword() with an invalid index

7.36.2 Member Function Documentation

7.36.2.1 type_description()

```
std::string qpp::exception::NoCodeword::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

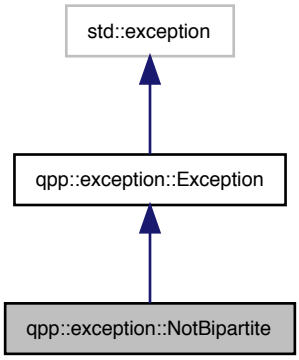
- classes/exception.h

7.37 qpp::exception::NotBipartite Class Reference

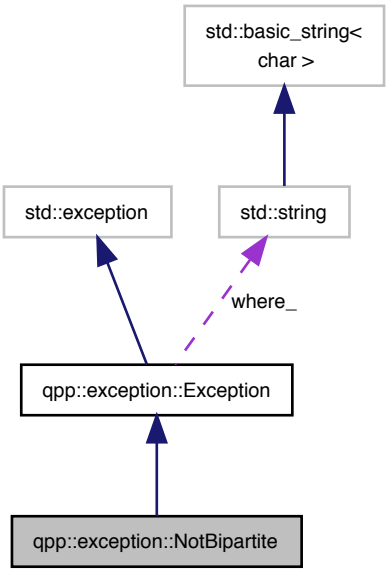
Not bi-partite exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::NotBipartite:



Collaboration diagram for qpp::exception::NotBipartite:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.37.1 Detailed Description

Not bi-partite exception.

std::vector<idx> of dimensions has size different from 2

7.37.2 Member Function Documentation

7.37.2.1 type_description()

```
std::string qpp::exception::NotBipartite::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

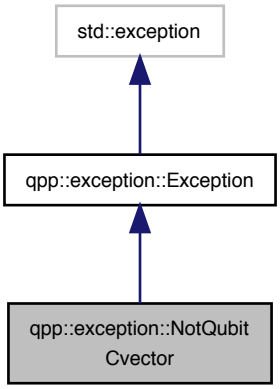
- classes/exception.h

7.38 qpp::exception::NotQubitCvector Class Reference

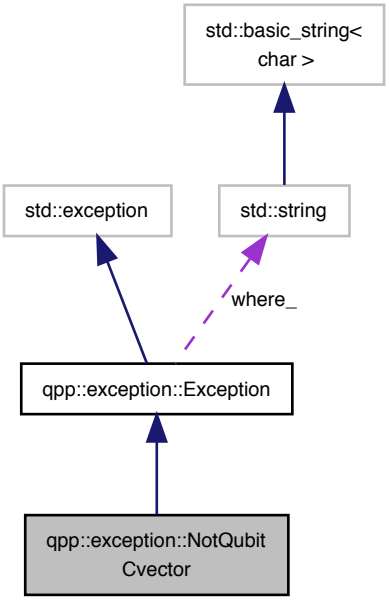
Column vector is not 2 x 1 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitCvector:



Collaboration diagram for qpp::exception::NotQubitCvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.38.1 Detailed Description

Column vector is not 2 x 1 exception.

Eigen::Matrix is not 2 x 1

7.38.2 Member Function Documentation

7.38.2.1 type_description()

```
std::string qpp::exception::NotQubitCvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

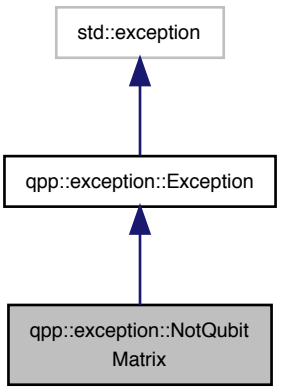
- classes/exception.h

7.39 qpp::exception::NotQubitMatrix Class Reference

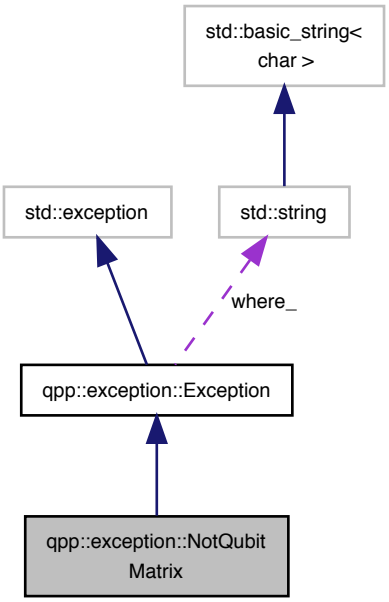
Matrix is not 2 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitMatrix:



Collaboration diagram for qpp::exception::NotQubitMatrix:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.39.1 Detailed Description

Matrix is not 2 x 2 exception.

Eigen::Matrix is not 2 x 2

7.39.2 Member Function Documentation

7.39.2.1 type_description()

```
std::string qpp::exception::NotQubitMatrix::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

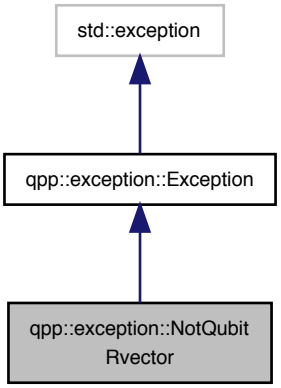
- classes/exception.h

7.40 qpp::exception::NotQubitRvector Class Reference

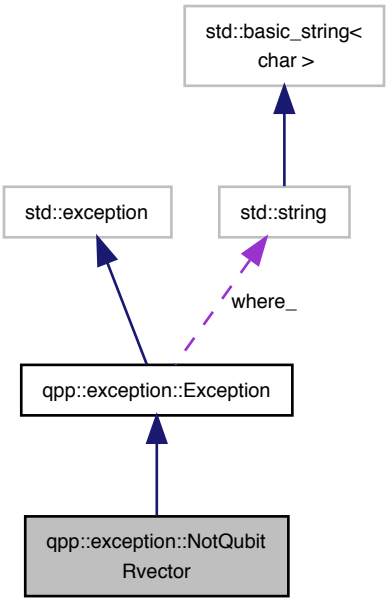
Row vector is not 1 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitRvector:



Collaboration diagram for qpp::exception::NotQubitRvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.40.1 Detailed Description

Row vector is not 1 x 2 exception.

Eigen::Matrix is not 1 x 2

7.40.2 Member Function Documentation

7.40.2.1 type_description()

```
std::string qpp::exception::NotQubitRvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

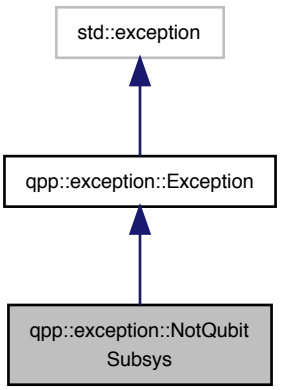
- classes/exception.h

7.41 qpp::exception::NotQubitSubsys Class Reference

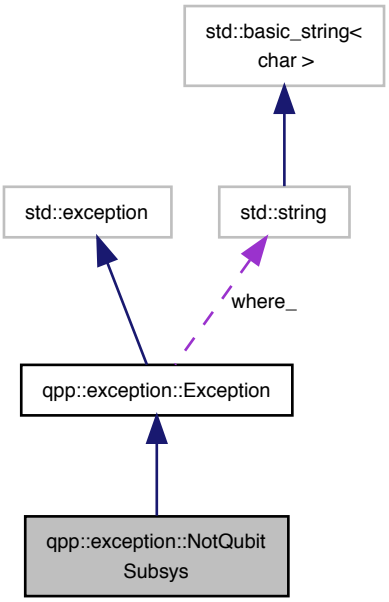
Subsystems are not qubits exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitSubsys:



Collaboration diagram for qpp::exception::NotQubitSubsys:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.41.1 Detailed Description

Subsystems are not qubits exception.

Subsystems are not 2-dimensional (qubits)

7.41.2 Member Function Documentation

7.41.2.1 type_description()

```
std::string qpp::exception::NotQubitSubsys::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

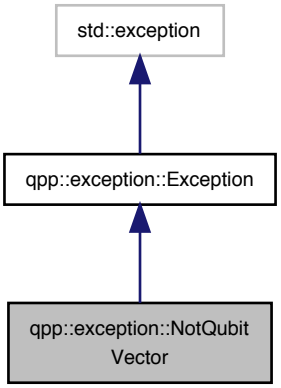
- classes/exception.h

7.42 qpp::exception::NotQubitVector Class Reference

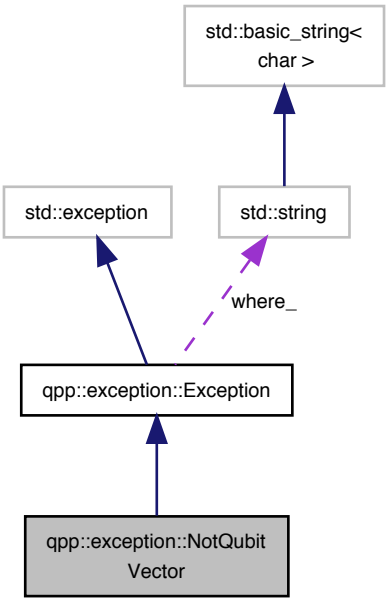
Vector is not 2 x 1 nor 1 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitVector:



Collaboration diagram for qpp::exception::NotQubitVector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.42.1 Detailed Description

Vector is not 2 x 1 nor 1 x 2 exception.

Eigen::Matrix is not 2 x 1 nor 1 x 2

7.42.2 Member Function Documentation

7.42.2.1 type_description()

```
std::string qpp::exception::NotQubitVector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

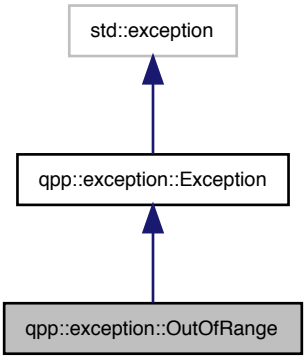
- classes/exception.h

7.43 qpp::exception::OutOfRange Class Reference

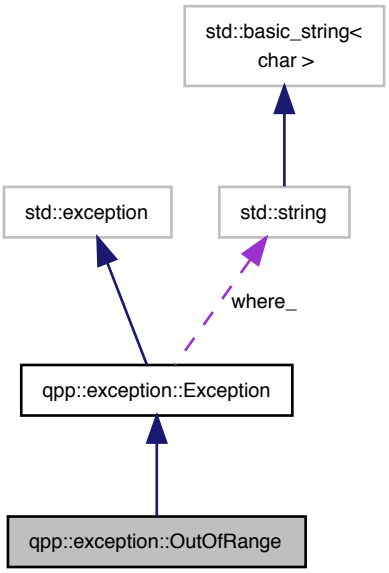
Parameter out of range exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::OutOfRange:



Collaboration diagram for qpp::exception::OutOfRange:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.43.1 Detailed Description

Parameter out of range exception.

Parameter out of range

7.43.2 Member Function Documentation

7.43.2.1 type_description()

```
std::string qpp::exception::OutOfRange::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

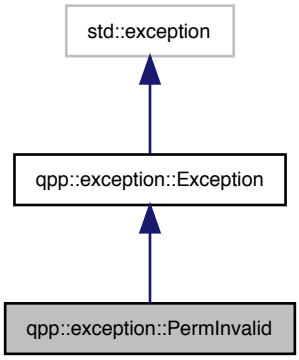
- classes/exception.h

7.44 qpp::exception::PermInvalid Class Reference

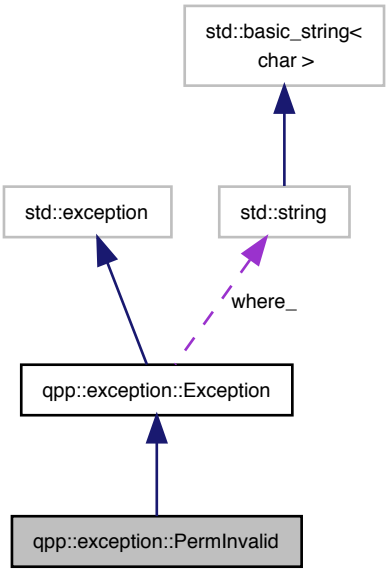
Invalid permutation exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::PermInvalid:



Collaboration diagram for qpp::exception::PermInvalid:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.44.1 Detailed Description

Invalid permutation exception.

std::vector<idx> does note represent a valid permutation

7.44.2 Member Function Documentation

7.44.2.1 type_description()

```
std::string qpp::exception::PermInvalid::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

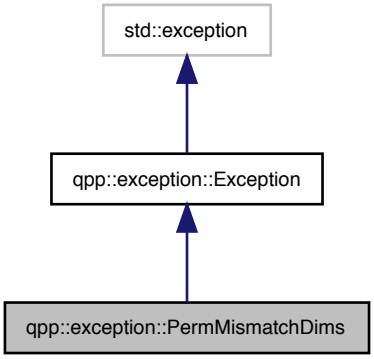
- classes/exception.h

7.45 qpp::exception::PermMismatchDims Class Reference

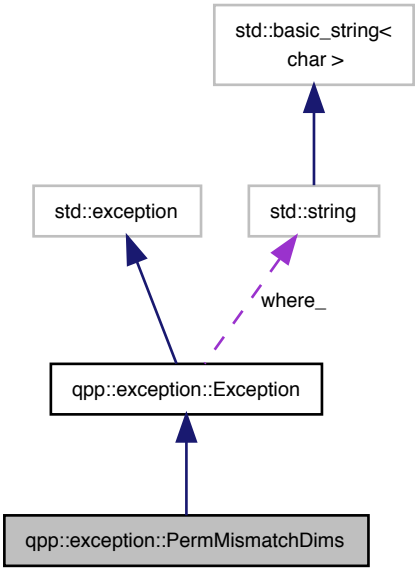
Permutation mismatch dimensions exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::PermMismatchDims:



Collaboration diagram for qpp::exception::PermMismatchDims:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.45.1 Detailed Description

Permutation mismatch dimensions exception.

Size of the std::vector<idx> representing the permutation is different from the size of the std::vector<idx> of dimensions

7.45.2 Member Function Documentation

7.45.2.1 type_description()

```
std::string qpp::exception::PermMismatchDims::type_description ( ) const  [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

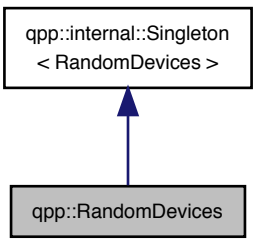
- classes/exception.h

7.46 qpp::RandomDevices Class Reference

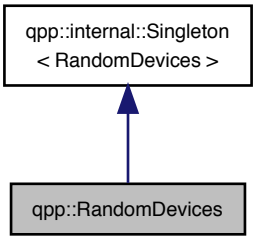
Singleton class that manages the source of randomness in the library.

```
#include <classes/random_devices.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



Public Member Functions

- std::mt19937 & get_prng ()

  Returns a reference to the internal PRNG object.
- std::istream & load (std::istream &is)

  Loads the state of the PRNG from an input stream.
- std::ostream & save (std::ostream &os) const

  Saves the state of the PRNG to an output stream.

Private Member Functions

- RandomDevices ()

  Initializes and seeds the random number generators.
- ~RandomDevices ()=default

  Default destructor.

Private Attributes

- std::random_device rd_

  *used to seed std::mt19937 prng_*
- std::mt19937 prng_

  Mersenne twister random number generator.

Friends

- class internal::Singleton< RandomDevices >

Additional Inherited Members

7.46.1 Detailed Description

Singleton class that manages the source of randomness in the library.

Consists of a wrapper around an std::mt19937 Mersenne twister random number generator engine and an std::random_device engine. The latter is used to seed the Mersenne twister.

Warning

This class DOES NOT seed the standard C number generator used by Eigen::Matrix::Random(), since it is not thread safe. Do not use Eigen::Matrix::Random() or functions that depend on the C style random number engine, but use qpp::rand() instead!

7.46.2 Constructor & Destructor Documentation

7.46.2.1 RandomDevices()

```
qpp::RandomDevices::RandomDevices ( )  [inline], [private]
```

Initializes and seeds the random number generators.

7.46.2.2 ~RandomDevices()

```
qpp::RandomDevices::~RandomDevices ( )  [private], [default]
```

Default destructor.

7.46.3 Member Function Documentation

7.46.3.1 get_prng()

```
std::mt19937& qpp::RandomDevices::get_prng ( )  [inline]
```

Returns a reference to the internal PRNG object.

Returns

Reference to the internal PRNG object

7.46.3.2 load()

```
std::istream& qpp::RandomDevices::load (
            std::istream & is )  [inline]
```

Loads the state of the PRNG from an input stream.

Parameters

is	Input stream

Returns

The input stream

7.46.3.3 save()

```
std::ostream& qpp::RandomDevices::save (
            std::ostream & os ) const  [inline]
```

Saves the state of the PRNG to an output stream.

Parameters

os	Output stream

Returns

The output stream

7.46.4 Friends And Related Function Documentation

7.46.4.1 internal::Singleton< RandomDevices >

```
friend class internal::Singleton< RandomDevices >  [friend]
```

7.46.5 Member Data Documentation

7.46.5.1 prng_

```
std::mt19937 qpp::RandomDevices::prng_  [private]
```

Mersenne twister random number generator.

7.46.5.2 rd_

```
std::random_device qpp::RandomDevices::rd_  [private]
```

used to seed std::mt19937 prng_

The documentation for this class was generated from the following file:

- classes/random_devices.h

7.47 qpp::internal::Singleton< T > Class Template Reference

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

Static Public Member Functions

- static T & get_instance () noexcept(std::is_nothrow_constructible< T >::value)
- static T & get_thread_local_instance () noexcept(std::is_nothrow_constructible< T >::value)

Protected Member Functions

- Singleton () noexcept=default
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete
- virtual ~Singleton ()=default

7.47.1 Detailed Description

template<typename T>
class qpp::internal::Singleton< T >

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from qpp::internal::Singleton, make qpp::internal::Singleton a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function qpp::internal::Singleton::get_instance() (qpp::internal::Singleton::get_thread_local_↩ instance()), which returns a reference (thread_local reference) to your newly created singleton (thread-safe in C++11).

Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>
{
       friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
    ~MySingleton()
    {
        // Implement the destructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
thread_local MySingleton& tls = MySingleton::get_thread_local_instance();
// Get a thread_local instance
```

See also

Code of qpp::Codes, qpp::Gates, qpp::Init, qpp::RandomDevices, qpp::States or qpp.h for real world examples of usage.

7.47.2 Constructor & Destructor Documentation

7.47.2.1 Singleton() [1/2]

```
template<typename T>
qpp::internal::Singleton< T >::Singleton ( )  [protected], [default], [noexcept]
```

7.47.2.2 Singleton() [2/2]

```
template<typename T>
qpp::internal::Singleton< T >::Singleton (
            const Singleton< T > &  )  [protected], [delete]
```

7.47.2.3 ~Singleton()

```
template<typename T>
virtual qpp::internal::Singleton< T >::~Singleton ( )  [protected], [virtual], [default]
```

7.47.3 Member Function Documentation

7.47.3.1 get_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_instance ( )  [inline], [static], [noexcept]
```

7.47.3.2 get_thread_local_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_thread_local_instance ( )  [inline], [static],
[noexcept]
```

7.47.3.3 operator=()

```
template<typename T>
Singleton& qpp::internal::Singleton< T >::operator= (
            const Singleton< T > &  )  [protected], [delete]
```

The documentation for this class was generated from the following file:

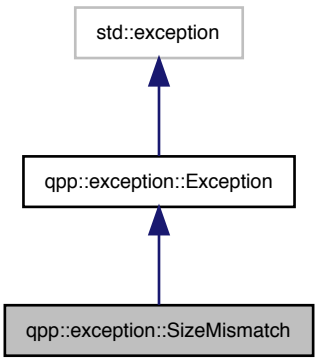
- internal/classes/singleton.h

7.48 qpp::exception::SizeMismatch Class Reference

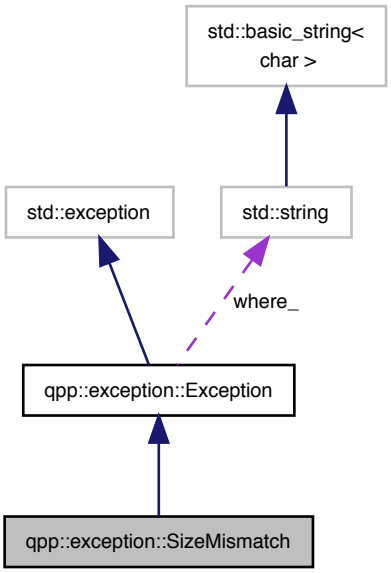
Size mismatch exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::SizeMismatch:



Collaboration diagram for qpp::exception::SizeMismatch:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.48.1 Detailed Description

Size mismatch exception.

Sizes do not match

7.48.2 Member Function Documentation

7.48.2.1 type_description()

```
std::string qpp::exception::SizeMismatch::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

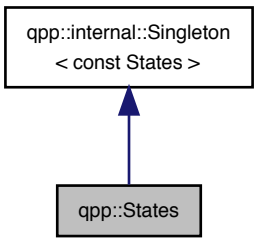
- classes/exception.h

7.49 qpp::States Class Reference

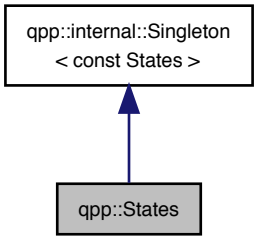
const Singleton class that implements most commonly used states

`#include <classes/states.h>`

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



Public Member Functions

- ket mes (idx d=2) const
  Maximally entangled state of 2 qudits.
- ket zero (idx n, idx d=2) const
  Zero state of n qudits.
- ket one (idx n, idx d=2) const
  One state of n qudits.
- ket jn (idx j, idx n, idx d=2) const
  $|j\rangle^{\otimes n}$ *state of n qudits*
- ket plus (idx n) const
  Plus state of n qubits.
- ket minus (idx n) const
  Minus state of n qubits.

Public Attributes

- ket x0 {ket::Zero(2)}

  Pauli Sigma-X 0-eigenstate |+>
- ket x1 {ket::Zero(2)}

  Pauli Sigma-X 1-eigenstate |->
- ket y0 {ket::Zero(2)}

  Pauli Sigma-Y 0-eigenstate |y+>
- ket y1 {ket::Zero(2)}

  Pauli Sigma-Y 1-eigenstate |y->
- ket z0 {ket::Zero(2)}

  Pauli Sigma-Z 0-eigenstate |0>
- ket z1 {ket::Zero(2)}

  Pauli Sigma-Z 1-eigenstate |1>
- cmat px0 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.
- cmat px1 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.
- cmat py0 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Y 0-eigenstate |y+><y+|.
- cmat py1 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Y 1-eigenstate |y-><y-|.
- cmat pz0 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.
- cmat pz1 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.
- ket b00 {ket::Zero(4)}

  Bell-00 state (following the convention in Nielsen and Chuang)
- ket b01 {ket::Zero(4)}

  Bell-01 state (following the convention in Nielsen and Chuang)
- ket b10 {ket::Zero(4)}

  Bell-10 state (following the convention in Nielsen and Chuang)
- ket b11 {ket::Zero(4)}

  Bell-11 state (following the convention in Nielsen and Chuang)
- cmat pb00 {cmat::Zero(4, 4)}

  Projector onto the Bell-00 state.
- cmat pb01 {cmat::Zero(4, 4)}

  Projector onto the Bell-01 state.
- cmat pb10 {cmat::Zero(4, 4)}

  Projector onto the Bell-10 state.
- cmat pb11 {cmat::Zero(4, 4)}

  Projector onto the Bell-11 state.
- ket GHZ {ket::Zero(8)}

  GHZ state.
- ket W {ket::Zero(8)}

  W state.
- cmat pGHZ {cmat::Zero(8, 8)}

  Projector onto the GHZ state.
- cmat pW {cmat::Zero(8, 8)}

  Projector onto the W state.

Private Member Functions

- States ()
- ~States ()=default

  Default destructor.

Friends

- class internal::Singleton< const States >

Additional Inherited Members

7.49.1 Detailed Description

const Singleton class that implements most commonly used states

7.49.2 Constructor & Destructor Documentation

7.49.2.1 States()

```
qpp::States::States ( )  [inline], [private]
```

Initialize the states

7.49.2.2 ~States()

```
qpp::States::~States ( )  [private], [default]
```

Default destructor.

7.49.3 Member Function Documentation

7.49.3.1 jn()

```
ket qpp::States::jn (
            idx j,
            idx n,
            idx d = 2 ) const  [inline]
```

$|j\rangle^{\otimes n}$ state of *n* qudits

Parameters

j	Non-negative integer
n	Non-negative integer
d	Subsystem dimensions

Returns

$|j\rangle^{\otimes n}$ state of *n* qudits

7.49.3.2 mes()

```
ket qpp::States::mes (
            idx d = 2 ) const  [inline]
```

Maximally entangled state of 2 qudits.

Parameters

d	Subsystem dimensions

Returns

Maximally entangled state $\frac{1}{\sqrt{d}} \sum_{j=0}^{d-1} |jj\rangle$ of 2 qudits

7.49.3.3 minus()

```
ket qpp::States::minus (
            idx n ) const  [inline]
```

Minus state of *n* qubits.

Parameters

n	Non-negative integer

Returns

Minus state $|-\rangle^{\otimes n}$ of *n* qubits

7.49.3.4 one()

```
ket qpp::States::one (
            idx n,
            idx d = 2 ) const  [inline]
```

One state of *n* qudits.

Parameters

n	Non-negative integer
d	Subsystem dimensions

Returns

One state $|1\rangle^{\otimes n}$ of *n* qudits

7.49.3.5 plus()

```
ket qpp::States::plus (
            idx n ) const  [inline]
```

Plus state of *n* qubits.

Parameters

n	Non-negative integer

Returns

Plus state $|+\rangle^{\otimes n}$ of *n* qubits

7.49.3.6 zero()

```
ket qpp::States::zero (
            idx n,
            idx d = 2 ) const  [inline]
```

Zero state of *n* qudits.

Parameters

n	Non-negative integer
d	Subsystem dimensions

Returns

Zero state $|0\rangle^{\otimes n}$ of *n* qudits

7.49.4 Friends And Related Function Documentation

7.49.4.1 internal::Singleton< const States >

```
friend class internal::Singleton< const States >  [friend]
```

7.49.5 Member Data Documentation

7.49.5.1 b00

```
ket qpp::States::b00 {ket::Zero(4)}
```

Bell-00 state (following the convention in Nielsen and Chuang)

7.49.5.2 b01

```
ket qpp::States::b01 {ket::Zero(4)}
```

Bell-01 state (following the convention in Nielsen and Chuang)

7.49.5.3 b10

```
ket qpp::States::b10 {ket::Zero(4)}
```

Bell-10 state (following the convention in Nielsen and Chuang)

7.49.5.4 b11

```
ket qpp::States::b11 {ket::Zero(4)}
```

Bell-11 state (following the convention in Nielsen and Chuang)

7.49.5.5 GHZ

```
ket qpp::States::GHZ {ket::Zero(8)}
```

GHZ state.

7.49.5.6 pb00

```
cmat qpp::States::pb00 {cmat::Zero(4, 4)}
```

Projector onto the Bell-00 state.

7.49.5.7 pb01

```
cmat qpp::States::pb01 {cmat::Zero(4, 4)}
```

Projector onto the Bell-01 state.

7.49.5.8 pb10

```
cmat qpp::States::pb10 {cmat::Zero(4, 4)}
```

Projector onto the Bell-10 state.

7.49.5.9 pb11

```
cmat qpp::States::pb11 {cmat::Zero(4, 4)}
```

Projector onto the Bell-11 state.

7.49.5.10 pGHZ

```
cmat qpp::States::pGHZ {cmat::Zero(8, 8)}
```

Projector onto the GHZ state.

7.49.5.11 pW

```
cmat qpp::States::pW {cmat::Zero(8, 8)}
```

Projector onto the W state.

7.49.5.12 px0

```
cmat qpp::States::px0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 0-eigenstate $|+\rangle\langle+|$.

7.49.5.13 px1

```
cmat qpp::States::px1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 1-eigenstate $|-\rangle\langle-|$.

7.49.5.14 py0

```
cmat qpp::States::py0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 0-eigenstate $|y+\rangle\langle y+|$.

7.49.5.15 py1

```
cmat qpp::States::py1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 1-eigenstate $|y-\rangle\langle y-|$.

7.49.5.16 pz0

```
cmat qpp::States::pz0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 0-eigenstate $|0\rangle\langle0|$.

7.49.5.17 pz1

```
cmat qpp::States::pz1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 1-eigenstate $|1><1|$.

7.49.5.18 W

```
ket qpp::States::W {ket::Zero(8)}
```

W state.

7.49.5.19 x0

```
ket qpp::States::x0 {ket::Zero(2)}
```

Pauli Sigma-X 0-eigenstate $|+>$

7.49.5.20 x1

```
ket qpp::States::x1 {ket::Zero(2)}
```

Pauli Sigma-X 1-eigenstate $|->$

7.49.5.21 y0

```
ket qpp::States::y0 {ket::Zero(2)}
```

Pauli Sigma-Y 0-eigenstate $|y+>$

7.49.5.22 y1

```
ket qpp::States::y1 {ket::Zero(2)}
```

Pauli Sigma-Y 1-eigenstate $|y->$

7.49.5.23 z0

```
ket qpp::States::z0 {ket::Zero(2)}
```

Pauli Sigma-Z 0-eigenstate $|0\rangle$

7.49.5.24 z1

```
ket qpp::States::z1 {ket::Zero(2)}
```

Pauli Sigma-Z 1-eigenstate $|1\rangle$

The documentation for this class was generated from the following file:

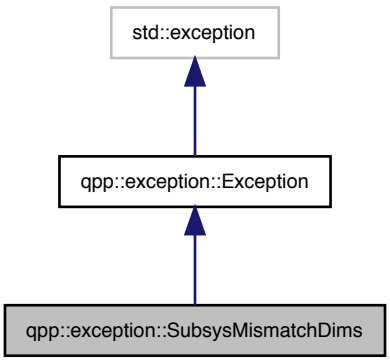
- classes/states.h

7.50 qpp::exception::SubsysMismatchDims Class Reference

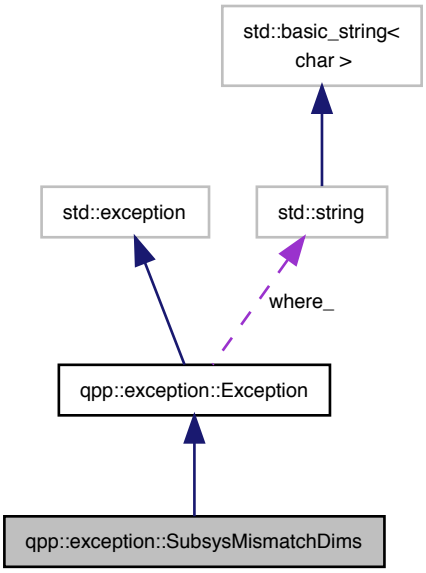
Subsystems mismatch dimensions exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::SubsysMismatchDims:



Collaboration diagram for qpp::exception::SubsysMismatchDims:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.50.1 Detailed Description

Subsystems mismatch dimensions exception.

std::vector<idx> of subsystem labels has duplicates, or has entries that are larger than the size of the std::vector<idx> of dimensions

7.50.2 Member Function Documentation

7.50.2.1 type_description()

```
std::string qpp::exception::SubsysMismatchDims::type_description ( ) const  [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

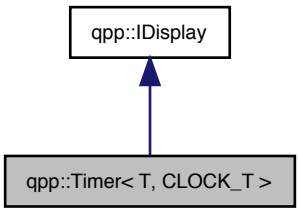
- classes/exception.h

7.51 qpp::Timer< T, CLOCK_T > Class Template Reference

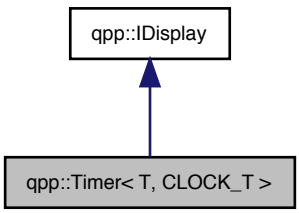
Chronometer.

`#include <classes/timer.h>`

Inheritance diagram for qpp::Timer< T, CLOCK_T >:



Collaboration diagram for qpp::Timer< T, CLOCK_T >:



Public Member Functions

- Timer () noexcept

  Constructs an instance with the current time as the starting point.
- void tic () noexcept

  Resets the chronometer.
- const Timer & toc () noexcept

  Stops the chronometer.
- double tics () const noexcept

  Time passed in the duration specified by T.
- template<typename U = T>
  U get_duration () const noexcept

  Duration specified by U.
- Timer (const Timer &)=default

  Default copy constructor.
- Timer (Timer &&)=default

  Default move constructor.
- Timer & operator= (const Timer &)=default

  Default copy assignment operator.
- Timer & operator= (Timer &&)=default

  Default move assignment operator.
- virtual ~Timer ()=default

  Default virtual destructor.

Protected Attributes

- CLOCK_T::time_point start_
- CLOCK_T::time_point end_

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  qpp::IDisplay::display() override

7.51.1 Detailed Description

template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
class qpp::Timer< T, CLOCK_T >

Chronometer.

Template Parameters

T	Tics duration, default is std::chrono::duration<double, 1>, i.e. seconds in double precision
CLOCK_T	Clock's type, default is std::chrono::steady_clock, not affected by wall clock changes during runtime

7.51.2 Constructor & Destructor Documentation

7.51.2.1 Timer() [1/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer ( )  [inline], [noexcept]
```

Constructs an instance with the current time as the starting point.

7.51.2.2 Timer() [2/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer (
            const Timer< T, CLOCK_T > &  )  [default]
```

Default copy constructor.

7.51.2.3 Timer() [3/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer (
            Timer< T, CLOCK_T > &&  )  [default]
```

Default move constructor.

7.51.2.4 ~Timer()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
virtual qpp::Timer< T, CLOCK_T >::~Timer ( )  [virtual], [default]
```

Default virtual destructor.

7.51.3 Member Function Documentation

7.51.3.1 display()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
std::ostream& qpp::Timer< T, CLOCK_T >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override

Parameters

os	Output stream

Returns

Writes to the output stream the number of tics (specified by T) that passed between the instantiation/reset and invocation of qpp::Timer::toc().

Implements qpp::IDisplay.

7.51.3.2 get_duration()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
template<typename U = T>
U qpp::Timer< T, CLOCK_T >::get_duration ( ) const  [inline], [noexcept]
```

Duration specified by U.

Template Parameters

U	Duration, default is T, which defaults to std::chrono::duration<double, 1>, i.e. seconds in double precision

Returns

Duration that passed between the instantiation/reset and invocation of qpp::Timer::toc()

7.51.3.3 operator=() [1/2]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
Timer& qpp::Timer< T, CLOCK_T >::operator= (
            const Timer< T, CLOCK_T > &  )  [default]
```

Default copy assignment operator.

7.51.3.4 operator=() [2/2]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
Timer& qpp::Timer< T, CLOCK_T >::operator= (
            Timer< T, CLOCK_T > &&  )  [default]
```

Default move assignment operator.

7.51.3.5 tic()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
void qpp::Timer< T, CLOCK_T >::tic ( )  [inline], [noexcept]
```

Resets the chronometer.

Resets the starting/ending point to the current time

7.51.3.6 tics()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
double qpp::Timer< T, CLOCK_T >::tics ( ) const  [inline], [noexcept]
```

Time passed in the duration specified by T.

Returns

Number of tics (specified by T) that passed between the instantiation/reset and invocation of qpp::Timer::toc()

7.51.3.7 toc()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
const Timer& qpp::Timer< T, CLOCK_T >::toc ( )  [inline], [noexcept]
```

Stops the chronometer.

Set the current time as the ending point

Returns

Current instance

7.51.4 Member Data Documentation

7.51.4.1 end_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::end_  [protected]
```

7.51.4.2 start_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::start_  [protected]
```

The documentation for this class was generated from the following file:

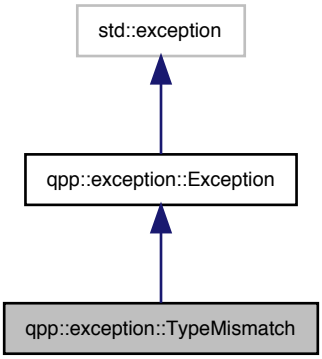
- classes/timer.h

7.52 qpp::exception::TypeMismatch Class Reference

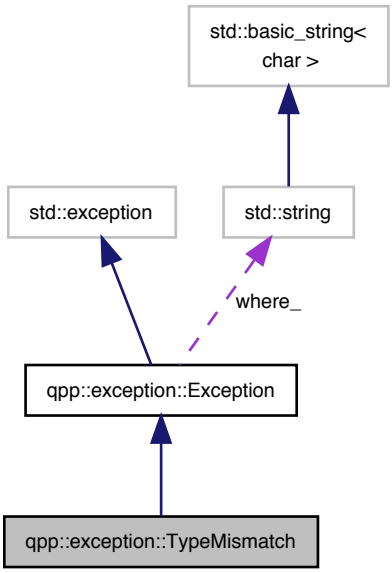
Type mismatch exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::TypeMismatch:



Collaboration diagram for qpp::exception::TypeMismatch:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.52.1 Detailed Description

Type mismatch exception.

Scalar types do not match

7.52.2 Member Function Documentation

7.52.2.1 type_description()

```
std::string qpp::exception::TypeMismatch::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

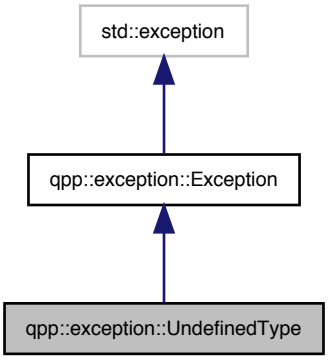
- classes/exception.h

7.53 qpp::exception::UndefinedType Class Reference

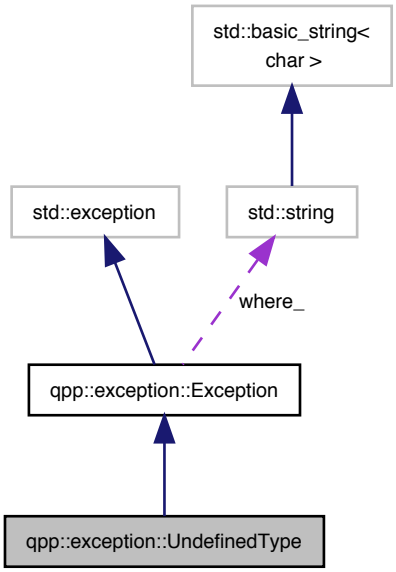
Not defined for this type exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::UndefinedType:



Collaboration diagram for qpp::exception::UndefinedType:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.53.1 Detailed Description

Not defined for this type exception.

Templated specialization is not defined for this type

7.53.2 Member Function Documentation

7.53.2.1 type_description()

```
std::string qpp::exception::UndefinedType::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

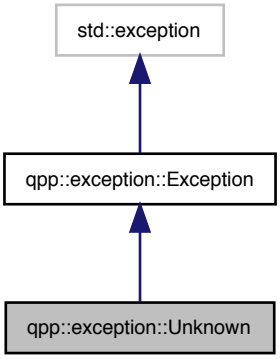
- classes/exception.h

7.54 qpp::exception::Unknown Class Reference

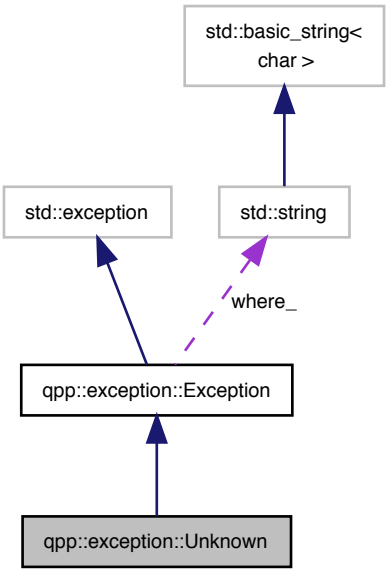
Unknown exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::Unknown:



Collaboration diagram for qpp::exception::Unknown:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.54.1 Detailed Description

Unknown exception.

Thrown when no other exception is suitable (not recommended, it is better to define another suitable exception type)

7.54.2 Member Function Documentation

7.54.2.1 type_description()

```
std::string qpp::exception::Unknown::type_description ( ) const  [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

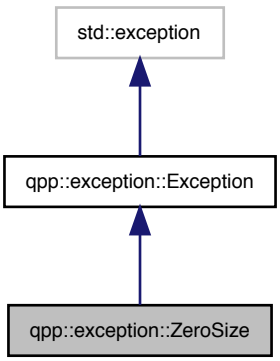
- classes/exception.h

7.55 qpp::exception::ZeroSize Class Reference

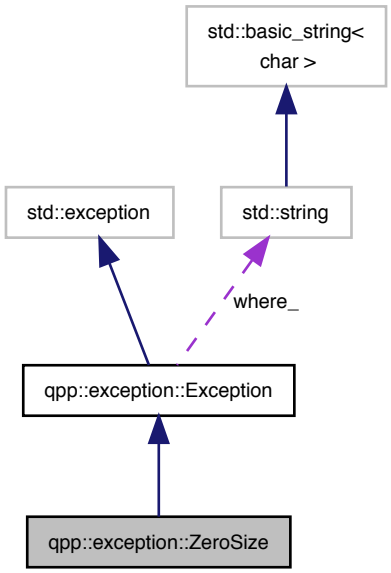
Object has zero size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::ZeroSize:



Collaboration diagram for qpp::exception::ZeroSize:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.55.1 Detailed Description

Object has zero size exception.

Zero sized object, e.g. empty Eigen::Matrix or std::vector with no elements

7.55.2 Member Function Documentation

7.55.2.1 type_description()

```
std::string qpp::exception::ZeroSize::type_description ( ) const  [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

- classes/exception.h

Chapter 8

File Documentation

8.1 classes/codes.h File Reference

Quantum error correcting codes.

Classes

- class qpp::Codes

  const Singleton class that defines quantum error correcting codes

Namespaces

- qpp

  Quantum++ main namespace.

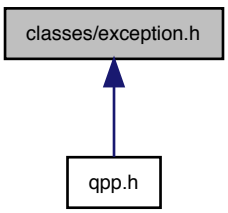
8.1.1 Detailed Description

Quantum error correcting codes.

8.2 classes/exception.h File Reference

Exceptions.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::exception::Exception

  Base class for generating Quantum++ custom exceptions.
- class qpp::exception::Unknown

  Unknown exception.
- class qpp::exception::ZeroSize

  Object has zero size exception.
- class qpp::exception::MatrixNotSquare

  Matrix is not square exception.
- class qpp::exception::MatrixNotCvector

  Matrix is not a column vector exception.
- class qpp::exception::MatrixNotRvector

  Matrix is not a row vector exception.
- class qpp::exception::MatrixNotVector

  Matrix is not a vector exception.
- class qpp::exception::MatrixNotSquareNorCvector

  Matrix is not square nor column vector exception.
- class qpp::exception::MatrixNotSquareNorRvector

  Matrix is not square nor row vector exception.
- class qpp::exception::MatrixNotSquareNorVector

  Matrix is not square nor vector exception.
- class qpp::exception::MatrixMismatchSubsys

  Matrix mismatch subsystems exception.
- class qpp::exception::DimsInvalid

  Invalid dimension(s) exception.
- class qpp::exception::DimsNotEqual

  Dimensions not equal exception.
- class qpp::exception::DimsMismatchMatrix

  Dimension(s) mismatch matrix size exception.
- class qpp::exception::DimsMismatchCvector

  Dimension(s) mismatch column vector size exception.
- class qpp::exception::DimsMismatchRvector

  Dimension(s) mismatch row vector size exception.
- class qpp::exception::DimsMismatchVector

  Dimension(s) mismatch vector size exception.
- class qpp::exception::SubsysMismatchDims

  Subsystems mismatch dimensions exception.
- class qpp::exception::PermInvalid

  Invalid permutation exception.
- class qpp::exception::PermMismatchDims

  Permutation mismatch dimensions exception.
- class qpp::exception::NotQubitMatrix

  Matrix is not 2 x 2 exception.
- class qpp::exception::NotQubitCvector

  Column vector is not 2 x 1 exception.
- class qpp::exception::NotQubitRvector

  Row vector is not 1 x 2 exception.
- class qpp::exception::NotQubitVector

  Vector is not 2 x 1 nor 1 x 2 exception.
- class qpp::exception::NotQubitSubsys

Subsystems are not qubits exception.

- class qpp::exception::NotBipartite

  Not bi-partite exception.
- class qpp::exception::NoCodeword

  Codeword does not exist exception.
- class qpp::exception::OutOfRange

  Parameter out of range exception.
- class qpp::exception::TypeMismatch

  Type mismatch exception.
- class qpp::exception::SizeMismatch

  Size mismatch exception.
- class qpp::exception::UndefinedType

  Not defined for this type exception.
- class qpp::exception::CustomException

  Custom exception.

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::exception

  Quantum++ exception hierarchy namespace.

8.2.1 Detailed Description

Exceptions.

8.3 classes/gates.h File Reference

Quantum gates.

Classes

- class qpp::Gates

  const Singleton class that implements most commonly used gates

Namespaces

- qpp

  Quantum++ main namespace.

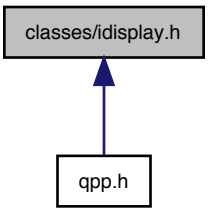
8.3.1 Detailed Description

Quantum gates.

8.4 classes/idisplay.h File Reference

Display interface via the non-virtual interface (NVI)

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::IDisplay

  Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

Namespaces

- qpp

  Quantum++ main namespace.

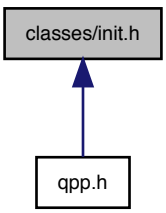
8.4.1 Detailed Description

Display interface via the non-virtual interface (NVI)

8.5 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Init

  const Singleton class that performs additional initializations/cleanups

Namespaces

- qpp

  Quantum++ main namespace.

8.5.1 Detailed Description

Initialization.

8.6 classes/random_devices.h File Reference

Random devices.

Classes

- class qpp::RandomDevices

  Singleton class that manages the source of randomness in the library.

Namespaces

- qpp

  Quantum++ main namespace.

8.6.1 Detailed Description

Random devices.

8.7 classes/states.h File Reference

Quantum states.

Classes

- class qpp::States

  const Singleton class that implements most commonly used states

Namespaces

- qpp
  Quantum++ main namespace.

8.7.1 Detailed Description

Quantum states.

8.8 classes/timer.h File Reference

Timing.

Classes

- class qpp::Timer< T, CLOCK_T >
  Chronometer.

Namespaces

- qpp
  Quantum++ main namespace.

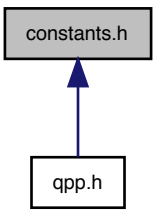
8.8.1 Detailed Description

Timing.

8.9 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- constexpr cplx qpp::operator"" _i (unsigned long long int x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr cplx qpp::operator"" _i (long double x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- cplx qpp::omega (idx D)

  D-th root of unity.

Variables

- constexpr double qpp::chop = 1e-10

  Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.
- constexpr double qpp::eps = 1e-12

  Used to decide whether a number or expression in double precision is zero or not.
- constexpr idx qpp::maxn = 64

  Maximum number of allowed qubits/qudits (subsystems)
- constexpr double qpp::pi = 3.14159265358979323846264338327950288 4

  π
- constexpr double qpp::ee = 2.71828182845904523536028747135266249 7

  Base of natural logarithm, e.
- constexpr double qpp::infty = std::numeric_limits<double>::max()

  Used to denote infinity in double precision.

8.9.1 Detailed Description

Constants.

8.10 entanglement.h File Reference

Entanglement functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt coefficients of the bi-partite pure state A.
- template<typename Derived >
  dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt coefficients of the bi-partite pure state A.
- template<typename Derived >
  cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Alice side.
- template<typename Derived >
  cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Alice side.
- template<typename Derived >
  cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Bob side.
- template<typename Derived >
  cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Bob side.
- template<typename Derived >
  std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)

  G-concurrence of the bi-partite pure state A.
- template<typename Derived >
  double qpp::negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::concurrence (const Eigen::MatrixBase< Derived > &A)

  Wootters concurrence of the bi-partite qubit mixed state A.

8.10.1 Detailed Description

Entanglement functions.

8.11 entropies.h File Reference

Entropy functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  double qpp::entropy (const Eigen::MatrixBase< Derived > &A)

  von-Neumann entropy of the density matrix A
- double qpp::entropy (const std::vector< double > &prob)

  Shannon entropy of the probability distribution prob.
- template<typename Derived >
  double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

  Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- double qpp::renyi (const std::vector< double > &prob, double alpha)

  Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template<typename Derived >
  double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)

  Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- double qpp::tsallis (const std::vector< double > &prob, double q)

  Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template<typename Derived >
  double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

  Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived >
  double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)

  Quantum mutual information between 2 subsystems of a composite system.

8.11.1 Detailed Description

Entropy functions.

8.12 experimental/experimental.h File Reference

Experimental/test functions/classes.

```
#include <algorithm>
#include <cassert>
#include <climits>
#include <cstddef>
#include <random>
#include <utility>
#include <vector>
```

Classes

- class qpp::experimental::Dynamic_bitset
- class qpp::experimental::Bit_circuit
- struct qpp::experimental::Bit_circuit::Gate_count

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::experimental

  Experimental/test functions/classes, do not use or modify.

Typedefs

- using idx = std::size_t

8.12.1 Detailed Description

Experimental/test functions/classes.

8.12.2 Typedef Documentation

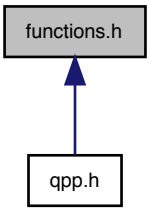
8.12.2.1 idx

```
using idx = std::size_t
```

8.13 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



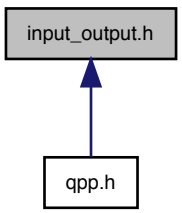
8.13.1 Detailed Description

Generic quantum computing functions.

8.14 input_output.h File Reference

Input/output functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

  Eigen expression ostream manipulator.
- internal::IOManipEigen qpp::disp (cplx z, double chop=qpp::chop)

  Complex number ostream manipulator.
- template<typename InputIterator >
  internal::IOManipRange< InputIterator > qpp::disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

  Range ostream manipulator.
- template<typename Container >
  internal::IOManipRange< typename Container::const_iterator > qpp::disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="]", typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template<typename PointerType >
  internal::IOManipPointer< PointerType > qpp::disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")

  C-style pointer ostream manipulator.
- template<typename Derived >
  void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

  Saves Eigen expression to a binary file (internal format) in double precision.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::load (const std::string &fname)

  Loads Eigen matrix from a binary file (internal format) in double precision.

8.14.1 Detailed Description

Input/output functions.

8.15 instruments.h File Reference

Measurement functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Generalized inner product.
- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)

  Generalized inner product.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Measures the state A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)

  Measures the state A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

  Measures the state A in the orthonormal basis specified by the unitary matrix U.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

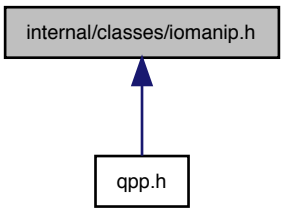
8.15.1 Detailed Description

Measurement functions.

8.16 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::IOManipRange< InputIterator >
- class qpp::internal::IOManipPointer< PointerType >
- class qpp::internal::IOManipEigen

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

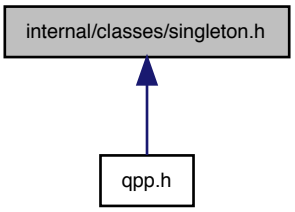
8.16.1 Detailed Description

Input/output manipulators.

8.17 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::Singleton< T >

  Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

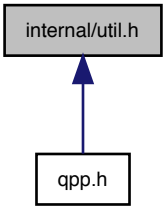
8.17.1 Detailed Description

Singleton pattern via CRTP.

8.18 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



Classes

- struct qpp::internal::Display_Impl_

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

Functions

- void qpp::internal::n2multiidx (idx n, idx numdims, const idx ∗const dims, idx ∗result) noexcept
- idx qpp::internal::multiidx2n (const idx ∗const midx, idx numdims, const idx ∗const dims) noexcept
- template<typename Derived >
  bool qpp::internal::check_square_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_rvector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_cvector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
  bool qpp::internal::check_nonzero_size (const T &x) noexcept
- template<typename T1 , typename T2 >
  bool qpp::internal::check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept
- bool qpp::internal::check_dims (const std::vector< idx > &dims)
- template<typename Derived >
  bool qpp::internal::check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)

- template<typename Derived >
  bool qpp::internal::check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- bool qpp::internal::check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept
- bool qpp::internal::check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template<typename Derived >
  bool qpp::internal::check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept
- bool qpp::internal::check_perm (const std::vector< idx > &perm)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::internal::kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::internal::dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
  void qpp::internal::variadic_vector_emplace (std::vector< T > &)
- template<typename T , typename First , typename... Args>
  void qpp::internal::variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)
- idx qpp::internal::get_num_subsys (idx sz, idx d)
- idx qpp::internal::get_dim_subsys (idx sz, idx N)

8.18.1 Detailed Description

Internal utility functions.

8.19 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::Scalar > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< !std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

8.19.1 Detailed Description

Input/output interfacing with MATLAB.

8.20 number_theory.h File Reference

Number theory functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- std::vector< int > qpp::x2contfrac (double x, idx N, idx cut=1e5)

  Simple continued fraction expansion.
- double qpp::contfrac2x (const std::vector< int > &cf, idx N=idx(-1))

  Real representation of a simple continued fraction.
- bigint qpp::gcd (bigint a, bigint b)

  Greatest common divisor of two integers.
- bigint qpp::gcd (const std::vector< bigint > &as)

  Greatest common divisor of a list of integers.
- bigint qpp::lcm (bigint a, bigint b)

  Least common multiple of two integers.
- bigint qpp::lcm (const std::vector< bigint > &as)

  Least common multiple of a list of integers.

- std::vector< idx > qpp::invperm (const std::vector< idx > &perm)

  Inverse permutation.
- std::vector< idx > qpp::compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

  Compose permutations.
- std::vector< bigint > qpp::factors (bigint a)

  Prime factor decomposition.
- bigint qpp::modmul (bigint a, bigint b, bigint p)

  Modular multiplication without overflow.
- bigint qpp::modpow (bigint a, bigint n, bigint p)

  Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.
- std::tuple< bigint, bigint, bigint > qpp::egcd (bigint a, bigint b)

  Extended greatest common divisor of two integers.
- bigint qpp::modinv (bigint a, bigint p)

  Modular inverse of a mod p.
- bool qpp::isprime (bigint p, idx k=80)

  Primality test based on the Miller-Rabin's algorithm.
- bigint qpp::randprime (bigint a, bigint b, idx N=1000)

  Generates a random big prime uniformly distributed in the interval [a, b].

8.20.1 Detailed Description

Number theory functions.

8.21 operations.h File Reference

Quantum operation functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.

- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Applies the channel specified by the set of Kraus operators Ks to the density matrix A.
- template<typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- template<typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- cmat qpp::kraus2super (const std::vector< cmat > &Ks)

  Superoperator matrix.
- cmat qpp::kraus2choi (const std::vector< cmat > &Ks)

  Choi matrix.
- std::vector< cmat > qpp::choi2kraus (const cmat &A)

  Orthogonal Kraus operators from Choi matrix.
- cmat qpp::choi2super (const cmat &A)

  Converts Choi matrix to superoperator matrix.
- cmat qpp::super2choi (const cmat &A)

  Converts superoperator matrix to Choi matrix.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Partial transpose.

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)

  Subsystem permutation.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)

  Subsystem permutation.

8.21.1 Detailed Description

Quantum operation functions.

8.22 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```
#include <algorithm>
#include <cassert>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iterator>
#include <limits>
#include <memory>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/idisplay.h"
```

```
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/init.h"
#include "functions.h"
```

Namespaces

- qpp

  Quantum++ main namespace.

Macros

- #define QPP_UNUSED_

8.22.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

8.22.2 Macro Definition Documentation

8.22.2.1 QPP_UNUSED_

```
#define QPP_UNUSED_
```

8.23 random.h File Reference

Randomness-related functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- double qpp::rand (double a, double b)

  Generates a random real number uniformly distributed in the interval [a, b)
- bigint qpp::rand (bigint a, bigint b)

  Generates a random big integer uniformly distributed in the interval [a, b].
- idx qpp::randidx (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

  Generates a random index (idx) uniformly distributed in the interval [a, b].
- template<typename Derived >
  Derived qpp::rand (idx rows, idx cols, double a=0, double b=1)

  Generates a random matrix with entries uniformly distributed in the interval [a, b)
- template<>
  dmat qpp::rand (idx rows, idx cols, double a, double b)

  Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
- template<>
  cmat qpp::rand (idx rows, idx cols, double a, double b)

  Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
- template<typename Derived >
  Derived qpp::randn (idx rows, idx cols, double mean=0, double sigma=1)

  Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>
  dmat qpp::randn (idx rows, idx cols, double mean, double sigma)

  Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)
- template<>
  cmat qpp::randn (idx rows, idx cols, double mean, double sigma)

  Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)
- double qpp::randn (double mean=0, double sigma=1)

  Generates a random real number (double) normally distributed in N(mean, sigma)
- cmat qpp::randU (idx D=2)

  Generates a random unitary matrix.
- cmat qpp::randV (idx Din, idx Dout)

  Generates a random isometry matrix.
- std::vector< cmat > qpp::randkraus (idx N, idx D=2)

  Generates a set of random Kraus operators.
- cmat qpp::randH (idx D=2)

  Generates a random Hermitian matrix.
- ket qpp::randket (idx D=2)

  Generates a random normalized ket (pure state vector)
- cmat qpp::randrho (idx D=2)

  Generates a random density matrix.
- std::vector< idx > qpp::randperm (idx N)

  Generates a random uniformly distributed permutation.
- std::vector< double > qpp::randprob (idx N)

  Generates a random probability vector uniformly distributed over the probability simplex.

8.23.1 Detailed Description

Randomness-related functions.

8.24 statistics.h File Reference

Statistics functions.

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- std::vector< double > qpp::uniform (idx N)

  Uniform probability distribution vector.
- std::vector< double > qpp::marginalX (const dmat &probXY)

  Marginal distribution.
- std::vector< double > qpp::marginalY (const dmat &probXY)

  Marginal distribution.
- template<typename Container >
  double qpp::avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Average.
- template<typename Container >
  double qpp::cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Covariance.
- template<typename Container >
  double qpp::var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Variance.
- template<typename Container >
  double qpp::sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Standard deviation.
- template<typename Container >
  double qpp::cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Correlation.

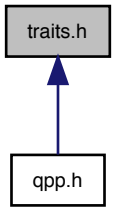
8.24.1 Detailed Description

Statistics functions.

8.25 traits.h File Reference

Type traits.

This graph shows which files directly or indirectly include this file:



Classes

- struct qpp::make_void< Ts >
  Helper for qpp::to_void<> alias template.
- struct qpp::is_iterable< T, typename >
  Checks whether T is compatible with an STL-like iterable container.
- struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().↩ end()), typename T::value_type > >
  Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct qpp::is_matrix_expression< Derived >
  Checks whether the type is an Eigen matrix expression.
- struct qpp::is_complex< T >
  Checks whether the type is a complex type.
- struct qpp::is_complex< std::complex< T > >
  Checks whether the type is a complex number type, specialization for complex types.

Namespaces

- qpp
  Quantum++ main namespace.

Typedefs

- template<typename... Ts>
  using qpp::to_void = typename make_void< Ts... >::type
  Alias template that implements the proposal for void_t.

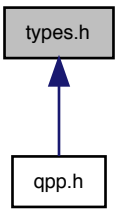
8.25.1 Detailed Description

Type traits.

8.26 types.h File Reference

Type aliases.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Typedefs

- using qpp::idx = std::size_t

  Non-negative integer index.
- using qpp::bigint = long long int

  Big integer.
- using qpp::cplx = std::complex< double >

  Complex number in double precision.
- using qpp::ket = Eigen::VectorXcd

  Complex (double precision) dynamic Eigen column vector.
- using qpp::bra = Eigen::RowVectorXcd

  Complex (double precision) dynamic Eigen row vector.
- using qpp::cmat = Eigen::MatrixXcd

  Complex (double precision) dynamic Eigen matrix.
- using qpp::dmat = Eigen::MatrixXd

  Real (double precision) dynamic Eigen matrix.
- template<typename Scalar >
  using qpp::dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

  Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar >
  using qpp::dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >

  Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar >
  using qpp::dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >

  Dynamic Eigen row vector over the field specified by Scalar.

8.26.1 Detailed Description

Type aliases.

8.27 /Users/vlad/Dropbox/programming/cpp/qpp/README.md File Reference

Index

/Users/vlad/Dropbox/programming/cpp/qpp/READM↩
E.md, 245
~Codes
qpp::Codes, 94
~Gates
qpp::Gates, 127
~IDisplay
qpp::IDisplay, 136
~Init
qpp::Init, 138
~RandomDevices
qpp::RandomDevices, 189
~Singleton
qpp::internal::Singleton, 192
~States
qpp::States, 197
~Timer
qpp::Timer, 208

A_
qpp::internal::IOManipEigen, 141
all
qpp::experimental::Dynamic_bitset, 112
any
qpp::experimental::Dynamic_bitset, 112
apply
qpp, 24–26
applyCTRL
qpp, 26, 27
avg
qpp, 28

b00
qpp::States, 200
b01
qpp::States, 200
b10
qpp::States, 200
b11
qpp::States, 200
bigint
qpp, 22
bra
qpp, 22

CNOTba
qpp::Gates, 132
CNOT
qpp::Gates, 132
qpp::experimental::Bit_circuit, 90
qpp::experimental::Bit_circuit::Gate_count, 123
CTRL
qpp::Gates, 127
check_cvector
qpp::internal, 84
check_dims
qpp::internal, 84
check_dims_match_cvect
qpp::internal, 84
check_dims_match_mat
qpp::internal, 85
check_dims_match_rvect
qpp::internal, 85
check_eq_dims
qpp::internal, 85
check_matching_sizes
qpp::internal, 85
check_nonzero_size
qpp::internal, 85
check_perm
qpp::internal, 85
check_qubit_cvector
qpp::internal, 86
check_qubit_matrix
qpp::internal, 86
check_qubit_rvector
qpp::internal, 86
check_qubit_vector
qpp::internal, 86
check_rvector
qpp::internal, 86
check_square_mat
qpp::internal, 86
check_subsys_match_dims
qpp::internal, 87
check_vector
qpp::internal, 87
choi2kraus
qpp, 28
choi2super
qpp, 29
chop
qpp, 80
chop_
qpp::internal::IOManipEigen, 141
classes/codes.h, 219
classes/exception.h, 219
classes/gates.h, 221
classes/idisplay.h, 222

classes/init.h, 222
classes/random_devices.h, 223
classes/states.h, 223
classes/timer.h, 224
cmat
    qpp, 22
Codes
    qpp::Codes, 94
codeword
    qpp::Codes, 94
compperm
    qpp, 29
concurrence
    qpp, 29
constants.h, 224
contfrac2x
    qpp, 30
cor
    qpp, 30
count
    qpp::experimental::Dynamic_bitset, 113
cov
    qpp, 31
cplx
    qpp, 22
CustomException
    qpp::exception::CustomException, 96
CZ
    qpp::Gates, 132

data
    qpp::experimental::Dynamic_bitset, 113
dirsum2
    qpp::internal, 87
disp
    qpp, 31–33
display
    qpp::IDisplay, 136
    qpp::Timer, 208
    qpp::internal::IOManipEigen, 140
    qpp::internal::IOManipPointer, 143
    qpp::internal::IOManipRange, 146
display_impl_
    qpp::internal::Display_Impl_, 109
dmat
    qpp, 22
dyn_col_vect
    qpp, 22
dyn_mat
    qpp, 23
dyn_row_vect
    qpp, 23
Dynamic_bitset
    qpp::experimental::Dynamic_bitset, 112

ee
    qpp, 80
egcd
    qpp, 34
end_
    qpp::Timer, 210
    qpp::internal::IOManipPointer, 143
    qpp::internal::IOManipRange, 147
entanglement
    qpp, 34, 35
entanglement.h, 225
entropies.h, 227
entropy
    qpp, 35
eps
    qpp, 80
Exception
    qpp::exception::Exception, 122
expandout
    qpp::Gates, 128, 129
experimental.h
    idx, 228
experimental/experimental.h, 228

FRED
    qpp::Gates, 132
    qpp::experimental::Bit_circuit, 91
    qpp::experimental::Bit_circuit::Gate_count, 123
factors
    qpp, 36
Fd
    qpp::Gates, 129
first_
    qpp::internal::IOManipRange, 147
flip
    qpp::experimental::Dynamic_bitset, 113
functions.h, 229

GHZ
    qpp::States, 200
gate_count
    qpp::experimental::Bit_circuit, 92
Gates
    qpp::Gates, 126
gcd
    qpp, 36, 37
gconcurrence
    qpp, 37
get
    qpp::experimental::Dynamic_bitset, 114
get_dim_subsys
    qpp::internal, 87
get_duration
    qpp::Timer, 209
get_instance
    qpp::internal::Singleton, 192
get_num_subsys
    qpp::internal, 87
get_prng
    qpp::RandomDevices, 189
get_thread_local_instance
    qpp::internal::Singleton, 193

H
qpp::Gates, 132

IDisplay
qpp::IDisplay, 135, 136
IOManipEigen
qpp::internal::IOManipEigen, 140
IOManipPointer
qpp::internal::IOManipPointer, 142, 143
IOManipRange
qpp::internal::IOManipRange, 146
Id
qpp::Gates, 130
Id2
qpp::Gates, 132
idx
experimental.h, 228
qpp, 23
index_
qpp::experimental::Dynamic_bitset, 114
infty
qpp, 80
Init
qpp::Init, 138
input_output.h, 229
instruments.h, 230
internal/classes/iomanip.h, 232
internal/classes/singleton.h, 233
internal/util.h, 233
internal::Singleton< const Codes >
qpp::Codes, 95
internal::Singleton< const Gates >
qpp::Gates, 131
internal::Singleton< const Init >
qpp::Init, 139
internal::Singleton< const States >
qpp::States, 200
internal::Singleton< RandomDevices >
qpp::RandomDevices, 190
invperm
qpp, 38
ip
qpp, 38, 39
isprime
qpp, 39

jn
qpp::States, 197

ket
qpp, 23
kraus2choi
qpp, 39
kraus2super
qpp, 40
kron2
qpp::internal, 87

last_
qpp::internal::IOManipRange, 147
lcm
qpp, 40, 41
load
qpp, 41
qpp::RandomDevices, 189
loadMATLAB
qpp, 42
lognegativity
qpp, 43

MATLAB/matlab.h, 235
marginalX
qpp, 44
marginalY
qpp, 44
maxn
qpp, 81
measure
qpp, 45–49
measure_seq
qpp, 50
mes
qpp::States, 198
minus
qpp::States, 198
modinv
qpp, 51
modmul
qpp, 52
modpow
qpp, 52
multiidx2n
qpp::internal, 88

n2multiidx
qpp::internal, 88
N_
qpp::experimental::Dynamic_bitset, 119
qpp::internal::IOManipPointer, 144
NOT
qpp::experimental::Bit_circuit, 91
qpp::experimental::Bit_circuit::Gate_count, 123
negativity
qpp, 53
none
qpp::experimental::Dynamic_bitset, 114
number_theory.h, 236

offset_
qpp::experimental::Dynamic_bitset, 114
omega
qpp, 53
one
qpp::States, 198
operations.h, 237
operator!=
qpp::experimental::Dynamic_bitset, 115
operator<<

qpp::IDisplay, 137
qpp::experimental::Dynamic_bitset, 118
operator=
qpp::IDisplay, 136
qpp::Timer, 209
qpp::internal::IOManipPointer, 143
qpp::internal::IOManipRange, 146
qpp::internal::Singleton, 193
operator==
qpp::experimental::Dynamic_bitset, 115
operator"" _i
qpp, 55

p_
qpp::internal::IOManipPointer, 144
pGHZ
qpp::States, 201
pb00
qpp::States, 201
pb01
qpp::States, 201
pb10
qpp::States, 201
pb11
qpp::States, 201
pi
qpp, 81
plus
qpp::States, 199
prng_
qpp::RandomDevices, 190
ptrace
qpp, 55, 56
ptrace1
qpp, 56, 57
ptrace2
qpp, 57, 58
ptranspose
qpp, 58, 59
pW
qpp::States, 201
px0
qpp::States, 202
px1
qpp::States, 202
py0
qpp::States, 202
py1
qpp::States, 202
pz0
qpp::States, 202
pz1
qpp::States, 202

QPP_UNUSED_
qpp.h, 240
qmutualinfo
qpp, 59, 60
qpp, 13

apply, 24–26
applyCTRL, 26, 27
avg, 28
bigint, 22
bra, 22
choi2kraus, 28
choi2super, 29
chop, 80
cmat, 22
compperm, 29
concurrence, 29
contfrac2x, 30
cor, 30
cov, 31
cplx, 22
disp, 31–33
dmat, 22
dyn_col_vect, 22
dyn_mat, 23
dyn_row_vect, 23
ee, 80
egcd, 34
entanglement, 34, 35
entropy, 35
eps, 80
factors, 36
gcd, 36, 37
gconcurrence, 37
idx, 23
infty, 80
invperm, 38
ip, 38, 39
isprime, 39
ket, 23
kraus2choi, 39
kraus2super, 40
lcm, 40, 41
load, 41
loadMATLAB, 42
lognegativity, 43
marginalX, 44
marginalY, 44
maxn, 81
measure, 45–49
measure_seq, 50
modinv, 51
modmul, 52
modpow, 52
negativity, 53
omega, 53
operator"" _i, 55
pi, 81
ptrace, 55, 56
ptrace1, 56, 57
ptrace2, 57, 58
ptranspose, 58, 59
qmutualinfo, 59, 60
rand, 60–62

randH, 63
randidx, 63
randket, 63
randkraus, 64
randn, 64–66
randperm, 66
randprime, 67
randprob, 67
randrho, 67
randU, 68
randV, 68
renyi, 68, 69
save, 69
saveMATLAB, 70
schmidtA, 71
schmidtB, 72
schmidtcoeffs, 73
schmidtprobs, 74
sigma, 75
super2choi, 75
syspermute, 77
to_void, 24
tsallis, 78
uniform, 79
var, 79
x2contfrac, 79
qpp.h, 239
QPP_UNUSED_, 240
qpp::Bit_circuit, 92
qpp::Codes, 92
~Codes, 94
Codes, 94
codeword, 94
internal::Singleton< const Codes >, 95
Type, 93
qpp::Dynamic_bitset, 119
qpp::Gates, 124
~Gates, 127
CNOTba, 132
CNOT, 132
CTRL, 127
CZ, 132
expandout, 128, 129
FRED, 132
Fd, 129
Gates, 126
H, 132
Id, 130
Id2, 132
internal::Singleton< const Gates >, 131
Rn, 130
S, 133
SWAP, 133
T, 133
TOF, 133
X, 133
Xd, 131
Y, 133
Z, 134
Zd, 131
qpp::IDisplay, 134
~IDisplay, 136
display, 136
IDisplay, 135, 136
operator<<, 137
operator=, 136
qpp::Init, 137
~Init, 138
Init, 138
internal::Singleton< const Init >, 139
qpp::RandomDevices, 187
~RandomDevices, 189
get_prng, 189
internal::Singleton< RandomDevices >, 190
load, 189
prng_, 190
RandomDevices, 189
rd_, 190
save, 190
qpp::States, 195
~States, 197
b00, 200
b01, 200
b10, 200
b11, 200
GHZ, 200
internal::Singleton< const States >, 200
jn, 197
mes, 198
minus, 198
one, 198
pGHZ, 201
pb00, 201
pb01, 201
pb10, 201
pb11, 201
plus, 199
pW, 201
px0, 202
px1, 202
py0, 202
py1, 202
pz0, 202
pz1, 202
States, 197
W, 203
x0, 203
x1, 203
y0, 203
y1, 203
z0, 203
z1, 204
zero, 199
qpp::Timer
~Timer, 208
display, 208

end_, 210
get_duration, 209
operator=, 209
start_, 210
tic, 209
tics, 210
Timer, 208
toc, 210
qpp::Timer< T, CLOCK_T >, 206
qpp::exception, 81
qpp::exception::CustomException, 95
CustomException, 96
type_description, 97
what_, 97
qpp::exception::DimsInvalid, 98
type_description, 99
qpp::exception::DimsMismatchCvector, 99
type_description, 101
qpp::exception::DimsMismatchMatrix, 101
type_description, 102
qpp::exception::DimsMismatchRvector, 103
type_description, 104
qpp::exception::DimsMismatchVector, 105
type_description, 106
qpp::exception::DimsNotEqual, 107
type_description, 108
qpp::exception::Exception, 120
Exception, 122
type_description, 122
what, 122
where_, 123
qpp::exception::MatrixMismatchSubsys, 154
type_description, 155
qpp::exception::MatrixNotCvector, 155
type_description, 157
qpp::exception::MatrixNotRvector, 157
type_description, 158
qpp::exception::MatrixNotSquare, 159
type_description, 160
qpp::exception::MatrixNotSquareNorCvector, 161
type_description, 162
qpp::exception::MatrixNotSquareNorRvector, 163
type_description, 164
qpp::exception::MatrixNotSquareNorVector, 165
type_description, 166
qpp::exception::MatrixNotVector, 167
type_description, 168
qpp::exception::NoCodeword, 169
type_description, 170
qpp::exception::NotBipartite, 171
type_description, 172
qpp::exception::NotQubitCvector, 172
type_description, 174
qpp::exception::NotQubitMatrix, 174
type_description, 175
qpp::exception::NotQubitRvector, 176
type_description, 177
qpp::exception::NotQubitSubsys, 178
type_description, 179
qpp::exception::NotQubitVector, 180
type_description, 181
qpp::exception::OutOfRange, 182
type_description, 183
qpp::exception::PermInvalid, 184
type_description, 185
qpp::exception::PermMismatchDims, 185
type_description, 187
qpp::exception::SizeMismatch, 193
type_description, 194
qpp::exception::SubsysMismatchDims, 204
type_description, 205
qpp::exception::TypeMismatch, 211
type_description, 212
qpp::exception::UndefinedType, 213
type_description, 214
qpp::exception::Unknown, 214
type_description, 216
qpp::exception::ZeroSize, 216
type_description, 217
qpp::experimental, 83
qpp::experimental::Bit_circuit, 89
CNOT, 90
FRED, 91
gate_count, 92
NOT, 91
reset, 91
SWAP, 91
TOF, 91
X, 91
qpp::experimental::Bit_circuit::Gate_count, 123
CNOT, 123
FRED, 123
NOT, 123
SWAP, 124
TOF, 124
X, 124
qpp::experimental::Dynamic_bitset, 110
all, 112
any, 112
count, 113
data, 113
Dynamic_bitset, 112
flip, 113
get, 114
index_, 114
N_, 119
none, 114
offset_, 114
operator!=, 115
operator<<, 118
operator==, 115
rand, 115, 116
reset, 116
set, 117
size, 117
storage_size, 117

storage_size_, 119
storage_type, 112
to_string, 118
v_, 119
value_type, 112
qpp::internal, 83
check_cvector, 84
check_dims, 84
check_dims_match_cvect, 84
check_dims_match_mat, 85
check_dims_match_rvect, 85
check_eq_dims, 85
check_matching_sizes, 85
check_nonzero_size, 85
check_perm, 85
check_qubit_cvector, 86
check_qubit_matrix, 86
check_qubit_rvector, 86
check_qubit_vector, 86
check_rvector, 86
check_square_mat, 86
check_subsys_match_dims, 87
check_vector, 87
dirsum2, 87
get_dim_subsys, 87
get_num_subsys, 87
kron2, 87
multiidx2n, 88
n2multiidx, 88
variadic_vector_emplace, 88
qpp::internal::Display_Impl_, 109
display_impl_, 109
qpp::internal::IOManipEigen, 139
A_, 141
chop_, 141
display, 140
IOManipEigen, 140
qpp::internal::IOManipPointer
display, 143
end_, 143
IOManipPointer, 142, 143
N_, 144
operator=, 143
p_, 144
separator_, 144
start_, 144
qpp::internal::IOManipPointer< PointerType >, 141
qpp::internal::IOManipRange
display, 146
end_, 147
first_, 147
IOManipRange, 146
last_, 147
operator=, 146
separator_, 147
start_, 147
qpp::internal::IOManipRange< InputIterator >, 145
qpp::internal::Singleton
~Singleton, 192
get_instance, 192
get_thread_local_instance, 193
operator=, 193
Singleton, 192
qpp::internal::Singleton< T >, 191
qpp::is_complex< std::complex< T > >, 149
qpp::is_complex< T >, 148
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >, 151
qpp::is_iterable< T, typename >, 150
qpp::is_matrix_expression< Derived >, 152
qpp::make_void
type, 153
qpp::make_void< Ts >, 153

rand
qpp, 60–62
qpp::experimental::Dynamic_bitset, 115, 116
randH
qpp, 63
randidx
qpp, 63
randket
qpp, 63
randkraus
qpp, 64
randn
qpp, 64–66
random.h, 240
RandomDevices
qpp::RandomDevices, 189
randperm
qpp, 66
randprime
qpp, 67
randprob
qpp, 67
randrho
qpp, 67
randU
qpp, 68
randV
qpp, 68
rd_
qpp::RandomDevices, 190
renyi
qpp, 68, 69
reset
qpp::experimental::Bit_circuit, 91
qpp::experimental::Dynamic_bitset, 116
Rn
qpp::Gates, 130

S
qpp::Gates, 133
SWAP
qpp::Gates, 133

qpp::experimental::Bit_circuit, 91
qpp::experimental::Bit_circuit::Gate_count, 124
save
qpp, 69
qpp::RandomDevices, 190
saveMATLAB
qpp, 70
schmidtA
qpp, 71
schmidtB
qpp, 72
schmidtcoeffs
qpp, 73
schmidtprobs
qpp, 74
separator_
qpp::internal::IOManipPointer, 144
qpp::internal::IOManipRange, 147
set
qpp::experimental::Dynamic_bitset, 117
sigma
qpp, 75
Singleton
qpp::internal::Singleton, 192
size
qpp::experimental::Dynamic_bitset, 117
start_
qpp::Timer, 210
qpp::internal::IOManipPointer, 144
qpp::internal::IOManipRange, 147
States
qpp::States, 197
statistics.h, 242
storage_size
qpp::experimental::Dynamic_bitset, 117
storage_size_
qpp::experimental::Dynamic_bitset, 119
storage_type
qpp::experimental::Dynamic_bitset, 112
super2choi
qpp, 75
syspermute
qpp, 77

T
qpp::Gates, 133
TOF
qpp::Gates, 133
qpp::experimental::Bit_circuit, 91
qpp::experimental::Bit_circuit::Gate_count, 124
tic
qpp::Timer, 209
tics
qpp::Timer, 210
Timer
qpp::Timer, 208
to_string
qpp::experimental::Dynamic_bitset, 118
to_void
qpp, 24
toc
qpp::Timer, 210
traits.h, 243
tsallis
qpp, 78
Type
qpp::Codes, 93
type
qpp::make_void, 153
type_description
qpp::exception::CustomException, 97
qpp::exception::DimsInvalid, 99
qpp::exception::DimsMismatchCvector, 101
qpp::exception::DimsMismatchMatrix, 102
qpp::exception::DimsMismatchRvector, 104
qpp::exception::DimsMismatchVector, 106
qpp::exception::DimsNotEqual, 108
qpp::exception::Exception, 122
qpp::exception::MatrixMismatchSubsys, 155
qpp::exception::MatrixNotCvector, 157
qpp::exception::MatrixNotRvector, 158
qpp::exception::MatrixNotSquare, 160
qpp::exception::MatrixNotSquareNorCvector, 162
qpp::exception::MatrixNotSquareNorRvector, 164
qpp::exception::MatrixNotSquareNorVector, 166
qpp::exception::MatrixNotVector, 168
qpp::exception::NoCodeword, 170
qpp::exception::NotBipartite, 172
qpp::exception::NotQubitCvector, 174
qpp::exception::NotQubitMatrix, 175
qpp::exception::NotQubitRvector, 177
qpp::exception::NotQubitSubsys, 179
qpp::exception::NotQubitVector, 181
qpp::exception::OutOfRange, 183
qpp::exception::PermInvalid, 185
qpp::exception::PermMismatchDims, 187
qpp::exception::SizeMismatch, 194
qpp::exception::SubsysMismatchDims, 205
qpp::exception::TypeMismatch, 212
qpp::exception::UndefinedType, 214
qpp::exception::Unknown, 216
qpp::exception::ZeroSize, 217
types.h, 244

uniform
qpp, 79

v_
qpp::experimental::Dynamic_bitset, 119
value_type
qpp::experimental::Dynamic_bitset, 112
var
qpp, 79
variadic_vector_emplace
qpp::internal, 88

W
qpp::States, 203

what
qpp::exception::Exception, 122
what_
qpp::exception::CustomException, 97
where_
qpp::exception::Exception, 123

X
qpp::Gates, 133
qpp::experimental::Bit_circuit, 91
qpp::experimental::Bit_circuit::Gate_count, 124
x0
qpp::States, 203
x1
qpp::States, 203
x2contfrac
qpp, 79
Xd
qpp::Gates, 131

Y
qpp::Gates, 133
y0
qpp::States, 203
y1
qpp::States, 203

Z
qpp::Gates, 134
z0
qpp::States, 203
z1
qpp::States, 204
Zd
qpp::Gates, 131
zero
qpp::States, 199