

Quantum++

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Chapter 1

Quantum++

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Quantum++ is a C++11 general purpose quantum computing library, composed solely of template header files. Quantum++ is written in standard C++11 and has very low external dependencies, using only the [Eigen 3](#) linear algebra header-only template library and, if available, the [OpenMP](#) multi-processing library.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance.

If you are interesting in contributing, please contact me. To contribute, you need to have a good knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and working experience with [Eigen 3](#).

For additional [Eigen 3](#) documentation see <http://eigen.tuxfamily.org/dox/>. For a simple [Eigen 3](#) quick ASCII reference see <http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt>.

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Building instructions

Configuration:

- Compiler: [g++](#) version 4.8 or later (for good C++11 support)
- [Eigen 3](#) library located in \$HOME/eigen
- Quantum++ library located in \$HOME/qpp
- [MATLAB](#) compiler include header files: /Applications/MATLAB_R2015b.app/extern/include
- [MATLAB](#) compiler shared library files: /Applications/MATLAB_R2015b.app/bin/maci64

Building without a build system

- Example file: \$HOME/qpp/examples/minimal.cpp
- Output executable: \$HOME/qpp/examples/minimal
- Must run the commands below from inside the directory \$HOME/qpp/examples

Release version (without MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
-O3 -DNDEBUG -DEIGEN_NO_DEBUG \
-isystem $HOME/eigen -I $HOME/qpp/include \
minimal.cpp -o minimal
```

Debug version (without MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
-g3 -DDEBUG \
-isystem $HOME/eigen -I $HOME/qpp/include \
minimal.cpp -o minimal
```

Release version (with MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
-O3 -DNDEBUG -DEIGEN_NO_DEBUG \
-isystem $HOME/eigen -I $HOME/qpp/include \
-I/Applications/MATLAB_R2015b.app/extern/include \
-L/Applications/MATLAB_R2015b.app/bin/mac64 \
-lmx -lmat minimal.cpp -o minimal
```

Debug version (with MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
-g3 -DDEBUG \
-isystem $HOME/eigen -I $HOME/qpp/include \
-I /Applications/MATLAB_R2015b.app/extern/include \
-L /Applications/MATLAB_R2015b.app/bin/mac64 \
-lmx -lmat minimal.cpp -o minimal
```

Building using cmake

The current version of the repository has a `./CMakeLists.txt` configuration file for building examples using `cmake`. To build an example using `cmake`, I recommend an out-of-source build, i.e., from the root of the project (where `./include` is located), type

```
mkdir ./build
cd ./build
cmake ..
make
```

The above commands build the release version (default) executable `qpp`, from the source file `./examples/minimal.cpp`, without MATLAB support (default), inside the directory `./build`. To build a different configuration, e.g. debug version with MATLAB support, type from the root of the project

```
cd ./build
rm -rf *
cmake -DCMAKE_BUILD_TYPE=Debug -DWITH_MATLAB=ON ..
make
```

Or, to disable OpenMP support (enabled by default), type

```
cd ./build
rm -rf *
cmake -DWITH_OPENMP=OFF ..
make
```

To change the name of the example file, the location of the `Eigen 3` library or the location of `MATLAB` installation, edit the `./CMakeLists.txt` file. See also `./CMakeLists.txt` for additional options. Do not forget to remove everything from the `./build` directory before a fresh build!

Additional remarks

- The C++ compiler must be C++11 compliant.
- If using Windows, I recommend compiling under cygwin via `cmake` and `g++`. See also <http://stackoverflow.com/questions/28997206/cygwin-support-for-c11-in-g4-9-2> for a bug related to lack of support for some C++11 math functions, and how to fix it. Quick fix: patch the standard library header file `<cmath>` using the provided patch `./cmath_cygwin.patch`.
- If your compiler does not support OpenMP (as it is the case e.g with `clang++`), disable OpenMP in your build, as otherwise the linker may not find the `gomp` library.
- If you run the program on OS X with MATLAB support, make sure that the environment variable `DYLD_LIBRARY_PATH` is set to point to the MATLAB compiler library location, see the `run OSX MATLAB` script. Otherwise, you will get a runtime error like `dyld: Library not loaded: @rpath/libmat.dylib`.

* I recommend running via a script, as otherwise setting the '`DYLD_LIBRARY_PATH`' globally may interfere with [macports] (<https://www.macports.org/>)' [cmake] (<http://www.cmake.org/>) installation (in case you use [cmake] (<http://www.cmake.org/>) from [macports] (<https://www.macports.org/>)). If you use a script, then the environment variable is local to the script and does not interfere with the rest of the system.

* Example of script, assumed to be located in the root directory of Quantum++:

```
#!/bin/sh

MATLAB=/Applications/MATLAB_R2015b.app
export DYLD_LIBRARY_PATH=$DYLD_LIBRARY_PATH:$MATLAB/bin/maci64

./build/qpp
```

- If you build a debug version with `g++` under OS X and use `gdb` to step inside template functions you may want to add `-fno-weak` compiler flag. See <http://stackoverflow.com/questions/23330641/gnu-gdb-can-not-step-into-template-functions-os-x-mavericks> for more details about this problem.

Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp	Quantum++ main namespace	13
qpp::experimental	Experimental/test functions/classes, do not use or modify	80
qpp::internal	Internal utility functions, do not use/modify	80
qpp::internal::__details		83

Chapter 3

Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::internal::_details::_Display_Impl	85
qpp::internal::IOManipEigen	101
std::exception	
qpp::Exception	88
false_type	
qpp::is_complex< T >	107
qpp::is_iterable< T, typename >	109
qpp::is_matrix_expression< Derived >	111
qpp::IDisplay	97
qpp::internal::IOManipEigen	101
qpp::internal::IOManipPointer< PointerType >	103
qpp::internal::IOManipRange< InputIterator >	105
qpp::Timer< T, CLOCK_T >	121
qpp::internal::Singleton< T >	115
qpp::internal::Singleton< const Codes >	115
qpp::Codes	85
qpp::internal::Singleton< const Gates >	115
qpp::Gates	91
qpp::internal::Singleton< const Init >	115
qpp::Init	100
qpp::internal::Singleton< const States >	115
qpp::States	116
qpp::internal::Singleton< RandomDevices >	115
qpp::RandomDevices	113
true_type	
qpp::is_complex< std::complex< T > >	108
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >	110
qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >	112

Chapter 4

Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

qpp::internal::_details::_Display_Impl	85
qpp::Codes	
Const Singleton class that defines quantum error correcting codes	85
qpp::Exception	
Generates custom exceptions, used when validating function parameters	88
qpp::Gates	
Const Singleton class that implements most commonly used gates	91
qpp::IDisplay	
Abstract class (interface) that mandates the definition of virtual std::ostream& <code>display(std::ostream& os) const</code>	97
qpp::Init	
Const Singleton class that performs additional initializations/cleanups	100
qpp::internal::IOManipEigen	
qpp::internal::IOManipPointer< PointerType >	
qpp::internal::IOManipRange< InputIterator >	
qpp::is_complex< T >	
Checks whether the type is a complex type	107
qpp::is_complex< std::complex< T > >	
Checks whether the type is a complex number type, specialization for complex types	108
qpp::is_iterable< T, typename >	
Checks whether <i>T</i> is compatible with an STL-like iterable container	109
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >	
Checks whether <i>T</i> is compatible with an STL-like iterable container, specialization for STL-like iterable containers	110
qpp::is_matrix_expression< Derived >	
Checks whether the type is an Eigen matrix expression	111
qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >	
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions	112
qpp::RandomDevices	
Singleton class that manages the source of randomness in the library	113
qpp::internal::Singleton< T >	
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)	115
qpp::States	
Const Singleton class that implements most commonly used states	116

qpp::Timer< T, CLOCK_T >	
Chronometer	121

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

<code>constants.h</code>		
Constants	130
<code>entanglement.h</code>		
Entanglement functions	131
<code>entropies.h</code>		
Entropy functions	132
<code>functions.h</code>		
Generic quantum computing functions	134
<code>input_output.h</code>		
Input/output functions	138
<code>instruments.h</code>		
Measurement functions	139
<code>macros.h</code>		
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<code>number_theory.h</code>		
Number theory functions	146
<code>operations.h</code>		
Quantum operation functions	147
<code>qpp.h</code>		
Quantum++ main header file, includes all other necessary headers	149
<code>random.h</code>		
Randomness-related functions	151
<code>statistics.h</code>		
Statistics functions	152
<code>traits.h</code>		
Type traits	153
<code>types.h</code>		
Type aliases	154
<code>classes/codes.h</code>		
Quantum error correcting codes	125
<code>classes/exception.h</code>		
Exceptions	125
<code>classes/gates.h</code>		
Quantum gates	126
<code>classes/display.h</code>		
Display interface via the non-virtual interface (NVI)	127
<code>classes/init.h</code>		
Initialization	128

classes/random_devices.h	128
Random devices	
classes/states.h	129
Quantum states	
classes/timer.h	130
Timing	
experimental/experimental.h	134
Experimental/test functions/classes	
internal/util.h	143
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internal/classes/iomanip.h	141
Input/output manipulators	
internal/classes/singleton.h	142
Singleton pattern via CRTP	
MATLAB/matlab.h	145
Input/output interfacing with MATLAB	

Chapter 6

Namespace Documentation

6.1 qpp Namespace Reference

Quantum++ main namespace.

Namespaces

- [experimental](#)
Experimental/test functions/classes, do not use or modify.
- [internal](#)
Internal utility functions, do not use/modify.

Classes

- class [Codes](#)
const Singleton class that defines quantum error correcting codes
- class [Exception](#)
Generates custom exceptions, used when validating function parameters.
- class [Gates](#)
const Singleton class that implements most commonly used gates
- class [IDisplay](#)
Abstract class (interface) that mandates the definition of virtual std::ostream& [display\(std::ostream& os\) const](#).
- class [Init](#)
const Singleton class that performs additional initializations/cleanups
- struct [is_complex](#)
Checks whether the type is a complex type.
- struct [is_complex< std::complex< T > >](#)
Checks whether the type is a complex number type, specialization for complex types.
- struct [is_iterable](#)
Checks whether T is compatible with an STL-like iterable container.
- struct [is_iterable< T, to_void< decltype\(std::declval< T >\(\).begin\(\)\), decltype\(std::declval< T >\(\).end\(\)\), typename T::value_type > >](#)
Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct [is_matrix_expression](#)
Checks whether the type is an Eigen matrix expression.
- struct [is_matrix_expression< typename Eigen::MatrixBase< Derived > >](#)
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

- class **RandomDevices**
Singeleton class that manages the source of randomness in the library.
- class **States**
const Singleton class that implements most commonly used states
- class **Timer**
Chronometer.

Typedefs

- template<typename... >
 using **to_void** = void
Alias template that implements the proposal for void_t.
- using **idx** = std::size_t
Non-negative integer index.
- using **bigint** = long long int
Big integer.
- using **ubigint** = unsigned long long int
Non-negative big integer.
- using **cplx** = std::complex< double >
Complex number in double precision.
- using **ket** = Eigen::VectorXcd
Complex (double precision) dynamic Eigen column vector.
- using **bra** = Eigen::RowVectorXcd
Complex (double precision) dynamic Eigen row vector.
- using **cmat** = Eigen::MatrixXcd
Complex (double precision) dynamic Eigen matrix.
- using **dmat** = Eigen::MatrixXd
Real (double precision) dynamic Eigen matrix.
- template<typename Scalar >
 using **dyn_mat** = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >
Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar >
 using **dyn_col_vect** = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >
Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar >
 using **dyn_row_vect** = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >
Dynamic Eigen row vector over the field specified by Scalar.

Functions

- constexpr **cplx operator""_i** (unsigned long long int x) noexcept
User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr **cplx operator""_i** (long double x) noexcept
User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- **cplx omega** (**idx** D)
D-th root of unity.
- template<typename Derived >
dyn_col_vect< double > **schmidtcoeffs** (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)
Schmidt coefficients of the bi-partite pure state A.

- template<typename Derived>

cmat schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)

Schmidt basis on Alice side.
- template<typename Derived>

cmat schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)

Schmidt basis on Bob side.
- template<typename Derived>

std::vector< double > **schmidtprobs** (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)

Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived>

double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)

Entanglement of the bi-partite pure state A.
- template<typename Derived>

double gconcurrence (const Eigen::MatrixBase< Derived > &A)

G-concurrence of the bi-partite pure state A.
- template<typename Derived>

double negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)

Negativity of the bi-partite mixed state A.
- template<typename Derived>

double lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &dims)

Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived>

double concurrence (const Eigen::MatrixBase< Derived > &A)

Wootters concurrence of the bi-partite qubit mixed state A.
- template<typename Derived>

double entropy (const Eigen::MatrixBase< Derived > &A)

von-Neumann entropy of the density matrix A
- **double entropy** (const std::vector< double > &prob)

Shannon entropy of the probability distribution prob.
- template<typename Derived>

double renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- **double renyi** (const std::vector< double > &prob, double alpha)

Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template<typename Derived>

double tsallis (const Eigen::MatrixBase< Derived > &A, double q)

Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- **double tsallis** (const std::vector< double > &prob, double q)

Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template<typename Derived>

double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &subsysA, const std::vector< **idx** > &subsysB, const std::vector< **idx** > &dims)

Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived>

double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< **idx** > &subsysA, const std::vector< **idx** > &subsysB, **idx** d=2)

Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived>

dyn_mat< typename Derived::Scalar > **transpose** (const Eigen::MatrixBase< Derived > &A)

Transpose.
- template<typename Derived>

dyn_mat< typename Derived::Scalar > **conjugate** (const Eigen::MatrixBase< Derived > &A)

Complex conjugate.

- template<typename Derived>
`dyn_mat< typename Derived::Scalar > adjoint` (const Eigen::MatrixBase< Derived > &A)

Adjoint.

- template<typename Derived>
`dyn_mat< typename Derived::Scalar > inverse` (const Eigen::MatrixBase< Derived > &A)

Inverse.

- template<typename Derived>
`Derived::Scalar trace` (const Eigen::MatrixBase< Derived > &A)

Trace.

- template<typename Derived>
`Derived::Scalar det` (const Eigen::MatrixBase< Derived > &A)

Determinant.

- template<typename Derived>
`Derived::Scalar logdet` (const Eigen::MatrixBase< Derived > &A)

Logarithm of the determinant.

- template<typename Derived>
`Derived::Scalar sum` (const Eigen::MatrixBase< Derived > &A)

Element-wise sum of A.

- template<typename Derived>
`Derived::Scalar prod` (const Eigen::MatrixBase< Derived > &A)

Element-wise product of A.

- template<typename Derived>
`double norm` (const Eigen::MatrixBase< Derived > &A)

Frobenius norm.

- template<typename Derived>
`std::pair< dyn_col_vect< cplx >, cmat > eig` (const Eigen::MatrixBase< Derived > &A)

Full eigen decomposition.

- template<typename Derived>
`dyn_col_vect< cplx > evals` (const Eigen::MatrixBase< Derived > &A)

Eigenvalues.

- template<typename Derived>
`cmat evecs` (const Eigen::MatrixBase< Derived > &A)

Eigenvectors.

- template<typename Derived>
`std::pair< dyn_col_vect< double >, cmat > heig` (const Eigen::MatrixBase< Derived > &A)

Full eigen decomposition of Hermitian expression.

- template<typename Derived>
`dyn_col_vect< double > hevals` (const Eigen::MatrixBase< Derived > &A)

Hermitian eigenvalues.

- template<typename Derived>
`cmat hevects` (const Eigen::MatrixBase< Derived > &A)

Hermitian eigenvectors.

- template<typename Derived>
`std::tuple< cmat, dyn_col_vect< double >, cmat > svd` (const Eigen::MatrixBase< Derived > &A)

Full singular value decomposition.

- template<typename Derived>
`dyn_col_vect< double > svals` (const Eigen::MatrixBase< Derived > &A)

Singular values.

- template<typename Derived>
`cmat svdU` (const Eigen::MatrixBase< Derived > &A)

Left singular vectors.

- template<typename Derived>

cmat svdV (const Eigen::MatrixBase< Derived > &A)

Right singular vectors.
- template<typename Derived>

cmat funm (const Eigen::MatrixBase< Derived > &A, **cplx**(*f)(const **cplx** &))

Functional calculus f(A)
- template<typename Derived>

cmat sqrtm (const Eigen::MatrixBase< Derived > &A)

Matrix square root.
- template<typename Derived>

cmat absm (const Eigen::MatrixBase< Derived > &A)

Matrix absolut value.
- template<typename Derived>

cmat expm (const Eigen::MatrixBase< Derived > &A)

Matrix exponential.
- template<typename Derived>

cmat logm (const Eigen::MatrixBase< Derived > &A)

Matrix logarithm.
- template<typename Derived>

cmat sinm (const Eigen::MatrixBase< Derived > &A)

Matrix sin.
- template<typename Derived>

cmat cosm (const Eigen::MatrixBase< Derived > &A)

Matrix cos.
- template<typename Derived>

cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const **cplx** z)

Matrix power.
- template<typename Derived>

dyn_mat< typename Derived::Scalar > **powm** (const Eigen::MatrixBase< Derived > &A, **idx** n)

Matrix power.
- template<typename Derived>

double schatten (const Eigen::MatrixBase< Derived > &A, double p)

Schatten matrix norm.
- template<typename OutputScalar , typename Derived>

dyn_mat< OutputScalar > **cwise** (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename Derived::Scalar &))

Functor.
- template<typename T >

dyn_mat< typename T::Scalar > **kron** (const T &head)

Kronecker product.
- template<typename T , typename... Args>

dyn_mat< typename T::Scalar > **kron** (const T &head, const Args &...tail)

Kronecker product.
- template<typename Derived >

dyn_mat< typename Derived::Scalar > **kron** (const std::vector< Derived > &As)

Kronecker product.
- template<typename Derived >

dyn_mat< typename Derived::Scalar > **kron** (const std::initializer_list< Derived > &As)

Kronecker product.
- template<typename Derived >

dyn_mat< typename Derived::Scalar > **kronpow** (const Eigen::MatrixBase< Derived > &A, **idx** n)

Kronecker power.

- template<typename T >
`dyn_mat< typename T::Scalar > dirsum` (const T &head)
Direct sum.
- template<typename T , typename... Args>
`dyn_mat< typename T::Scalar > dirsum` (const T &head, const Args &...tail)
Direct sum.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > dirsum` (const std::vector< Derived > &As)
Direct sum.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > dirsum` (const std::initializer_list< Derived > &As)
Direct sum.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > dirsumpow` (const Eigen::MatrixBase< Derived > &A, `idx` n)
Direct sum power.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > reshape` (const Eigen::MatrixBase< Derived > &A, `idx` rows, `idx` cols)
Reshape.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > comm` (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
Commutator.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > anticommm` (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
Anti-commutator.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > prj` (const Eigen::MatrixBase< Derived > &V)
Projector.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > grams` (const std::vector< Derived > &Vs)
Gram-Schmidt orthogonalization.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > grams` (const std::initializer_list< Derived > &Vs)
Gram-Schmidt orthogonalization.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > grams` (const Eigen::MatrixBase< Derived > &A)
Gram-Schmidt orthogonalization.
- std::vector< `idx` > `n2multiidx` (`idx` n, const std::vector< `idx` > &dims)
Non-negative integer index to multi-index.
- `idx multiidx2n` (const std::vector< `idx` > &midx, const std::vector< `idx` > &dims)
Multi-index to non-negative integer index.
- `ket mket` (const std::vector< `idx` > &mask, const std::vector< `idx` > &dims)
Multi-partite qudit ket.
- `ket mket` (const std::vector< `idx` > &mask, `idx` d=2)
Multi-partite qudit ket.
- `cmat mpqrj` (const std::vector< `idx` > &mask, const std::vector< `idx` > &dims)
Projector onto multi-partite qudit ket.
- `cmat mpqrj` (const std::vector< `idx` > &mask, `idx` d=2)
Projector onto multi-partite qudit ket.
- template<typename InputIterator >
std::vector< double > `abssq` (InputIterator first, InputIterator last)

- template<typename Container >
`std::vector< double > abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)`

Computes the absolute values squared of an STL-like range of complex numbers.
- template<typename Derived >
`std::vector< double > abssq (const Eigen::MatrixBase< Derived > &A)`

Computes the absolute values squared of an STL-like container.
- template<typename InputIterator >
`std::iterator_traits< InputIterator >::value_type sum (InputIterator first, InputIterator last)`

Computes the absolute values squared of an Eigen expression.
- template<typename Container >
`Container::value_type sum (const Container &c)`

Element-wise sum of an STL-like range.
- template<typename InputIterator >
`std::iterator_traits< InputIterator >::value_type prod (InputIterator first, InputIterator last)`

Element-wise product of an STL-like range.
- template<typename Container >
`Container::value_type prod (const Container &c)`

Element-wise product of the elements of an STL-like container.
- template<typename Derived >
`dyn_col_vect< typename Derived::Scalar > rho2pure (const Eigen::MatrixBase< Derived > &A)`

Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- template<typename T >
`std::vector< T > complement (std::vector< T > subsys, idx N)`

Constructs the complement of a subsystem vector.
- template<typename Derived >
`std::vector< double > rho2bloch (const Eigen::MatrixBase< Derived > &A)`

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- `cmat bloch2rho (const std::vector< double > &r)`

Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.
- template<typename Derived >
`internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)`

Eigen expression ostream manipulator.
- `internal::IOManipEigen disp (cplx z, double chop=qpp::chop)`

Complex number ostream manipulator.
- template<typename InputIterator >
`internal::IOManipRange< InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="])`

Range ostream manipulator.
- template<typename Container >
`internal::IOManipRange< typename Container::const_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="])`

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template<typename PointerType >
`internal::IOManipPointer< PointerType > disp (const PointerType *p, idx n, const std::string &separator, const std::string &start="[", const std::string &end="])`

C-style pointer ostream manipulator.
- template<typename Derived >
`void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`

Saves Eigen expression to a binary file (internal format) in double precision.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > load (const std::string &fname)`

- Loads Eigen matrix from a binary file (internal format) in double precision.*
- template<typename Derived>


```
dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)
```

Generalized inner product.
 - template<typename Derived>


```
dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)
```

Generalized inner product.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)
```

Measures the state A using the set of Kraus operators Ks.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)
```

Measures the state A using the set of Kraus operators Ks.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)
```

Measures the state A in the orthonormal basis specified by the unitary matrix U.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)
```

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)
```

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)
```

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)
```

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)
```

Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
 - template<typename Derived>


```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)
```

Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
 - template<typename Derived>


```
std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)
```

Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
 - template<typename Derived>


```
std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)
```

- Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.*
- template<typename Derived>
Derived [loadMATLABmatrix](#) (const std::string &mat_file, const std::string &var_name)
Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.
 - template<>
dmat [loadMATLABmatrix](#) (const std::string &mat_file, const std::string &var_name)
Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
 - template<>
cmat [loadMATLABmatrix](#) (const std::string &mat_file, const std::string &var_name)
Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))
 - template<typename Derived>
void [saveMATLABmatrix](#) (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.
 - template<>
void [saveMATLABmatrix](#) (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
 - template<>
void [saveMATLABmatrix](#) (const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))
 - std::vector< int > [x2contrfrac](#) (double x, **idx** n, **idx** cut=1e5)
Simple continued fraction expansion.
 - double [contrfrac2x](#) (const std::vector< int > &cf, **idx** n)
Real representation of a simple continued fraction.
 - double [contrfrac2x](#) (const std::vector< int > &cf)
Real representation of a simple continued fraction.
 - ubigint [gcd](#) (ubigint m, ubigint n)
Greatest common divisor of two non-negative integers.
 - ubigint [gcd](#) (const std::vector< ubigint > &ns)
Greatest common divisor of a list of non-negative integers.
 - ubigint [lcm](#) (ubigint m, ubigint n)
Least common multiple of two positive integers.
 - ubigint [lcm](#) (const std::vector< ubigint > &ns)
Least common multiple of a list of positive integers.
 - std::vector< **idx** > [invperm](#) (const std::vector< **idx** > &perm)
Inverse permutation.
 - std::vector< **idx** > [compperm](#) (const std::vector< **idx** > &perm, const std::vector< **idx** > &sigma)
Compose permutations.
 - std::vector< ubigint > [factors](#) (ubigint n)
Prime factor decomposition.
 - bool [isprime](#) (ubigint n)
Primality test.
 - ubigint [modpow](#) (ubigint a, ubigint n, ubigint p)
Integer power modulo p.
 - template<typename Derived1, typename Derived2>
dyn_mat< typename Derived1::Scalar > [applyCTRL](#) (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< **idx** > &ctrl, const std::vector< **idx** > &subsys, const std::vector< **idx** > &dims)
Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > applyCTRL` (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< `idx` > &ctrl, const std::vector< `idx` > &subsys, `idx d=2`)
Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > apply` (const Eigen::MatrixBase< Derived1 > &state, const Eigen< ->::MatrixBase< Derived2 > &A, const std::vector< `idx` > &subsys, const std::vector< `idx` > &dims)
Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > apply` (const Eigen::MatrixBase< Derived1 > &state, const Eigen< ->::MatrixBase< Derived2 > &A, const std::vector< `idx` > &subsys, `idx d=2`)
Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived >
`cmat apply` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks)
Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.
- template<typename Derived >
`cmat apply` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks, const std::vector< `idx` > &subsys, const std::vector< `idx` > &dims)
Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- template<typename Derived >
`cmat apply` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks, const std::vector< `idx` > &subsys, `idx d=2`)
Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- `cmat kraus2super` (const std::vector< `cmat` > &Ks)
Superoperator matrix.
- `cmat kraus2choi` (const std::vector< `cmat` > &Ks)
Choi matrix.
- `std::vector< cmat > choi2kraus` (const `cmat` &A)
Orthogonal Kraus operators from Choi matrix.
- `cmat choi2super` (const `cmat` &A)
Converts Choi matrix to superoperator matrix.
- `cmat super2choi` (const `cmat` &A)
Converts superoperator matrix to Choi matrix.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > ptrace1` (const Eigen::MatrixBase< Derived > &A, const std< ->::vector< `idx` > &dims)
Partial trace.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > ptrace2` (const Eigen::MatrixBase< Derived > &A, const std< ->::vector< `idx` > &dims)
Partial trace.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > ptrace` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsys, const std::vector< `idx` > &dims)
Partial trace.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > ptrace` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsys, `idx d=2`)
Partial trace.

- template<typename Derived>

`dyn_mat< typename Derived::Scalar > ptranspose` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Partial transpose.
- template<typename Derived>

`dyn_mat< typename Derived::Scalar > ptranspose` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

Partial transpose.
- template<typename Derived>

`dyn_mat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)

Subsystem permutation.
- template<typename Derived>

`dyn_mat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)

Subsystem permutation.
- double `rand` (double a=0, double b=1)

Generates a random real number uniformly distributed in the interval [a, b]
- bigint `rand` (bigint a=std::numeric_limits< bigint >::min(), bigint b=std::numeric_limits< bigint >::max())

Generates a random big integer uniformly distributed in the interval [a, b].
- ubigint `rand` (ubigint a=std::numeric_limits< ubigint >::min(), ubigint b=std::numeric_limits< ubigint >::max())

Generates a random non-negative big integer uniformly distributed in the interval [a, b].
- idx `randidx` (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

Generates a random index (idx) uniformly distributed in the interval [a, b].
- template<typename Derived>

Derived `rand` (idx rows, idx cols, double a=0, double b=1)

Generates a random matrix with entries uniformly distributed in the interval [a, b]
- template<>

`dmat rand` (idx rows, idx cols, double a, double b)

Generates a random real matrix with entries uniformly distributed in the interval [a, b], specialization for double matrices (`qpp::dmat`)
- template<>

`cmat rand` (idx rows, idx cols, double a, double b)

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b], specialization for complex matrices (`qpp::cmat`)
- template<typename Derived>

Derived `randn` (idx rows, idx cols, double mean=0, double sigma=1)

Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>

`dmat randn` (idx rows, idx cols, double mean, double sigma)

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (`qpp::dmat`)
- template<>

`cmat randn` (idx rows, idx cols, double mean, double sigma)

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (`qpp::cmat`)
- double `randn` (double mean=0, double sigma=1)

Generates a random real number (double) normally distributed in N(mean, sigma)
- `cmat randU` (idx D)

Generates a random unitary matrix.
- `cmat randV` (idx Din, idx Dout)

Generates a random isometry matrix.

- `std::vector< cmat > randkraus (idx N, idx D)`
Generates a set of random Kraus operators.
- `cmat randH (idx D)`
Generates a random Hermitian matrix.
- `ket randket (idx D)`
Generates a random normalized ket (pure state vector)
- `cmat randrho (idx D)`
Generates a random density matrix.
- `std::vector< idx > randperm (idx n)`
Generates a random uniformly distributed permutation.
- `std::vector< double > uniform (idx N)`
Uniform probability distribution vector.
- `std::vector< double > marginalX (const dmat &probXY)`
Marginal distribution.
- `std::vector< double > marginalY (const dmat &probXY)`
Marginal distribution.
- template<typename Container >
`double avg (const std::vector< double > &prob, const Container &X)`
Average.
- template<typename Container >
`double cov (const dmat &probXY, const Container &X, const Container &Y)`
Covariance.
- template<typename Container >
`double var (const std::vector< double > &prob, const Container &X)`
Variance.
- template<typename Container >
`double sigma (const std::vector< double > &prob, const Container &X)`
Standard deviation.
- template<typename Container >
`double cor (const dmat &probXY, const Container &X, const Container &Y)`
Correlation.

Variables

- `constexpr double chop = 1e-10`
Used in `qpp::disp()` for setting to zero numbers that have their absolute value smaller than `qpp::chop`.
- `constexpr double eps = 1e-12`
Used to decide whether a number or expression in double precision is zero or not.
- `constexpr idx maxn = 64`
Maximum number of allowed qu(d)its (subsystems)
- `constexpr double pi = 3.141592653589793238462643383279502884`
 π
- `constexpr double ee = 2.718281828459045235360287471352662497`
Base of natural logarithm, e.
- `constexpr double infty = std::numeric_limits<double>::infinity()`
Used to denote infinity in double precision.

6.1.1 Detailed Description

Quantum++ main namespace.

6.1.2 Typedef Documentation

6.1.2.1 using qpp::bigint = `typedef long long int`

Big integer.

6.1.2.2 using qpp::bra = `typedef Eigen::RowVectorXcd`

Complex (double precision) dynamic Eigen row vector.

6.1.2.3 using qpp::cmat = `typedef Eigen::MatrixXcd`

Complex (double precision) dynamic Eigen matrix.

6.1.2.4 using qpp::cplx = `typedef std::complex<double>`

Complex number in double precision.

6.1.2.5 using qpp::dmat = `typedef Eigen::MatrixXd`

Real (double precision) dynamic Eigen matrix.

6.1.2.6 template<typename Scalar > using qpp::dyn_col_vect = `typedef Eigen::Matrix<Scalar, Eigen::Dynamic, 1>`

Dynamic Eigen column vector over the field specified by *Scalar*.

Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
auto colvect = dyn_col_vect<float>(2);
```

6.1.2.7 template<typename Scalar > using qpp::dyn_mat = `typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>`

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
auto mat = dyn_mat<float>(2, 3);
```

6.1.2.8 template<typename Scalar > using qpp::dyn_row_vect = `typedef Eigen::Matrix<Scalar, 1, Eigen::Dynamic>`

Dynamic Eigen row vector over the field specified by *Scalar*.

Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
auto rowvect = dyn_row_vect<float>(3);
```

6.1.2.9 using qpp::idx = `typedef std::size_t`

Non-negative integer index.

6.1.2.10 using qpp::ket = `typedef Eigen::VectorXcd`

Complex (double precision) dynamic Eigen column vector.

6.1.2.11 template<typename... > using qpp::to_void = `typedef void`

Alias template that implements the proposal for `void_t`.

See also

<http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911>

6.1.2.12 using qpp::ubigint = `typedef unsigned long long int`

Non-negative big integer.

6.1.3 Function Documentation

6.1.3.1 template<typename Derived > cmat qpp::absm (const Eigen::MatrixBase< Derived > & A)

Matrix absolut value.

Parameters

A	Eigen expression
---	------------------

Returns

Matrix absolut value of A

6.1.3.2 template<typename InputIterator > std::vector<double> qpp::abssq (InputIterator *first*, InputIterator *last*)

Computes the absolute values squared of an STL-like range of complex numbers.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

Returns

Real vector consisting of the range absolut values squared

6.1.3.3 template<typename Container > std::vector<double> qpp::abssq (const Container & c, typename std::enable_if< is_iterable< Container >::value >::type * = nullptr)

Computes the absolute values squared of an STL-like container.

Parameters

c	STL-like container
---	--------------------

Returns

Real vector consisting of the container's absolut values squared

6.1.3.4 template<typename Derived > std::vector<double> qpp::abssq (const Eigen::MatrixBase< Derived > & A)

Computes the absolute values squared of an Eigen expression.

Parameters

A	Eigen expression
---	------------------

Returns

Real vector consisting of the absolute values squared

6.1.3.5 template<typename Derived> **dyn_mat<typename Derived::Scalar> qpp::adjoint** (const Eigen::MatrixBase<Derived> & A)

Adjoint.

Parameters

A	Eigen expression
---	------------------

Returns

Adjoint (Hermitian conjugate) of A, as a dynamic matrix over the same scalar field as A

6.1.3.6 template<typename Derived1, typename Derived2> **dyn_mat<typename Derived1::Scalar> qpp::anticomm** (const Eigen::MatrixBase<Derived1> & A, const Eigen::MatrixBase<Derived2> & B)

Anti-commutator.

See also

[qpp::comm\(\)](#)

Anti-commutator $\{A, B\} = AB + BA$. Both A and B must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Anti-commutator $AB + BA$, as a dynamic matrix over the same scalar field as A

6.1.3.7 template<typename Derived1, typename Derived2> **dyn_mat<typename Derived1::Scalar> qpp::apply** (const Eigen::MatrixBase<Derived1> & state, const Eigen::MatrixBase<Derived2> & A, const std::vector<idx> & subsys, const std::vector<idx> & dims)

Applies the gate A to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate A must match the dimension of *subsys*

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.8 template<typename Derived1 , typename Derived2 > **dyn_mat<typename Derived1::Scalar> qpp::apply (const Eigen::MatrixBase< Derived1 > & *state*, const Eigen::MatrixBase< Derived2 > & *A*, const std::vector< idx > & *subsys*, idx *d* = 2)**

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>d</i>	Subsystem dimensions

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.9 template<typename Derived > **cmat qpp::apply (const Eigen::MatrixBase< Derived > & *rho*, const std::vector< cmat > & *Ks*)**

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *rho*.

Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators

Returns

Output density matrix after the action of the channel

6.1.3.10 template<typename Derived > **cmat qpp::apply (const Eigen::MatrixBase< Derived > & *rho*, const std::vector< cmat > & *Ks*, const std::vector< idx > & *subsys*, const std::vector< idx > & *dims*)**

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *rho*.

Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes where the Kraus operators <i>Ks</i> are applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

Output density matrix after the action of the channel

6.1.3.11 template<typename Derived > cmat qpp::apply (const Eigen::MatrixBase< Derived > & *rho*, const std::vector< cmat > & *Ks*, const std::vector< idx > & *subsys*, idx *d* = 2)

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *rho*.

Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes where the Kraus operators <i>Ks</i> are applied
<i>d</i>	Subsystem dimensions

Returns

Output density matrix after the action of the channel

6.1.3.12 template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > & *state*, const Eigen::MatrixBase< Derived2 > & *A*, const std::vector< idx > & *ctrl*, const std::vector< idx > & *subsys*, const std::vector< idx > & *dims*)

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

[qpp::Gates::CTRL\(\)](#)

Note

The dimension of the gate *A* must match the dimension of *subsys*. Also, all control subsystems in *ctrl* must have the same dimension.

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

CTRL-A gate applied to the part *subsys* of *state*

```
6.1.3.13 template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
    const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< idx >
    & ctrl, const std::vector< idx > & subsys, idx d = 2 )
```

Applies the controlled-gate A to the part $subsys$ of the multi-partite state vector or density matrix $state$.

See also

[qpp::Gates::CTRL\(\)](#)

Note

The dimension of the gate A must match the dimension of $subsys$

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate A is applied
<i>d</i>	Subsystem dimensions

Returns

CTRL-A gate applied to the part $subsys$ of $state$

```
6.1.3.14 template<typename Container > double qpp::avg ( const std::vector< double > & prob, const Container & X )
```

Average.

Parameters

<i>prob</i>	Real probability vector representing the probability distribution of X
<i>X</i>	Random variable values represented by an STL-like container

Returns

Average of X

```
6.1.3.15 cmat qpp::bloch2rho ( const std::vector< double > & r ) [inline]
```

Computes the density matrix corresponding to the 3-dimensional real Bloch vector r .

See also

[qpp::rho2bloch\(\)](#)

Parameters

<i>r</i>	3-dimensional real vector
----------	---------------------------

Returns

Qubit density matrix

6.1.3.16 std::vector<cmat> qpp::choi2kraus (const cmat & A) [inline]

Orthogonal Kraus operators from Choi matrix.

See also

[qpp::kraus2choi\(\)](#)

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix A

Note

The Kraus operators satisfy $\text{Tr}(K_i^\dagger K_j) = \delta_{ij}$ for all $i \neq j$

Parameters

A	Choi matrix
---	-------------

Returns

Set of orthogonal Kraus operators

6.1.3.17 cmat qpp::choi2super (const cmat & A) [inline]

Converts Choi matrix to superoperator matrix.

See also

[qpp::super2choi\(\)](#)

Parameters

A	Choi matrix
---	-------------

Returns

Superoperator matrix

6.1.3.18 template<typename Derived1, typename Derived2> dyn_mat<typename Derived1::Scalar> qpp::comm (const Eigen::MatrixBase<Derived1> & A, const Eigen::MatrixBase<Derived2> & B)

Commutator.

See also

[qpp::anticomm\(\)](#)

Commutator $[A, B] = AB - BA$. Both A and B must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Commutator $AB - BA$, as a dynamic matrix over the same scalar field as A

6.1.3.19 template<typename T> std::vector<T> qpp::complement (std::vector<T> subsys, idx N)

Constructs the complement of a subsystem vector.

Parameters

<i>subsys</i>	Subsystem vector
<i>N</i>	Total number of systems

Returns

The complement of *subsys* with respect to the set $\{0, 1, \dots, N - 1\}$

6.1.3.20 `std::vector<idx> qpp::compperm (const std::vector< idx > & perm, const std::vector< idx > & sigma) [inline]`

Compose permutations.

Parameters

<i>perm</i>	Permutation
<i>sigma</i>	Permutation

Returns

Composition of the permutations $perm \circ sigma = perm(sigma)$

6.1.3.21 `template<typename Derived > double qpp::concurrence (const Eigen::MatrixBase< Derived > & A)`

Wootters concurrence of the bi-partite qubit mixed state *A*.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Wootters concurrence

6.1.3.22 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::conjugate (const Eigen::MatrixBase< Derived > & A)`

Complex conjugate.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.23 `double qpp::contfrac2x (const std::vector< int > & cf, idx n) [inline]`

Real representation of a simple continued fraction.

See also

[qpp::x2contfrac\(\)](#)

Parameters

<i>cf</i>	Integer vector containing the simple continued fraction expansion
<i>n</i>	Number of terms considered in the continued fraction expansion. If <i>n</i> is greater than the size of <i>cf</i> , then all terms in <i>cf</i> are considered.

Returns

Real representation of the simple continued fraction

6.1.3.24 double qpp::contfrac2x (const std::vector< int > & *cf*) [inline]

Real representation of a simple continued fraction.

See also

[qpp::x2contfrac\(\)](#)

Parameters

<i>cf</i>	Integer vector containing the simple continued fraction expansion
-----------	-------------------------------------------------------------------

Returns

Real representation of the simple continued fraction

6.1.3.25 template<typename Container > double qpp::cor (const dmat & *probXY*, const Container & *X*, const Container & *Y*)

Correlation.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of <i>X</i> and <i>Y</i> in lexicographical order (<i>X</i> labels the rows, <i>Y</i> labels the columns)
<i>X</i>	Random variable values represented by an STL-like container
<i>Y</i>	Random variable values represented by an STL-like container

Returns

Correlation of *X* and *Y*

6.1.3.26 template<typename Derived > cmat qpp::cosm (const Eigen::MatrixBase< Derived > & *A*)

Matrix cos.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Matrix cosine of *A*

6.1.3.27 template<typename Container > double qpp::cov (const dmat & *probXY*, const Container & *X*, const Container & *Y*)

Covariance.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
X	Random variable values represented by an STL-like container
Y	Random variable values represented by an STL-like container

Returns

Covariance of X and Y

6.1.3.28 `template<typename OutputScalar , typename Derived > dyn_mat<OutputScalar> qpp::cwise (const Eigen::MatrixBase< Derived > & A, OutputScalar(*)(const typename Derived::Scalar &) f)`

Functor.

Parameters

<i>A</i>	Eigen expression
<i>f</i>	Pointer-to-function from scalars of <i>A</i> to <i>OutputScalar</i>

Returns

Component-wise $f(A)$, as a dynamic matrix over the *OutputScalar* scalar field

6.1.3.29 `template<typename Derived > Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > & A)`

Determinant.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Determinant of *A*, as a scalar over the same scalar field as *A*. Returns $\pm\infty$ when the determinant overflows/underflows.

6.1.3.30 `template<typename T > dyn_mat<typename T::Scalar> qpp::dirsum (const T & head)`

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Used to stop the recursion for the variadic template version of [qpp::dirsum\(\)](#)

Parameters

<i>head</i>	Eigen expression
-------------	------------------

Returns

Its argument *head*

6.1.3.31 template<typename T , typename... Args> **dyn_mat<typename T::Scalar> qpp::dirsum (const T & *head*, const Args &... *tail*)**

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Parameters

<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)

Returns

Direct sum of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.32 template<typename Derived > **dyn_mat<typename Derived::Scalar> qpp::dirsum (const std::vector< Derived > & *As*)**

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Parameters

<i>As</i>	std::vector of Eigen expressions
-----------	----------------------------------

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.33 template<typename Derived > **dyn_mat<typename Derived::Scalar> qpp::dirsum (const std::initializer_list< Derived > & *As*)**

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Parameters

<i>As</i>	std::initializer_list of Eigen expressions, such as {A1, A2, ... ,Ak}
-----------	-----------------------------------------------------------------------

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.34 template<typename Derived> **dyn_mat<typename Derived::Scalar> qpp::dirsumpow (const Eigen::MatrixBase<Derived> & A, idx n)**

Direct sum power.

See also

[qpp::dirsum\(\)](#)

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Direct sum of A with itself n times $A^{\oplus n}$, as a dynamic matrix over the same scalar field as A

6.1.3.35 template<typename Derived> **internal::IOManipEigen qpp::disp (const Eigen::MatrixBase<Derived> & A, double chop = qpp::chop)**

Eigen expression ostream manipulator.

Parameters

A	Eigen expression
chop	Set to zero the elements smaller in absolute value than <i>chop</i>

Returns

Instance of `qpp::internal::internal::IOManipEigen`

6.1.3.36 **internal::IOManipEigen qpp::disp (cplx z, double chop = qpp::chop) [inline]**

Complex number ostream manipulator.

Parameters

z	Complex number (or any other type implicitly cast-able to <code>std::complex<double></code>)
chop	Set to zero the elements smaller in absolute value than <i>chop</i>

Returns

Instance of `qpp::internal::internal::IOManipEigen`

6.1.3.37 template<typename InputIterator> **internal::IOManipRange<InputIterator> qpp::disp (InputIterator first, InputIterator last, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")**

Range ostream manipulator.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

Returns

Instance of `qpp::internal::internal::IOManipRange`

6.1.3.38 `template<typename Container > internal::IOManipRange<typename Container::const_iterator> qpp::disp (const Container & c, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")`

Standard container ostream manipulator. The container must support `std::begin()`, `std::end()` and forward iteration.

Parameters

<i>c</i>	Container
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

Returns

Instance of `qpp::internal::internal::IOManipRange`

6.1.3.39 `template<typename PointerType > internal::IOManipPointer<PointerType> qpp::disp (const PointerType * p, idx n, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")`

C-style pointer ostream manipulator.

Parameters

<i>p</i>	Pointer to the first element
<i>n</i>	Number of elements to be displayed
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

Returns

Instance of `qpp::internal::internal::IOManipPointer`

6.1.3.40 `template<typename Derived > std::pair<dyn_col_vect < cplx>, cmat> qpp::eig (const Eigen::MatrixBase<Derived > & A)`

Full eigen decomposition.

See also

[qpp::heig\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

Pair of: 1. Eigenvalues of A , as a complex dynamic column vector, and 2. Eigenvectors of A , as columns of a complex dynamic matrix

6.1.3.41 template<typename Derived> double qpp::entanglement (const Eigen::MatrixBase<Derived> & A, const std::vector<idx> & dims)

Entanglement of the bi-partite pure state A .

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

[qpp::entropy\(\)](#)

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Entanglement, with the logarithm in base 2

6.1.3.42 template<typename Derived> double qpp::entropy (const Eigen::MatrixBase<Derived> & A)

von-Neumann entropy of the density matrix A

Parameters

A	Eigen expression
---	------------------

Returns

von-Neumann entropy, with the logarithm in base 2

6.1.3.43 double qpp::entropy (const std::vector<double> & prob) [inline]

Shannon entropy of the probability distribution $prob$.

Parameters

prob	Real probability vector
------	-------------------------

Returns

Shannon entropy, with the logarithm in base 2

6.1.3.44 template<typename Derived> **dyn_col_vect<cplx> qpp::evals (const Eigen::MatrixBase<Derived> & A)**

Eigenvalues.

See also

[qpp::hevals\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

Eigenvalues of A , as a complex dynamic column vector

6.1.3.45 template<typename Derived> **cmat qpp::evecs (const Eigen::MatrixBase<Derived> & A)**

Eigenvectors.

See also

[qpp::hevecs\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

Eigenvectors of A , as columns of a complex dynamic matrix

6.1.3.46 template<typename Derived> **cmat qpp::expm (const Eigen::MatrixBase<Derived> & A)**

Matrix exponential.

Parameters

A	Eigen expression
---	------------------

Returns

Matrix exponential of A

6.1.3.47 std::vector<ubigint> **qpp::factors (ubigint n) [inline]**

Prime factor decomposition.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

<i>n</i>	Integer strictly greater than 1
----------	---------------------------------

Returns

Integer vector containing the factors

6.1.3.48 `template<typename Derived> cmat qpp::funm (const Eigen::MatrixBase< Derived > & A, cplx(*)<const cplx &> f)`

Functional calculus $f(A)$

Parameters

<i>A</i>	Eigen expression
<i>f</i>	Pointer-to-function from complex to complex

Returns

$f(A)$

6.1.3.49 `ubigint qpp::gcd (ubigint m, ubigint n) [inline]`

Greatest common divisor of two non-negative integers.

See also

[qpp::lcm\(\)](#)

Parameters

<i>m</i>	Non-negative integer
<i>n</i>	Non-negative integer

Returns

Greatest common divisor of *m* and *n*

6.1.3.50 `ubigint qpp::gcd (const std::vector< ubigint > & ns) [inline]`

Greatest common divisor of a list of non-negative integers.

See also

[qpp::lcm\(\)](#)

Parameters

<i>ns</i>	List of non-negative integers
-----------	-------------------------------

Returns

Greatest common divisor of all numbers in *ns*

6.1.3.51 template<typename Derived > double qpp::gconcurrence (const Eigen::MatrixBase< Derived > & A)

G-concurrence of the bi-partite pure state A.

Note

Both local dimensions must be equal

Uses [qpp::logdet\(\)](#) to avoid overflows

See also

[qpp::logdet\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

G-concurrence

6.1.3.52 template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::grams (const std::vector< Derived > & Vs)

Gram-Schmidt orthogonalization.

Parameters

Vs	std::vector of Eigen expressions as column vectors
----	----------------------------------------------------

Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.53 template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::grams (const std::initializer_list< Derived > & Vs)

Gram-Schmidt orthogonalization.

Parameters

Vs	std::initializer_list of Eigen expressions as column vectors
----	--------------------------------------------------------------

Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.54 template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::grams (const Eigen::MatrixBase< Derived > & A)

Gram-Schmidt orthogonalization.

Parameters

A	Eigen expression, the input vectors are the columns of A
---	------------------------------------------------------------

Returns

Gram-Schmidt vectors of the columns of A , as columns of a dynamic matrix over the same scalar field as A

6.1.3.55 template<typename Derived > std::pair<dyn_col_vect<double>, cmat> qpp::heig (const Eigen::MatrixBase<Derived> & A)

Full eigen decomposition of Hermitian expression.

See also

[qpp::eig\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

Pair of: 1. Eigenvalues of A , as a real dynamic column vector, and 2. Eigenvectors of A , as columns of a complex dynamic matrix

6.1.3.56 template<typename Derived > dyn_col_vect<double> qpp::hevals (const Eigen::MatrixBase<Derived> & A)

Hermitian eigenvalues.

See also

[qpp::evals\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

Eigenvalues of Hermitian A , as a real dynamic column vector

6.1.3.57 template<typename Derived > cmat qpp::hevects (const Eigen::MatrixBase<Derived> & A)

Hermitian eigenvectors.

See also

[qpp::evects\(\)](#)

Parameters

A	Eigen expression
---	------------------

Returns

Eigenvectors of Hermitian A , as columns of a complex matrix

6.1.3.58 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::inverse (const Eigen::MatrixBase<Derived> & A)`

Inverse.

Parameters

A	Eigen expression
---	------------------

Returns

Inverse of A , as a dynamic matrix over the same scalar field as A

6.1.3.59 `std::vector<idx> qpp::invperm (const std::vector<idx> & perm) [inline]`

Inverse permutation.

Parameters

perm	Permutation
------	-------------

Returns

Inverse of the permutation $perm$

6.1.3.60 `template<typename Derived> dyn_col_vect<typename Derived::Scalar> qpp::ip (const Eigen::MatrixBase<Derived> & phi, const Eigen::MatrixBase<Derived> & psi, const std::vector<idx> & subsys, const std::vector<idx> & dims)`

Generalized inner product.

Parameters

<i>phi</i>	Column vector Eigen expression
<i>psi</i>	Column vector Eigen expression
<i>subsys</i>	Subsystem indexes over which <i>phi</i> is defined
<i>dims</i>	Dimensions of the multi-partite system

Returns

The inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.61 `template<typename Derived> dyn_col_vect<typename Derived::Scalar> qpp::ip (const Eigen::MatrixBase<Derived> & phi, const Eigen::MatrixBase<Derived> & psi, const std::vector<idx> & subsys, idx d = 2)`

Generalized inner product.

Parameters

<i>phi</i>	Column vector Eigen expression
<i>psi</i>	Column vector Eigen expression
<i>subsys</i>	Subsystem indexes over which <i>phi</i> is defined
<i>d</i>	Subsystem dimensions

Returns

The inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.62 bool qpp::isprime(ubigint n) [inline]

Primality test.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

<i>n</i>	Integer strictly greater than 1
----------	---------------------------------

Returns

True if the number is prime, false otherwise

6.1.3.63 cmat qpp::kraus2choi(const std::vector< cmat > & Ks) [inline]

Choi matrix.

See also

[qpp::choi2kraus\(\)](#)

Constructs the Choi matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Note

The superoperator matrix *S* and the Choi matrix *C* are related by $S_{ab,mn} = C_{ma,nb}$

Parameters

<i>Ks</i>	Set of Kraus operators
-----------	------------------------

Returns

Choi matrix

6.1.3.64 cmat qpp::kraus2super(const std::vector< cmat > & Ks) [inline]

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Parameters

<i>Ks</i>	Set of Kraus operators
-----------	------------------------

Returns

Superoperator matrix

6.1.3.65 `template<typename T > dyn_mat<typename T::Scalar> qpp::kron (const T & head)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Used to stop the recursion for the variadic template version of [qpp::kron\(\)](#)

Parameters

<i>head</i>	Eigen expression
-------------	------------------

Returns

Its argument *head*

6.1.3.66 `template<typename T , typename... Args> dyn_mat<typename T::Scalar> qpp::kron (const T & head, const Args &... tail)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Parameters

<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)

Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.67 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::kron (const std::vector< Derived > & As)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Parameters

<code>As</code>	<code>std::vector of Eigen expressions</code>
-----------------	-----------------------------------------------

Returns

Kronecker product of all elements in `As`, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.68 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::kron (const std::initializer_list<Derived> & As)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Parameters

<code>As</code>	<code>std::initializer_list of Eigen expressions, such as {A1, A2, ... ,Ak}</code>
-----------------	------------------------------------------------------------------------------------

Returns

Kronecker product of all elements in `As`, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.69 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::kronpow (const Eigen::MatrixBase<Derived> & A, idx n)`

Kronecker power.

See also

[qpp::kron\(\)](#)

Parameters

<code>A</code>	Eigen expression
<code>n</code>	Non-negative integer

Returns

Kronecker product of `A` with itself `n` times $A^{\otimes n}$, as a dynamic matrix over the same scalar field as `A`

6.1.3.70 `ubigint qpp::lcm (ubigint m, ubigint n) [inline]`

Least common multiple of two positive integers.

See also

[qpp::gcd\(\)](#)

Parameters

<i>m</i>	Positive integer
<i>n</i>	Positive integer

Returns

Least common multiple of *m* and *n*

6.1.3.71 ubigint qpp::lcm (const std::vector<ubigint> & ns) [inline]

Least common multiple of a list of positive integers.

See also

[qpp::gcd\(\)](#)

Parameters

<i>ns</i>	List of positive integers
-----------	---------------------------

Returns

Least common multiple of all numbers in *ns*

6.1.3.72 template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::load (const std::string & fname)

Loads Eigen matrix from a binary file (internal format) in double precision.

See also

[qpp::save\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
auto mat = load<cmat>("input.bin");
```

Parameters

<i>A</i>	Eigen expression
<i>fname</i>	Output file name

6.1.3.73 template<typename Derived> Derived qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

See also

[qpp::saveMATLABmatrix\(\)](#)

This is the generic version that always throws [qpp::Exception::Type::UNDEFINED_TYPE](#). It is specialized only for [qpp::dmat](#) and [qpp::cmat](#) (the only matrix types that can be loaded)

6.1.3.74 template<> **dmat** qpp::loadMATLABmatrix (const std::string & *mat_file*, const std::string & *var_name*)
 [inline]

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))

See also

[qpp::saveMATLABmatrix\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
auto mat = loadMATLABmatrix<dmat>("input.mat");
```

Note

If *var_name* is a complex matrix, only the real part is loaded

Parameters

<i>mat_file</i>	MATLAB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen double dynamic matrix ([qpp::dmat](#))

6.1.3.75 template<> **cmat** qpp::loadMATLABmatrix (const std::string & *mat_file*, const std::string & *var_name*)
 [inline]

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

See also

[qpp::saveMATLABmatrix\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic complex matrix
// from the MATLAB file "input.mat"
auto mat = loadMATLABmatrix<cmat>("input.mat");
```

Parameters

<i>mat_file</i>	MATLAB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen complex dynamic matrix ([qpp::cmat](#))

6.1.3.76 template<typename Derived > Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > & *A*)

Logarithm of the determinant.

Useful when the determinant overflows/underflows

Parameters

A	Eigen expression
---	------------------

Returns

Logarithm of the determinant of A , as a scalar over the same scalar field as A

6.1.3.77 template<typename Derived> cmat qpp::logm (const Eigen::MatrixBase<Derived> & A)

Matrix logarithm.

Parameters

A	Eigen expression
---	------------------

Returns

Matrix logarithm of A

6.1.3.78 template<typename Derived> double qpp::lognegativity (const Eigen::MatrixBase<Derived> & A, const std::vector<idx> & dims)

Logarithmic negativity of the bi-partite mixed state A .

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.79 std::vector<double> qpp::marginalX (const dmat & probXY) [inline]

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
--------	----------------------------------------------------------------------------------------------------------------------------------------------------

Returns

Real vector consisting of the marginal distribution of X

6.1.3.80 std::vector<double> qpp::marginalY (const dmat & probXY) [inline]

Marginal distribution.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
---------------	----------------------------------------------------------------------------------------------------------------------------------------------------

Returns

Real vector consisting of the marginal distribution of Y

6.1.3.81 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::vector< cmat > & Ks)`

Measures the state A using the set of Kraus operators Ks .

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.82 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::initializer_list< cmat > & Ks)`

Measures the state A using the set of Kraus operators Ks .

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.83 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const cmat & U)`

Measures the state A in the orthonormal basis specified by the unitary matrix U .

Parameters

<i>A</i>	Eigen expression
<i>U</i>	Unitary matrix whose columns represent the measurement basis vectors

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.84 template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::vector< cmat > & Ks, const std::vector< idx > & subsys, const std::vector< idx > & dims)

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.85 template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::initializer_list< cmat > & Ks, const std::vector< idx > & subsys, const std::vector< idx > & dims)

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.86 template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::vector< cmat > & Ks, const std::vector< idx > & subsys, idx d = 2)

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.87 template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::initializer_list< cmat > & Ks, const std::vector< idx > & subsys, idx d = 2)

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.88 template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const cmat & V, const std::vector< idx > & subsys, const std::vector< idx > & dims)

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>V</i>	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.89 template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const cmat & V, const std::vector< idx > & subsys, idx d = 2)

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>V</i>	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.90 `template<typename Derived > std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (const Eigen::MatrixBase< Derived > & A, std::vector< idx > subsys, std::vector< idx > dims)`

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

[qpp::measure\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.91 `template<typename Derived > std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (const Eigen::MatrixBase< Derived > & A, std::vector< idx > subsys, idx d = 2)`

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

[qpp::measure\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.92 `ket qpp::mket (const std::vector< idx > & mask, const std::vector< idx > & dims) [inline]`

Multi-partite qudit ket.

Constructs the multi-partite qudit ket $|mask\rangle$, where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.93 ket qpp::mket (const std::vector< idx > & *mask*, idx *d* = 2) [inline]

Multi-partite qudit ket.

Constructs the multi-partite qudit ket $|mask\rangle$, all subsystem having equal dimension d . *mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than d .

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystem dimensions

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.94 ubigint qpp::modpow (ubigint *a*, ubigint *n*, ubigint *p*) [inline]

Integer power modulo p.

Computes $a^n \bmod p$

Parameters

<i>a</i>	Non-negative integer
<i>n</i>	Non-negative integer
<i>p</i>	Strictly positive integer

Returns

$a^n \bmod p$

6.1.3.95 cmat qpp::mprj (const std::vector< idx > & *mask*, const std::vector< idx > & *dims*) [inline]

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket $|mask\rangle$, where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.96 `cmat qpp::mprj(const std::vector< idx > & mask, idx d = 2) [inline]`

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket $|mask\rangle$, all subsystem having equal dimension d . $mask$ is a `std::vector` of non-negative integers, and each element in $mask$ has to be strictly smaller than d .

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystem dimensions

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.97 `idx qpp::multiidx2n (const std::vector< idx > & midx, const std::vector< idx > & dims) [inline]`

Multi-index to non-negative integer index.

See also

[qpp::n2multiidx\(\)](#)

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

<i>midx</i>	Multi-index
<i>dims</i>	Dimensions of the multi-partite system

Returns

Non-negative integer index

6.1.3.98 `std::vector<idx> qpp::n2multiidx (idx n, const std::vector< idx > & dims) [inline]`

Non-negative integer index to multi-index.

See also

[qpp::multiidx2n\(\)](#)

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

<i>n</i>	Non-negative integer index
<i>dims</i>	Dimensions of the multi-partite system

Returns

Multi-index of the same size as *dims*

6.1.3.99 `template<typename Derived > double qpp::negativity (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & dims)`

Negativity of the bi-partite mixed state *A*.

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Negativity

6.1.3.100 template<typename Derived> double qpp::norm (const Eigen::MatrixBase<Derived> & A)

Frobenius norm.

Parameters

<i>A</i>	Eigen expression
----------	------------------

ReturnsFrobenius norm of *A***6.1.3.101 cplx qpp::omega (idx *D*) [inline]**

D-th root of unity.

Parameters

<i>D</i>	Non-negative integer
----------	----------------------

ReturnsD-th root of unity $\exp(2\pi i/D)$ **6.1.3.102 constexpr cplx qpp::operator""_i (unsigned long long int *x*) [inline], [noexcept]**User-defined literal for complex $i = \sqrt{-1}$ (integer overload)

Example:

`auto z = 4_i; // type of z is std::complex<double>`**6.1.3.103 constexpr cplx qpp::operator""_i (long double *x*) [inline], [noexcept]**User-defined literal for complex $i = \sqrt{-1}$ (real overload)

Example:

`auto z = 4.5_i; // type of z is std::complex<double>`**6.1.3.104 template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::powm (const Eigen::MatrixBase<Derived> & A, idx *n*)**

Matrix power.

See also[qpp::spectralpowm\(\)](#)Explicitly multiplies the matrix *A* with itself *n* times. By convention $A^0 = I$.

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Matrix power A^n , as a dynamic matrix over the same scalar field as A

6.1.3.105 template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::prj (const Eigen::MatrixBase<Derived> & V)

Projector.

Normalized projector onto state vector

Parameters

V	Eigen expression
---	------------------

Returns

Projector onto the state vector V, or the matrix Zero if V has norm zero (i.e. smaller than `qpp::eps`), as a dynamic matrix over the same scalar field as A

6.1.3.106 template<typename Derived> Derived::Scalar qpp::prod (const Eigen::MatrixBase<Derived> & A)

Element-wise product of A.

Parameters

A	Eigen expression
---	------------------

Returns

Element-wise product of A, as a scalar over the same scalar field as A

6.1.3.107 template<typename InputIterator> std::iterator_traits<InputIterator>::value_type qpp::prod (InputIterator first, InputIterator last)

Element-wise product of an STL-like range.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Element-wise product of the range, as a scalar over the same scalar field as the range

6.1.3.108 template<typename Container> Container::value_type qpp::prod (const Container & c)

Element-wise product of the elements of an STL-like container.

Parameters

<i>c</i>	STL-like container
----------	--------------------

Returns

Element-wise product of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.109 template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::ptrace (const Eigen::MatrixBase<Derived > & *A*, const std::vector<idx> & *subsys*, const std::vector<idx> & *dims*)

Partial trace.

See also

[qpp::ptrace1\(\)](#), [qpp::ptrace2\(\)](#)

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>dims</i>	Dimensions of the multi-partite system

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.110 template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::ptrace (const Eigen::MatrixBase<Derived > & *A*, const std::vector<idx> & *subsys*, idx *d* = 2)

Partial trace.

See also

[qpp::ptrace1\(\)](#), [qpp::ptrace2\(\)](#)

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>d</i>	Subsystem dimensions

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.111 template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::ptrace1 (const Eigen::MatrixBase<Derived > & *A*, const std::vector<idx> & *dims*)

Partial trace.

See also

[qpp::ptrace2\(\)](#)

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system (must be a std::vector with 2 elements)

Returns

Partial trace $Tr_A(\cdot)$ over the first subsystem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as A

6.1.3.112 template<typename Derived> **dyn_mat<typename Derived::Scalar>** qpp::ptrace2 (const Eigen::MatrixBase<Derived> & *A*, const std::vector<idx> & *dims*)

Partial trace.

See also

[qpp::ptrace1\(\)](#)

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system (must be a std::vector with 2 elements)

Returns

Partial trace $Tr_B(\cdot)$ over the second subsystem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as A

6.1.3.113 template<typename Derived> **dyn_mat<typename Derived::Scalar>** qpp::ptranspose (const Eigen::MatrixBase<Derived> & *A*, const std::vector<idx> & *subsys*, const std::vector<idx> & *dims*)

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>dims</i>	Dimensions of the multi-partite system

Returns

Partial transpose $(\cdot)^T_{subsys}$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.114 template<typename Derived> **dyn_mat<typename Derived::Scalar>** qpp::ptranspose (const Eigen::MatrixBase<Derived> & *A*, const std::vector<idx> & *subsys*, idx *d* = 2)

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>d</i>	Subsystem dimensions

Returns

Partial transpose $(\cdot)^T_{subsys}$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.115 `template<typename Derived> double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsysA, const std::vector< idx > & subsysB, const std::vector< idx > & dims)`

Quantum mutual information between 2 subsystems of a composite system.

Parameters

<i>A</i>	Eigen expression
<i>subsysA</i>	Indexes of the first subsystem
<i>subsysB</i>	Indexes of the second subsystem
<i>dims</i>	Dimensions of the multi-partite system

Returns

Mutual information between the 2 subsystems

6.1.3.116 `template<typename Derived> double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsysA, const std::vector< idx > & subsysB, idx d = 2)`

Quantum mutual information between 2 subsystems of a composite system.

Parameters

<i>A</i>	Eigen expression
<i>subsysA</i>	Indexes of the first subsystem
<i>subsysB</i>	Indexes of the second subsystem
<i>d</i>	Subsystem dimensions

Returns

Mutual information between the 2 subsystems

6.1.3.117 `double qpp::rand (double a = 0, double b = 1) [inline]`

Generates a random real number uniformly distributed in the interval [a, b)

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

Returns

Random real number (double) uniformly distributed in the interval [a, b)

```
6.1.3.118 bigint qpp::rand ( bigint a = std::numeric_limits<bigint>::min(), bigint b =  
    std::numeric_limits<bigint>::max() ) [inline]
```

Generates a random big integer uniformly distributed in the interval [a, b].

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.119 `ubigint qpp::rand (ubigint a = std::numeric_limits<ubigint>::min (), ubigint b = std::numeric_limits<ubigint>::max ()) [inline]`

Generates a random non-negative big integer uniformly distributed in the interval [a, b].

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

Returns

Random non-negative big integer uniformly distributed in the interval [a, b]

6.1.3.120 `template<typename Derived > Derived qpp::rand (idx rows, idx cols, double a = 0, double b = 1)`

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat`

6.1.3.121 `template<> dmat qpp::rand (idx rows, idx cols, double a, double b) [inline]`

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (`qpp::dmat`)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries uniformly distributed in [-1,1)
auto mat = rand<dmat>(3, 3, -1, 1);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

Returns

Random real matrix

6.1.3.122 template<> cmat qpp::rand(idx rows, idx cols, double a, double b) [inline]

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) uniformly distributed in [-1,1)
auto mat = rand<cmat>(3, 3, -1, 1);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

Returns

Random complex matrix

6.1.3.123 cmat qpp::randH(idx D) [inline]

Generates a random Hermitian matrix.

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random Hermitian matrix

6.1.3.124 idx qpp::randidx(idx a = std::numeric_limits<idx>::min(), idx b = std::numeric_limits<idx>::max()) [inline]

Generates a random index (idx) uniformly distributed in the interval [a, b].

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

Returns

Random index (idx) uniformly distributed in the interval [a, b]

6.1.3.125 ket qpp::randket(idx D) [inline]

Generates a random normalized ket (pure state vector)

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random normalized ket

6.1.3.126 std::vector<cmat> qpp::randkraus (idx *N*, idx *D*) [inline]

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition $\sum_i K_i^\dagger K_i = I$

Parameters

<i>N</i>	Number of Kraus operators
<i>D</i>	Dimension of the Hilbert space

Returns

Set of *N* Kraus operators satisfying the closure condition

6.1.3.127 template<typename Derived > Derived qpp::randn (idx *rows*, idx *cols*, double *mean* = 0, double *sigma* = 1)

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws [qpp::Exception::Type::UNDEFINED_TYPE](#). It is specialized only for [qpp::dmat](#) and [qpp::cmat](#)

6.1.3.128 template<> dmat qpp::randn (idx *rows*, idx *cols*, double *mean*, double *sigma*) [inline]

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices ([qpp::dmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries normally distributed in N(0,2)
auto mat = randn<dmat>(3, 3, 0, 2);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

Returns

Random real matrix

6.1.3.129 template<> cmat qpp::randn (idx rows, idx cols, double mean, double sigma) [inline]

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) normally distributed in N(0,2)
auto mat = randn<cmat>(3, 3, 0, 2);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

Returns

Random complex matrix

6.1.3.130 double qpp::randn (double mean = 0, double sigma = 1) [inline]

Generates a random real number (double) normally distributed in N(mean, sigma)

Parameters

<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

Returns

Random real number normally distributed in N(mean, sigma)

6.1.3.131 std::vector<idx> qpp::randperm (idx n) [inline]

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by std::shuffle), so that all permutations are equally probable

Parameters

<i>n</i>	Size of the permutation
----------	-------------------------

Returns

Random permutation of size *n*

6.1.3.132 cmat qpp::randrho (idx D) [inline]

Generates a random density matrix.

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random density matrix

6.1.3.133 cmat qpp::randU (idx *D*) [inline]

Generates a random unitary matrix.

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random unitary

6.1.3.134 cmat qpp::randV (idx *Din*, idx *Dout*) [inline]

Generates a random isometry matrix.

Parameters

<i>Din</i>	Size of the input Hilbert space
<i>Dout</i>	Size of the output Hilbert space

Returns

Random isometry matrix

6.1.3.135 template<typename Derived> double qpp::renyi (const Eigen::MatrixBase<Derived> & *A*, double *alpha*)

Renyi- α entropy of the density matrix *A*, for $\alpha \geq 0$.

Note

When $\alpha \rightarrow 1$ the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

Parameters

<i>A</i>	Eigen expression
<i>alpha</i>	Non-negative real number, use qpp::infinity for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.136 double qpp::renyi (const std::vector<double> & *prob*, double *alpha*) [inline]

Renyi- α entropy of the probability distribution *prob*, for $\alpha \geq 0$.

Note

When $\alpha \rightarrow 1$ the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

Parameters

<i>prob</i>	Real probability vector
<i>alpha</i>	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.137 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::reshape (const Eigen::MatrixBase<Derived> & A, idx rows, idx cols)`

Reshape.

Uses column-major order when reshaping (same as MATLAB)

Parameters

<i>A</i>	Eigen expression
<i>rows</i>	Number of rows of the reshaped matrix
<i>cols</i>	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field as *A*

6.1.3.138 `template<typename Derived> std::vector<double> qpp::rho2bloch (const Eigen::MatrixBase<Derived> & A)`

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix *A*.

See also

[qpp::bloch2rho\(\)](#)

Note

It is implicitly assumed that the density matrix is Hermitian

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

3-dimensional Bloch vector

6.1.3.139 `template<typename Derived> dyn_col_vect<typename Derived::Scalar> qpp::rho2pure (const Eigen::MatrixBase<Derived> & A)`

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

Note

No purity check is done, the input state *A* must have rank one, otherwise the function returns the first non-zero eigenvector of *A*

Parameters

A	Eigen expression, assumed to be proportional to a projector onto a pure state, i.e. A is assumed to have rank one
---	-------------------------------------------------------------------------------------------------------------------

Returns

The unique non-zero eigenvector of A, as a dynamic column vector over the same scalar field as A

6.1.3.140 template<typename Derived > void qpp::save (const Eigen::MatrixBase< Derived > & A, const std::string & fname)

Saves Eigen expression to a binary file (internal format) in double precision.

See also

[qpp::load\(\)](#)

Parameters

A	Eigen expression
fname	Output file name

6.1.3.141 template<typename Derived > void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

See also

[qpp::loadMATLABmatrix\(\)](#)

This is the generic version that always throws [qpp::Exception::Type::UNDEFINED_TYPE](#). It is specialized only for [qpp::dmat](#) and [qpp::cmat](#) (the only matrix types that can be saved)

6.1.3.142 template<> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode) [inline]

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))

See also

[qpp::loadMATLABmatrix\(\)](#)

Parameters

A	Eigen expression over the complex field
mat_file	MATLAB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

6.1.3.143 template<> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< cmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode) [inline]

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

See also

[qpp::loadMATLABmatrix\(\)](#)

Parameters

<i>A</i>	Eigen expression over the complex field
<i>mat_file</i>	MATLAB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

6.1.3.144 template<typename Derived > double qpp::schatten (const Eigen::MatrixBase< Derived > & *A*, double *p*)

Schatten matrix norm.

Parameters

<i>A</i>	Eigen expression
<i>p</i>	Real number, greater or equal to 1, use qpp::infty for <i>p</i> = ∞

Returns

Schatten-*p* matrix norm of *A*

6.1.3.145 template<typename Derived > cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > & *A*, const std::vector< idx > & *dims*)

Schmidt basis on Alice side.

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Unitary matrix *U* whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.146 template<typename Derived > cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > & *A*, const std::vector< idx > & *dims*)

Schmidt basis on Bob side.

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Unitary matrix *V* whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.147 template<typename Derived > dyn_col_vect<double> qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > & *A*, const std::vector< idx > & *dims*)

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

[qpp::schmidtprobs\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Schmidt coefficients of *A*, as a real dynamic column vector

6.1.3.148 `template<typename Derived> std::vector<double> qpp::schmidtprobs (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & dims)`

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

[qpp::schmidtcoeffs\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Real vector consisting of the Schmidt probabilities of *A*

6.1.3.149 `template<typename Container> double qpp::sigma (const std::vector< double > & prob, const Container & X)`

Standard deviation.

Parameters

<i>prob</i>	Real probability vector representing the probability distribution of <i>X</i>
<i>X</i>	Random variable values represented by an STL-like container

Returns

Standard deviation of *X*

6.1.3.150 `template<typename Derived> cmat qpp::sinm (const Eigen::MatrixBase< Derived > & A)`

Matrix sin.

Parameters

A	Eigen expression
---	------------------

Returns

Matrix sine of A

6.1.3.151 template<typename Derived> cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > & A, const cplx z)

Matrix power.

See also

[qpp::powm\(\)](#)

Uses the spectral decomposition of A to compute the matrix power. By convention $A^0 = I$.

Parameters

A	Eigen expression
z	Complex number

Returns

Matrix power A^z

6.1.3.152 template<typename Derived> cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > & A)

Matrix square root.

Parameters

A	Eigen expression
---	------------------

Returns

Matrix square root of A

6.1.3.153 template<typename Derived> Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > & A)

Element-wise sum of A .

Parameters

A	Eigen expression
---	------------------

Returns

Element-wise sum of A , as a scalar over the same scalar field as A

6.1.3.154 template<typename InputIterator> std::iterator_traits<InputIterator>::value_type qpp::sum (InputIterator first, InputIterator last)

Element-wise sum of an STL-like range.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

Returns

Element-wise sum of the range, as a scalar over the same scalar field as the range

6.1.3.155 template<typename Container > Container::value_type qpp::sum (const Container & c)

Element-wise sum of the elements of an STL-like container.

Parameters

<i>c</i>	STL-like container
----------	--------------------

Returns

Element-wise sum of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.156 cmat qpp::super2choi (const cmat & A) [inline]

Converts superoperator matrix to Choi matrix.

See also

[qpp::choi2super\(\)](#)

Parameters

<i>A</i>	Superoperator matrix
----------	----------------------

Returns

Choi matrix

6.1.3.157 template<typename Derived > dyn_col_vect<double> qpp::svals (const Eigen::MatrixBase< Derived > & A)

Singular values.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Singular values of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.158 template<typename Derived > std::tuple<cmat, dyn_col_vect < double >, cmat> qpp::svd (const Eigen::MatrixBase< Derived > & A)

Full singular value decomposition.

Parameters

A	Eigen expression
---	------------------

Returns

Tuple of: 1. Left singular vectors of A , as columns of a complex dynamic matrix, 2. Singular values of A , ordered in decreasing order, as a real dynamic column vector, and 3. Right singular vectors of A , as columns of a complex dynamic matrix

6.1.3.159 template<typename Derived> cmat qpp::svdU (const Eigen::MatrixBase< Derived > & A)

Left singular vectors.

Parameters

A	Eigen expression
---	------------------

Returns

Complex dynamic matrix, whose columns are the left singular vectors of A

6.1.3.160 template<typename Derived> cmat qpp::svdV (const Eigen::MatrixBase< Derived > & A)

Right singular vectors.

Parameters

A	Eigen expression
---	------------------

Returns

Complex dynamic matrix, whose columns are the right singular vectors of A

6.1.3.161 template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::syspermute (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & perm, const std::vector< idx > & dims)

Subsystem permutation.

Permutates the subsystems of a state vector or density matrix. The qubit $perm[i]$ is permuted to the location i .

Parameters

A	Eigen expression
perm	Permutation
dims	Dimensions of the multi-partite system

Returns

Permuted system, as a dynamic matrix over the same scalar field as A

6.1.3.162 template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::syspermute (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & perm, idx d = 2)

Subsystem permutation.

Permutates the subsystems of a state vector or density matrix. The qubit $perm[i]$ is permuted to the location i .

Parameters

<i>A</i>	Eigen expression
<i>perm</i>	Permutation
<i>d</i>	Subsystem dimensions

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.163 template<typename Derived> Derived::Scalar qpp::trace (const Eigen::MatrixBase<Derived> & *A*)

Trace.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Trace of *A*, as a scalar over the same scalar field as *A*

6.1.3.164 template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::transpose (const Eigen::MatrixBase<Derived> & *A*)

Transpose.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Transpose of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.165 template<typename Derived> double qpp::tsallis (const Eigen::MatrixBase<Derived> & *A*, double *q*)

Tsallis- *q* entropy of the density matrix *A*, for $q \geq 0$.

Note

When $q \rightarrow 1$ the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base e

Parameters

<i>A</i>	Eigen expression
<i>q</i>	Non-negative real number

Returns

Tsallis- *q* entropy

6.1.3.166 double qpp::tsallis (const std::vector<double> & *prob*, double *q*) [inline]

Tsallis- *q* entropy of the probability distribution *prob*, for $q \geq 0$.

Note

When $q \rightarrow 1$ the Tsallis entropy converges to the Shannon entropy, with the logarithm in base e

Parameters

<i>prob</i>	Real probability vector
<i>q</i>	Non-negative real number

Returns

Tsallis- *q* entropy

6.1.3.167 std::vector<double> qpp::uniform (idx *N*) [inline]

Uniform probability distribution vector.

Parameters

<i>N</i>	Size of the alphabet
----------	----------------------

Returns

Real vector consisting of a uniform distribution of size *N*

6.1.3.168 template<typename Container > double qpp::var (const std::vector< double > & *prob*, const Container & *X*)

Variance.

Parameters

<i>prob</i>	Real probability vector representing the probability distribution of <i>X</i>
<i>X</i>	Random variable values represented by an STL-like container

Returns

Variance of *X*

6.1.3.169 std::vector<int> qpp::x2contfrac (double *x*, idx *n*, idx *cut*=1e5) [inline]

Simple continued fraction expansion.

See also

[qpp::contfrac2x\(\)](#)

Parameters

<i>x</i>	Real number
<i>n</i>	Number of terms in the expansion
<i>cut</i>	Stop the expansion when the next term is greater than <i>cut</i>

Returns

Integer vector containing the simple continued fraction expansion of *x*. If there are *m* less than *n* terms in the expansion, a shorter vector with *m* components is returned.

6.1.4 Variable Documentation

6.1.4.1 constexpr double qpp::chop = 1e-10

Used in [qpp::disp\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::chop](#).

6.1.4.2 `constexpr double qpp::ee = 2.718281828459045235360287471352662497`

Base of natural logarithm, e .

6.1.4.3 `constexpr double qpp::eps = 1e-12`

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::eps) // x is zero
```

6.1.4.4 `constexpr double qpp::infty = std::numeric_limits<double>::infinity()`

Used to denote infinity in double precision.

6.1.4.5 `constexpr idx qpp::maxn = 64`

Maximum number of allowed qu(d)its (subsystems)

Used internally to allocate arrays on the stack (for speed reasons)

6.1.4.6 `constexpr double qpp::pi = 3.141592653589793238462643383279502884`

π

6.2 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

6.2.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

6.3 qpp::internal Namespace Reference

Internal utility functions, do not use/modify.

Namespaces

- [_details](#)

Classes

- class [IOManipEigen](#)
- class [IOManipPointer](#)
- class [IOManipRange](#)
- class [Singleton](#)

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Functions

- void `_n2multiidx (idx n, idx numdims, const idx *dims, idx *result) noexcept`
- `idx _multiidx2n (const idx *midx, idx numdims, const idx *dims) noexcept`
- template<typename Derived>
 `bool _check_square_mat (const Eigen::MatrixBase< Derived > &A)`
- template<typename Derived>
 `bool _check_vector (const Eigen::MatrixBase< Derived > &A)`
- template<typename Derived>
 `bool _check_rvector (const Eigen::MatrixBase< Derived > &A)`
- template<typename Derived>
 `bool _check_cvector (const Eigen::MatrixBase< Derived > &A)`
- template<typename Derived>
 `bool _check_nonzero_size (const T &x) noexcept`
- template<typename T1, typename T2>
 `bool _check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept`
- `bool _check_dims (const std::vector< idx > &dims)`
- template<typename Derived>
 `bool _check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)`
- template<typename Derived>
 `bool _check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)`
- template<typename Derived>
 `bool _check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)`
- `bool _check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept`
- `bool _check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)`
- template<typename Derived>
 `bool _check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept`
- template<typename Derived>
 `bool _check_qubit_cvector (const Eigen::MatrixBase< Derived > &V) noexcept`
- template<typename Derived>
 `bool _check_qubit_rvector (const Eigen::MatrixBase< Derived > &V) noexcept`
- template<typename Derived>
 `bool _check_qubit_vector (const Eigen::MatrixBase< Derived > &V) noexcept`
- `bool _check_perm (const std::vector< idx > &perm)`
- template<typename Derived1, typename Derived2>
 `dyn_mat< typename Derived1::Scalar > _kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen<->::MatrixBase< Derived2 > &B)`
- template<typename Derived1, typename Derived2>
 `dyn_mat< typename Derived1::Scalar > _dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- template<typename T>
 `void variadic_vector_emplace (std::vector< T > &)`
- template<typename T, typename First, typename... Args>
 `void variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&...args)`

6.3.1 Detailed Description

Internal utility functions, do not use/modify.

6.3.2 Function Documentation

6.3.2.1 template<typename Derived> bool qpp::internal::_check_cvector (const Eigen::MatrixBase< Derived > & A)

6.3.2.2 bool qpp::internal::_check_dims (const std::vector< idx > & dims) [inline]

- 6.3.2.3 template<typename Derived > bool qpp::internal::_check_dims_match_cvect (const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & V)
- 6.3.2.4 template<typename Derived > bool qpp::internal::_check_dims_match_mat (const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & A)
- 6.3.2.5 template<typename Derived > bool qpp::internal::_check_dims_match_rvect (const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & V)
- 6.3.2.6 bool qpp::internal::_check_eq_dims (const std::vector< idx > & dims, idx dim) [inline], [noexcept]
- 6.3.2.7 template<typename T1 , typename T2 > bool qpp::internal::_check_matching_sizes (const T1 & lhs, const T2 & rhs) [noexcept]
- 6.3.2.8 template<typename T > bool qpp::internal::_check_nonzero_size (const T & x) [noexcept]
- 6.3.2.9 bool qpp::internal::_check_perm (const std::vector< idx > & perm) [inline]
- 6.3.2.10 template<typename Derived > bool qpp::internal::_check_qubit_cvector (const Eigen::MatrixBase< Derived > & V) [noexcept]
- 6.3.2.11 template<typename Derived > bool qpp::internal::_check_qubit_matrix (const Eigen::MatrixBase< Derived > & A) [noexcept]
- 6.3.2.12 template<typename Derived > bool qpp::internal::_check_qubit_rvector (const Eigen::MatrixBase< Derived > & V) [noexcept]
- 6.3.2.13 template<typename Derived > bool qpp::internal::_check_qubit_vector (const Eigen::MatrixBase< Derived > & V) [noexcept]
- 6.3.2.14 template<typename Derived > bool qpp::internal::_check_rvector (const Eigen::MatrixBase< Derived > & A)
- 6.3.2.15 template<typename Derived > bool qpp::internal::_check_square_mat (const Eigen::MatrixBase< Derived > & A)
- 6.3.2.16 bool qpp::internal::_check_subsys_match_dims (const std::vector< idx > & subsys, const std::vector< idx > & dims) [inline]
- 6.3.2.17 template<typename Derived > bool qpp::internal::_check_vector (const Eigen::MatrixBase< Derived > & A)
- 6.3.2.18 template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::internal::_dirsum2 (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)
- 6.3.2.19 template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::internal::_kron2 (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)
- 6.3.2.20 idx qpp::internal::_multiidx2n (const idx * midx, idx numdims, const idx * dims) [inline], [noexcept]
- 6.3.2.21 void qpp::internal::_n2multiidx (idx n, idx numdims, const idx * dims, idx * result) [inline], [noexcept]
- 6.3.2.22 template<typename T > void qpp::internal::variadic_vector_emplace (std::vector< T > &)
- 6.3.2.23 template<typename T , typename First , typename... Args> void qpp::internal::variadic_vector_emplace (std::vector< T > & v, First && first, Args &&... args)

6.4 qpp::internal::_details Namespace Reference

Classes

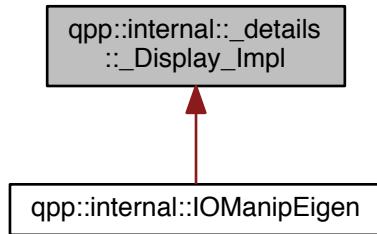
- struct [_Display_Impl](#)

Chapter 7

Class Documentation

7.1 `qpp::internal::_details::_Display_Impl` Struct Reference

```
#include <internal/classes/iomanip.h>
Inheritance diagram for qpp::internal::_details::_Display_Impl:
```



Public Member Functions

- template<typename T >
std::ostream & `_display_impl` (const T & _A, std::ostream & _os, double _chop=qpp::chop) const

7.1.1 Member Function Documentation

7.1.1.1 template<typename T > std::ostream& qpp::internal::_details::_Display_Impl::_display_impl (const T & _A, std::ostream & _os, double _chop = qpp::chop) const [inline]

The documentation for this struct was generated from the following file:

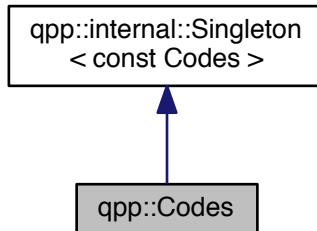
- internal/classes/[iomanip.h](#)

7.2 `qpp::Codes` Class Reference

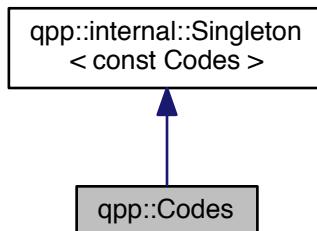
const Singleton class that defines quantum error correcting codes

```
#include <classes/codes.h>
```

Inheritance diagram for `qpp::Codes`:



Collaboration diagram for `qpp::Codes`:



Public Types

- enum `Type` { `Type::FIVE_QUBIT` = 1, `Type::SEVEN_QUBIT_STEANE`, `Type::NINE_QUBIT_SHOR` }
- Code types, add more codes here if needed.*

Public Member Functions

- `ket codeword (Type type, idx i) const`
- Returns the codeword of the specified code type.*

Private Member Functions

- `Codes ()`
Default constructor.
- `~Codes ()=default`
Default destructor.

Friends

- class [internal::Singleton< const Codes >](#)

Additional Inherited Members

7.2.1 Detailed Description

const Singleton class that defines quantum error correcting codes

7.2.2 Member Enumeration Documentation

7.2.2.1 enum qpp::Codes::Type [strong]

Code types, add more codes here if needed.

See also

[qpp::Codes::codeword\(\)](#)

Enumerator

- FIVE_QUBIT** [[5,1,3]] qubit code
- SEVEN_QUBIT_STEANE** [[7,1,3]] Steane qubit code
- NINE_QUBIT_SHOR** [[9,1,3]] Shor qubit code

7.2.3 Constructor & Destructor Documentation

7.2.3.1 qpp::Codes::Codes() [inline], [private]

Default constructor.

7.2.3.2 qpp::Codes::~Codes() [private], [default]

Default destructor.

7.2.4 Member Function Documentation

7.2.4.1 ket qpp::Codes::codeword(Type type, idx i) const [inline]

Returns the codeword of the specified code type.

See also

[qpp::Codes::Type](#)

Parameters

<i>type</i>	Code type
<i>i</i>	Codeword index

Returns

i-th codeword of the code *type*

7.2.5 Friends And Related Function Documentation

7.2.5.1 friend class internal::Singleton< const Codes > [friend]

The documentation for this class was generated from the following file:

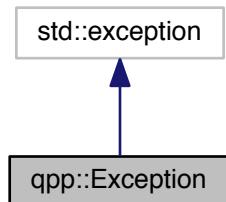
- classes/codes.h

7.3 qpp::Exception Class Reference

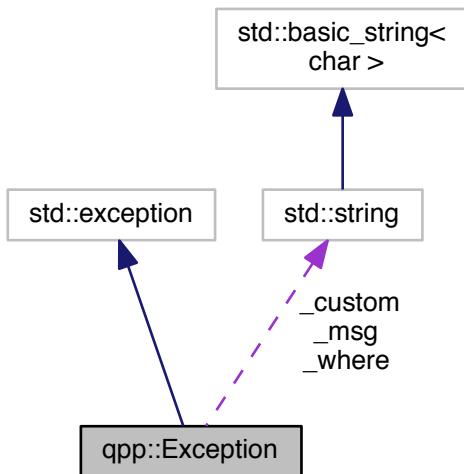
Generates custom exceptions, used when validating function parameters.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



Public Types

- enum `Type` {
 `Type::UNKNOWN_EXCEPTION` = 1, `Type::ZERO_SIZE`, `Type::MATRIX_NOT_SQUARE`, `Type::MATRIX_NOT_CVECTOR`,
`Type::MATRIX_NOT_RVECTOR`, `Type::MATRIX_NOT_VECTOR`, `Type::MATRIX_NOT_SQUARE_OR_CVECTOR`,
`Type::MATRIX_NOT_SQUARE_OR_RVECTOR`,
`Type::MATRIX_NOT_SQUARE_OR_VECTOR`, `Type::MATRIX_MISMATCH_SUBSYS`, `Type::DIMS_INVALID`,
`Type::DIMS_NOT_EQUAL`,
`Type::DIMS_MISMATCH_MATRIX`, `Type::DIMS_MISMATCH_CVECTOR`, `Type::DIMS_MISMATCH_RVECTOR`,
`Type::DIMS_MISMATCH_VECTOR`,
`Type::SUBSYS_MISMATCH_DIMS`, `Type::PERM_INVALID`, `Type::PERM_MISMATCH_DIMS`, `Type::NOT_QUBIT_MATRIX`,
`Type::NOT_QUBIT_CVECTOR`, `Type::NOT_QUBIT_RVECTOR`, `Type::NOT_QUBIT_VECTOR`, `Type::NOT_QUBIT_SUBSYS`,
`Type::NOT_BIPARTITE`, `Type::NO_CODEWORD`, `Type::OUT_OF_RANGE`, `Type::TYPE_MISMATCH`,
`Type::SIZE_MISMATCH`, `Type::UNDEFINED_TYPE`, `Type::CUSTOM_EXCEPTION` }

Exception types, add more here if needed.

Public Member Functions

- `Exception` (const std::string &where, const `Type` &type)
Constructs an exception.
- `Exception` (const std::string &where, const std::string &custom)
Constructs an exception.
- virtual const char * `what` () const noexceptoverride
Overrides std::exception::what()

Private Member Functions

- void `_construct_exception_msg` ()
Constructs the exception description from its type.

Private Attributes

- std::string `_where`
- std::string `_msg`
- `Type _type`
- std::string `_custom`

7.3.1 Detailed Description

Generates custom exceptions, used when validating function parameters.

Customize this class if more exceptions are needed

7.3.2 Member Enumeration Documentation

7.3.2.1 enum qpp::Exception::Type [strong]

Exception types, add more here if needed.

See also

[qpp::Exception::_construct_exception_msg\(\)](#)

Enumerator

UNKNOWN_EXCEPTION Unknown exception

ZERO_SIZE Zero sized object, e.g. empty Eigen::Matrix or std::vector<> with no elements

MATRIX_NOT_SQUARE Eigen::Matrix is not square

MATRIX_NOT_CVECTOR Eigen::Matrix is not a column vector

MATRIX_NOT_RVECTOR Eigen::Matrix is not a row vector

MATRIX_NOT_VECTOR Eigen::Matrix is not a row/column vector

MATRIX_NOT_SQUARE_OR_CVECTOR Eigen::Matrix is not square nor a column vector

MATRIX_NOT_SQUARE_OR_RVECTOR Eigen::Matrix is not square nor a row vector

MATRIX_NOT_SQUARE_OR_VECTOR Eigen::Matrix is not square nor a row/column vector

MATRIX_MISMATCH_SUBSYS Matrix size mismatch subsystem sizes (e.g. in [qpp::apply\(\)](#))

DIMS_INVALID std::vector<idx> of dimensions has zero size or contains zeros

DIMS_NOT_EQUAL Local/global dimensions are not equal

DIMS_MISMATCH_MATRIX Product of the elements of std::vector<idx> of dimensions is not equal to the number of rows of Eigen::Matrix (assumed to be a square matrix)

DIMS_MISMATCH_CVECTOR Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a column vector)

DIMS_MISMATCH_RVECTOR Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a row vector)

DIMS_MISMATCH_VECTOR Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a row/column vector)

SUBSYS_MISMATCH_DIMS std::vector<idx> of subsystem labels has duplicates, or has entries that are larger than the size of the std::vector<idx> of dimensions

PERM_INVALID std::vector<idx> does not represent a valid permutation

PERM_MISMATCH_DIMS Size of the std::vector<idx> representing the permutation is different from the size of the std::vector<idx> of dimensions

NOT_QUBIT_MATRIX Eigen::Matrix is not 2 x 2

NOT_QUBIT_CVECTOR Eigen::Matrix is not 2 x 1

NOT_QUBIT_RVECTOR Eigen::Matrix is not 1 x 2

NOT_QUBIT_VECTOR Eigen::Matrix is not 1 x 2 nor 2 x 1

NOT_QUBIT_SUBSYS Subsystems are not 2-dimensional

NOT_BIPARTITE std::vector<idx> of dimensions has size different from 2

NO_CODEWORD Codeword does not exist, thrown when calling [qpp::Codes::codeword\(\)](#) with invalid index *i*

OUT_OF_RANGE Parameter out of range

TYPE_MISMATCH Scalar types do not match

SIZE_MISMATCH Sizes do not match

UNDEFINED_TYPE Templatized specialization not defined for this type

CUSTOM_EXCEPTION Custom exception, user must provide a custom message

7.3.3 Constructor & Destructor Documentation

7.3.3.1 `qpp::Exception::Exception (const std::string & where, const Type & type) [inline]`

Constructs an exception.

Parameters

<i>where</i>	Text representing where the exception occurred
<i>type</i>	Exception type, defined in qpp::Exception::Type

7.3.3.2 qpp::Exception::Exception (const std::string & *where*, const std::string & *custom*) [inline]

Constructs an exception.

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

Parameters

<i>where</i>	Text representing where the exception occurred
<i>custom</i>	Exception description

7.3.4 Member Function Documentation**7.3.4.1 void qpp::Exception::_construct_exception_msg() [inline], [private]**

Constructs the exception description from its type.

See also

[qpp::Exception::Type](#)

Must modify the code of this function if more exceptions are added

7.3.4.2 virtual const char* qpp::Exception::what() const [inline], [override], [virtual], [noexcept]

Overrides std::exception::what()

Returns

[Exception](#) description

7.3.5 Member Data Documentation**7.3.5.1 std::string qpp::Exception::_custom [private]****7.3.5.2 std::string qpp::Exception::_msg [private]****7.3.5.3 Type qpp::Exception::_type [private]****7.3.5.4 std::string qpp::Exception::_where [private]**

The documentation for this class was generated from the following file:

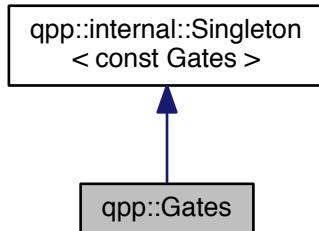
- classes/[exception.h](#)

7.4 qpp::Gates Class Reference

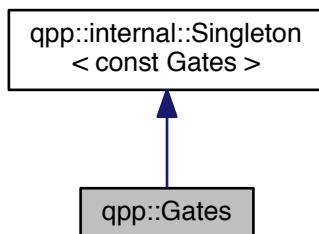
const Singleton class that implements most commonly used gates

```
#include <classes/gates.h>
```

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



Public Member Functions

- `cmat Rn (double theta, const std::vector< double > &n) const`
Rotation of theta about the 3-dimensional real unit vector n.
- `cmat Zd (idx D) const`
Generalized Z gate for qudits.
- `cmat Fd (idx D) const`
Fourier transform gate for qudits.
- `cmat Xd (idx D) const`
Generalized X gate for qudits.
- template<typename Derived = Eigen::MatrixXcd>
`Derived Id (idx D) const`
Identity gate.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx n, idx d=2) const`
Generates the multi-partite multiple-controlled-A gate in matrix form.

- template<typename Derived>
`dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::vector< idx > &dims) const`
Expands out.

Public Attributes

- `cmat Id2` {cmat::Identity(2, 2)}
Identity gate.
- `cmat H` {cmat::Zero(2, 2)}
Hadamard gate.
- `cmat X` {cmat::Zero(2, 2)}
Pauli Sigma-X gate.
- `cmat Y` {cmat::Zero(2, 2)}
Pauli Sigma-Y gate.
- `cmat Z` {cmat::Zero(2, 2)}
Pauli Sigma-Z gate.
- `cmat S` {cmat::Zero(2, 2)}
S gate.
- `cmat T` {cmat::Zero(2, 2)}
T gate.
- `cmat CNOT` {cmat::Identity(4, 4)}
Controlled-NOT control target gate.
- `cmat CZ` {cmat::Identity(4, 4)}
Controlled-Phase gate.
- `cmat CNOTba` {cmat::Zero(4, 4)}
Controlled-NOT target control gate.
- `cmat SWAP` {cmat::Identity(4, 4)}
SWAP gate.
- `cmat TOF` {cmat::Identity(8, 8)}
Toffoli gate.
- `cmat FRED` {cmat::Identity(8, 8)}
Fredkin gate.

Private Member Functions

- `Gates ()`
Initializes the gates.
- `~Gates ()=default`
Default destructor.

Friends

- class `internal::Singleton< const Gates >`

Additional Inherited Members

7.4.1 Detailed Description

const Singleton class that implements most commonly used gates

7.4.2 Constructor & Destructor Documentation

7.4.2.1 `qpp::Gates::Gates() [inline], [private]`

Initializes the gates.

7.4.2.2 `qpp::Gates::~Gates() [private], [default]`

Default destructor.

7.4.3 Member Function Documentation

7.4.3.1 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::Gates::CTRL(const Eigen::MatrixBase<Derived> & A, const std::vector<idx> & ctrl, const std::vector<idx> & subsys, idx n, idx d = 2) const [inline]`

Generates the multi-partite multiple-controlled-*A* gate in matrix form.

See also

[qpp::applyCTRL\(\)](#)

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>n</i>	Total number of subsystems
<i>d</i>	Subsystem dimensions

Returns

CTRL-*A* gate, as a matrix over the same scalar field as *A*

7.4.3.2 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::Gates::expandout(const Eigen::MatrixBase<Derived> & A, idx pos, const std::vector<idx> & dims) const [inline]`

Expands out.

See also

[qpp::kron\(\)](#)

Expands out *A* as a matrix in a multi-partite system. Faster than using [qpp::kron\(I, I, ..., I, A, I, ..., I\)](#).

Parameters

<i>A</i>	Eigen expression
----------	------------------

<i>pos</i>	Position
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with A on position *pos*, as a dynamic matrix over the same scalar field as A

7.4.3.3 cmat qpp::Gates::Fd (idx *D*) const [inline]

Fourier transform gate for qudits.

Note

Defined as $F = \sum_{jk} \exp(2\pi i j k / D) |j\rangle\langle k|$

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Fourier transform gate for qudits

7.4.3.4 template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id (idx *D*) const [inline]

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Identity gate

7.4.3.5 cmat qpp::Gates::Rn (double *theta*, const std::vector< double > & *n*) const [inline]

Rotation of *theta* about the 3-dimensional real unit vector *n*.

Parameters

<i>theta</i>	Rotation angle
<i>n</i>	3-dimensional real unit vector

Returns

Rotation gate

7.4.3.6 `cmat qpp::Gates::Xd (idx D) const [inline]`

Generalized X gate for qudits.

Note

Defined as $X = \sum_j |j \oplus 1\rangle\langle j|$

Parameters

D	Dimension of the Hilbert space
-----	--------------------------------

Returns

Generalized X gate for qudits

7.4.3.7 `cmat qpp::Gates::Zd (idx D) const [inline]`

Generalized Z gate for qudits.

Note

Defined as $Z = \sum_j \exp(2\pi ij/D) |j\rangle\langle j|$

Parameters

D	Dimension of the Hilbert space
-----	--------------------------------

Returns

Generalized Z gate for qudits

7.4.4 Friends And Related Function Documentation

7.4.4.1 friend class `internal::Singleton< const Gates >` [friend]

7.4.5 Member Data Documentation

7.4.5.1 `cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}`

Controlled-NOT control target gate.

7.4.5.2 `cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}`

Controlled-NOT target control gate.

7.4.5.3 `cmat qpp::Gates::CZ {cmat::Identity(4, 4)}`

Controlled-Phase gate.

7.4.5.4 `cmat qpp::Gates::FRED {cmat::Identity(8, 8)}`

Fredkin gate.

7.4.5.5 cmat qpp::Gates::H {cmat::Zero(2, 2)}

Hadamard gate.

7.4.5.6 cmat qpp::Gates::Id2 {cmat::Identity(2, 2)}

Identity gate.

7.4.5.7 cmat qpp::Gates::S {cmat::Zero(2, 2)}

S gate.

7.4.5.8 cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}

SWAP gate.

7.4.5.9 cmat qpp::Gates::T {cmat::Zero(2, 2)}

T gate.

7.4.5.10 cmat qpp::Gates::TOF {cmat::Identity(8, 8)}

Toffoli gate.

7.4.5.11 cmat qpp::Gates::X {cmat::Zero(2, 2)}

Pauli Sigma-X gate.

7.4.5.12 cmat qpp::Gates::Y {cmat::Zero(2, 2)}

Pauli Sigma-Y gate.

7.4.5.13 cmat qpp::Gates::Z {cmat::Zero(2, 2)}

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

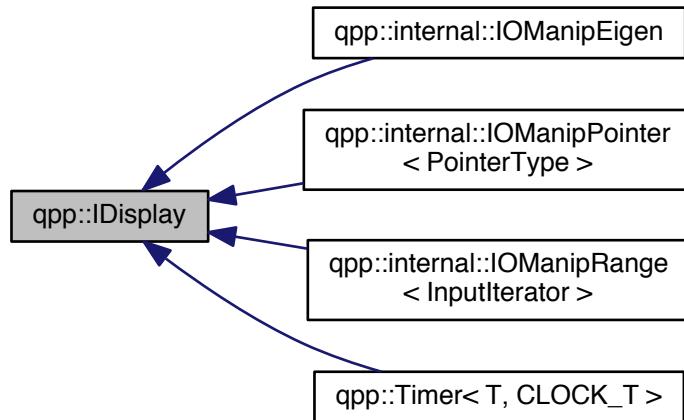
- [classes/gates.h](#)

7.5 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual std::ostream& [display\(std::ostream& os\) const](#).

```
#include <classes/idisplay.h>
```

Inheritance diagram for `qpp::IDisplay`:



Public Member Functions

- `IDisplay ()=default`
Default constructor.
- `IDisplay (const IDisplay &)=default`
Default copy constructor.
- `IDisplay (IDisplay &&)=default`
Default move constructor.
- `IDisplay & operator= (const IDisplay &)=default`
Default copy assignment operator.
- `IDisplay & operator= (IDisplay &&)=default`
Default move assignment operator.
- `virtual ~IDisplay ()=default`
Default virtual destructor.

Private Member Functions

- `virtual std::ostream & display (std::ostream &os) const =0`
Must be overridden by all derived classes.

Friends

- `std::ostream & operator<< (std::ostream &os, const IDisplay &rhs)`
Overloads the extraction operator.

7.5.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual std::ostream& `display(std::ostream& os) const`.

This class defines friend inline std::ostream& operator<< (std::ostream& os, const `qpp::IDisplay& rhs`). The latter delegates the work to the pure virtual function `qpp::IDisplay::display()` which has to be overridden by all derived classes.

7.5.2 Constructor & Destructor Documentation

7.5.2.1 `qpp::IDisplay::IDisplay() [default]`

Default constructor.

7.5.2.2 `qpp::IDisplay::IDisplay(const IDisplay &) [default]`

Default copy constructor.

7.5.2.3 `qpp::IDisplay::IDisplay(IDisplay &&) [default]`

Default move constructor.

7.5.2.4 `virtual qpp::IDisplay::~IDisplay() [virtual], [default]`

Default virtual destructor.

7.5.3 Member Function Documentation

7.5.3.1 `virtual std::ostream& qpp::IDisplay::display(std::ostream & os) const [private], [pure virtual]`

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const `IDisplay& rhs`).

Implemented in `qpp::internal::IOManipEigen`, `qpp::internal::IOManipPointer< PointerType >`, `qpp::internal::IOManipRange< InputIterator >`, and `qpp::Timer< T, CLOCK_T >`.

7.5.3.2 `IDisplay& qpp::IDisplay::operator=(const IDisplay &) [default]`

Default copy assignment operator.

7.5.3.3 `IDisplay& qpp::IDisplay::operator=(IDisplay &&) [default]`

Default move assignment operator.

7.5.4 Friends And Related Function Documentation

7.5.4.1 `std::ostream& operator<<(std::ostream & os, const IDisplay & rhs) [friend]`

Overloads the extraction operator.

Delegates the work to the virtual function `qpp::IDisplay::display()`

The documentation for this class was generated from the following file:

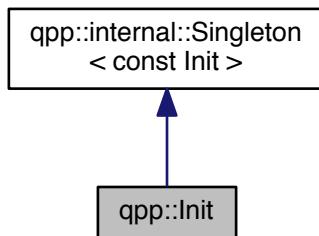
- [classes/idisplay.h](#)

7.6 `qpp::Init` Class Reference

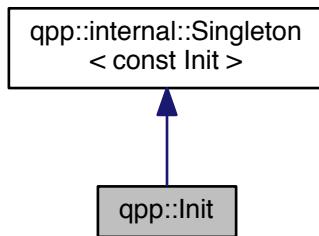
const Singleton class that performs additional initializations/cleanups

```
#include <classes/init.h>
```

Inheritance diagram for `qpp::Init`:



Collaboration diagram for `qpp::Init`:



Private Member Functions

- [`Init \(\)`](#)
Additional initializations.
- [`~Init \(\)`](#)
Cleanups.

Friends

- class [internal::Singleton< const Init >](#)

Additional Inherited Members

7.6.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

7.6.2 Constructor & Destructor Documentation

7.6.2.1 `qpp::Init::Init() [inline], [private]`

Additional initializations.

7.6.2.2 `qpp::Init::~Init() [inline], [private]`

Cleanups.

7.6.3 Friends And Related Function Documentation

7.6.3.1 friend class `internal::Singleton< const Init >` [friend]

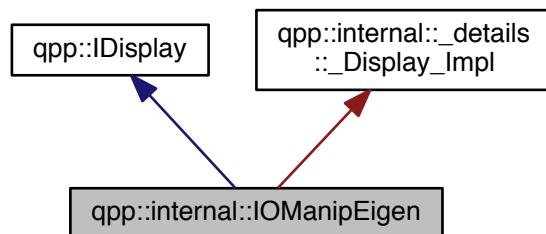
The documentation for this class was generated from the following file:

- [classes/init.h](#)

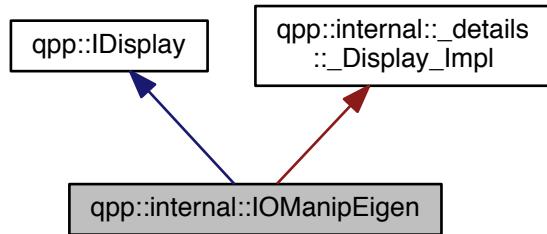
7.7 `qpp::internal::IOManipEigen` Class Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for `qpp::internal::IOManipEigen`:



Collaboration diagram for `qpp::internal::IOManipEigen`:



Public Member Functions

- template<typename Derived > `IOManipEigen` (const Eigen::MatrixBase< Derived > &A, double `chop=qpp::chop`)
- `IOManipEigen` (const `cplx` z, double `chop=qpp::chop`)

Private Member Functions

- `std::ostream & display (std::ostream &os) const override`
Must be overridden by all derived classes.

Private Attributes

- `cmat _A`
- double `_chop`

7.7.1 Constructor & Destructor Documentation

- 7.7.1.1 template<typename Derived > `qpp::internal::IOManipEigen::IOManipEigen (const Eigen::MatrixBase< Derived > &A, double chop = qpp::chop)` [inline], [explicit]
- 7.7.1.2 `qpp::internal::IOManipEigen::IOManipEigen (const cplx z, double chop = qpp::chop)` [inline], [explicit]

7.7.2 Member Function Documentation

- 7.7.2.1 `std::ostream& qpp::internal::IOManipEigen::display (std::ostream & os) const` [inline], [override], [private], [virtual]

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.
 Implements `qpp::IDisplay`.

7.7.3 Member Data Documentation

7.7.3.1 `cmat qpp::internal::IOManipEigen::_A` [private]

7.7.3.2 `double qpp::internal::IOManipEigen::_chop` [private]

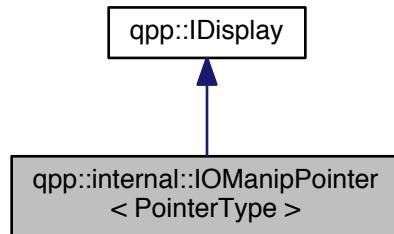
The documentation for this class was generated from the following file:

- `internal/classes/iomanip.h`

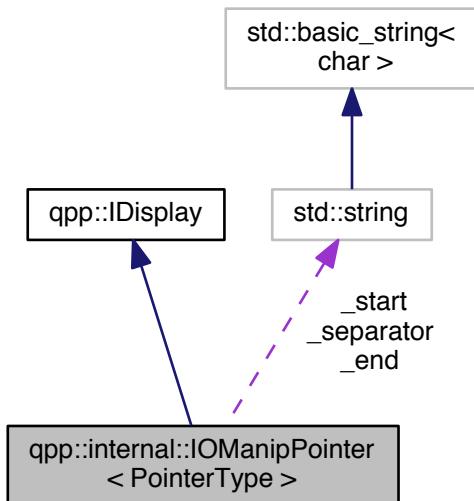
7.8 `qpp::internal::IOManipPointer< PointerType >` Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for `qpp::internal::IOManipPointer< PointerType >`:



Collaboration diagram for `qpp::internal::IOManipPointer< PointerType >`:



Public Member Functions

- `IOManipPointer` (const PointerType *`p`, `idx n`, const std::string &`separator`, const std::string &`start="["`, const std::string &`end="]"`)
- `IOManipPointer` (const `IOManipPointer` &)=default
- `IOManipPointer & operator=` (const `IOManipPointer` &)=default

Private Member Functions

- `std::ostream & display` (`std::ostream &os`) const override
Must be overridden by all derived classes.

Private Attributes

- `const PointerType * _p`
- `idx _n`
- `std::string _separator`
- `std::string _start`
- `std::string _end`

7.8.1 Constructor & Destructor Documentation

- 7.8.1.1 `template<typename PointerType> qpp::internal::IOManipPointer< PointerType >::IOManipPointer (const PointerType * p, idx n, const std::string & separator, const std::string & start = " [", const std::string & end = "] ") [inline], [explicit]`
- 7.8.1.2 `template<typename PointerType> qpp::internal::IOManipPointer< PointerType >::IOManipPointer (const IOManipPointer< PointerType > &) [default]`

7.8.2 Member Function Documentation

- 7.8.2.1 `template<typename PointerType> std::ostream& qpp::internal::IOManipPointer< PointerType >::display (std::ostream & os) const [inline], [override], [private], [virtual]`

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements `qpp::IDisplay`.

- 7.8.2.2 `template<typename PointerType> IOManipPointer& qpp::internal::IOManipPointer< PointerType >::operator= (const IOManipPointer< PointerType > &) [default]`

7.8.3 Member Data Documentation

- 7.8.3.1 `template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::_end [private]`
- 7.8.3.2 `template<typename PointerType> idx qpp::internal::IOManipPointer< PointerType >::_n [private]`
- 7.8.3.3 `template<typename PointerType> const PointerType* qpp::internal::IOManipPointer< PointerType >::_p [private]`

7.8.3.4 `template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::_separator`
`[private]`

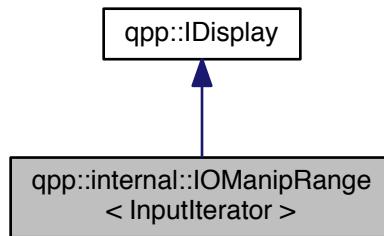
7.8.3.5 `template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::_start`
`[private]`

The documentation for this class was generated from the following file:

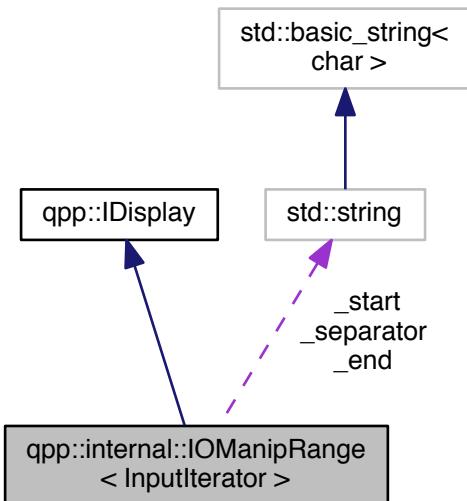
- `internal/classes/iomanip.h`

7.9 `qpp::internal::IOManipRange< InputIterator >` Class Template Reference

```
#include <internal/classes/iomanip.h>
Inheritance diagram for qpp::internal::IOManipRange< InputIterator >:
```



Collaboration diagram for qpp::internal::IOManipRange< InputIterator >:



Public Member Functions

- `IOManipRange` (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[, const std::string &end="])
- `IOManipRange` (const `IOManipRange` &)=default
- `IOManipRange & operator=` (const `IOManipRange` &)=default

Private Member Functions

- `std::ostream & display` (`std::ostream &os`) const override
Must be overridden by all derived classes.

Private Attributes

- `InputIterator _first`
- `InputIterator _last`
- `std::string _separator`
- `std::string _start`
- `std::string _end`

7.9.1 Constructor & Destructor Documentation

- 7.9.1.1 `template<typename InputIterator> qpp::internal::IOManipRange< InputIterator >::IOManipRange (InputIterator first, InputIterator last, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")` [inline], [explicit]
- 7.9.1.2 `template<typename InputIterator> qpp::internal::IOManipRange< InputIterator >::IOManipRange (const IOManipRange< InputIterator > &)` [default]

7.9.2 Member Function Documentation

- 7.9.2.1 `template<typename InputIterator> std::ostream& qpp::internal::IOManipRange< InputIterator >::display (std::ostream & os) const` [inline], [override], [private], [virtual]

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements `qpp::IDisplay`.

- 7.9.2.2 `template<typename InputIterator> IOManipRange& qpp::internal::IOManipRange< InputIterator >::operator= (const IOManipRange< InputIterator > &)` [default]

7.9.3 Member Data Documentation

- 7.9.3.1 `template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::_end` [private]

- 7.9.3.2 `template<typename InputIterator> InputIterator qpp::internal::IOManipRange< InputIterator >::_first` [private]

- 7.9.3.3 `template<typename InputIterator> InputIterator qpp::internal::IOManipRange< InputIterator >::_last` [private]

7.9.3.4 template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::_separator
[private]

7.9.3.5 template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::_start
[private]

The documentation for this class was generated from the following file:

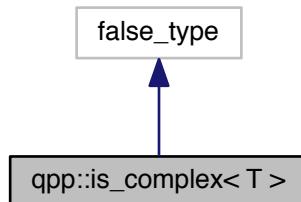
- [internal/classes/iomanip.h](#)

7.10 qpp::is_complex< T > Struct Template Reference

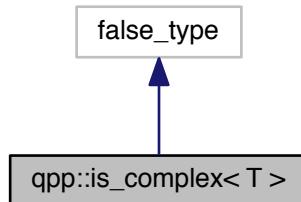
Checks whether the type is a complex type.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_complex< T >:



Collaboration diagram for qpp::is_complex< T >:



7.10.1 Detailed Description

```
template<typename T>struct qpp::is_complex< T >
```

Checks whether the type is a complex type.

Provides the member constant *value* which is equal to *true*, if the type is a complex type (i.e. `std::complex< T >`)

The documentation for this struct was generated from the following file:

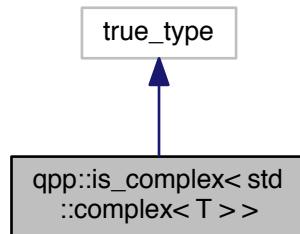
- [traits.h](#)

7.11 `qpp::is_complex< std::complex< T > >` Struct Template Reference

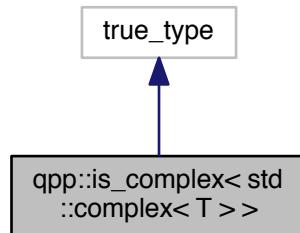
Checks whether the type is a complex number type, specialization for complex types.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_complex< std::complex< T > >`:



Collaboration diagram for `qpp::is_complex< std::complex< T > >`:



7.11.1 Detailed Description

```
template<typename T>struct qpp::is_complex< std::complex< T > >
```

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

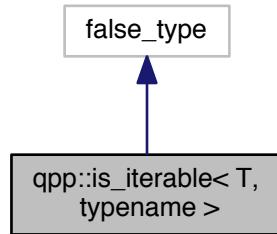
- [traits.h](#)

7.12 `qpp::is_iterable< T, typename >` Struct Template Reference

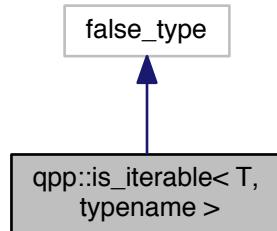
Checks whether T is compatible with an STL-like iterable container.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_iterable< T, typename >`:



Collaboration diagram for `qpp::is_iterable< T, typename >`:



7.12.1 Detailed Description

```
template<typename T, typename = void>struct qpp::is_iterable< T, typename >
```

Checks whether T is compatible with an STL-like iterable container.

Provides the member constant `value` which is equal to `true`, if T is compatible with an iterable container, i.e. provides at least `begin()` and `end()` member functions. Otherwise, `value` is equal to `false`.

The documentation for this struct was generated from the following file:

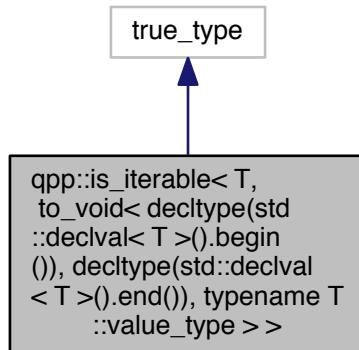
- [traits.h](#)

7.13 `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >` Struct Template Reference

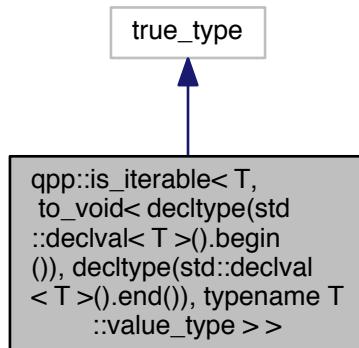
Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >`:



Collaboration diagram for `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >`:



7.13.1 Detailed Description

```
template<typename T>struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >
```

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

The documentation for this struct was generated from the following file:

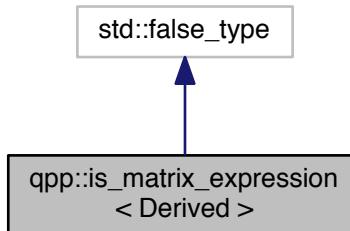
- [traits.h](#)

7.14 qpp::is_matrix_expression< Derived > Struct Template Reference

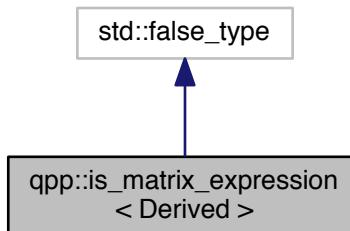
Checks whether the type is an Eigen matrix expression.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_matrix_expression< Derived >:



Collaboration diagram for qpp::is_matrix_expression< Derived >:



7.14.1 Detailed Description

```
template<typename Derived>struct qpp::is_matrix_expression< Derived >
```

Checks whether the type is an Eigen matrix expression.

Provides the member constant *value* which is equal to *true*, if the type is an Eigen matrix expression of type `Eigen::MatrixBase<Derived>`. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

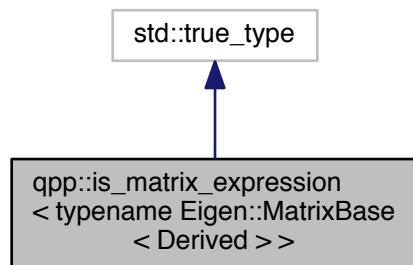
- [traits.h](#)

7.15 `qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >` Struct Template Reference

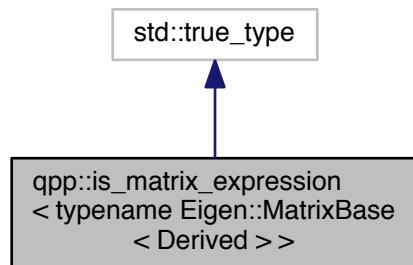
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >`:



Collaboration diagram for `qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >`:



7.15.1 Detailed Description

```
template<typename Derived>struct qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >
```

Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

The documentation for this struct was generated from the following file:

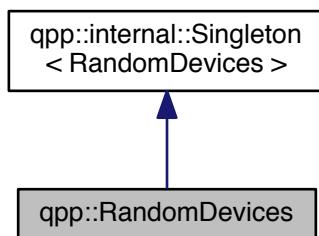
- [traits.h](#)

7.16 qpp::RandomDevices Class Reference

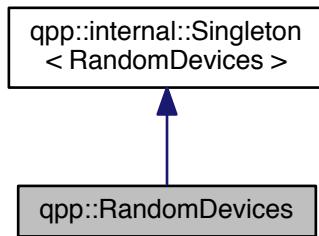
Singleton class that manages the source of randomness in the library.

```
#include <classes/random_devices.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



Public Attributes

- `std::mt19937 _rng`

Mersenne twister random number generator.

Private Member Functions

- `RandomDevices ()`

Initializes and seeds the random number generators.

- `~RandomDevices ()=default`
Default destructor.

Private Attributes

- `std::random_device _rd`
used to seed std::mt19937 _rng

Friends

- class `internal::Singleton< RandomDevices >`

Additional Inherited Members

7.16.1 Detailed Description

Singeleton class that manages the source of randomness in the library.

Consists of a wrapper around an `std::mt19937` Mersenne twister random number generator engine and an `std::random_device` engine. The latter is used to seed the Mersenne twister.

Warning

This class DOES NOT seed the standard C number generator used by `Eigen::Matrix::Random()`, since it is not thread safe. Do not use `Eigen::Matrix::Random()` or functions that depend on the C style random number engine, but use `qpp::rand()` instead!

7.16.2 Constructor & Destructor Documentation

7.16.2.1 qpp::RandomDevices::RandomDevices () [inline], [private]

Initializes and seeds the random number generators.

7.16.2.2 qpp::RandomDevices::~RandomDevices () [private], [default]

Default destructor.

7.16.3 Friends And Related Function Documentation

7.16.3.1 friend class `internal::Singleton< RandomDevices >` [friend]

7.16.4 Member Data Documentation

7.16.4.1 std::random_device qpp::RandomDevices::_rd [private]

used to seed `std::mt19937 _rng`

7.16.4.2 std::mt19937 qpp::RandomDevices::_rng

Mersenne twister random number generator.

The documentation for this class was generated from the following file:

- `classes/random_devices.h`

7.17 qpp::internal::Singleton< T > Class Template Reference

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

Static Public Member Functions

- static T & [get_instance](#) () noexcept(std::is_nothrow_constructible< T >::value)
- static thread_local T & [get_thread_local_instance](#) () noexcept(std::is_nothrow_constructible< T >::value)

Protected Member Functions

- [Singleton](#) () noexcept=default
- [Singleton](#) (const [Singleton](#) &)=delete
- [Singleton](#) & [operator=](#) (const [Singleton](#) &)=delete
- virtual ~[Singleton](#) ()=default

7.17.1 Detailed Description

```
template<typename T> class qpp::internal::Singleton< T >
```

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from [qpp::internal::Singleton](#), make [qpp::internal::Singleton](#) a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function [qpp::internal::Singleton::get_instance\(\)](#) ([qpp::internal::Singleton::get_thread_local_instance\(\)](#)), which returns a reference (thread_local reference) to your newly created singleton (thread-safe in C++11).

Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>
{
    friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
    ~MySingleton()
    {
        // Implement the destructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
thread_local MySingleton& tls = MySingleton::get_thread_local_instance();
// Get a thread_local instance
```

See also

Code of [qpp::Codes](#), [qpp::Gates](#), [qpp::Init](#), [qpp::RandomDevices](#), [qpp::States](#) or [qpp.h](#) for real world examples of usage.

7.17.2 Constructor & Destructor Documentation

7.17.2.1 `template<typename T> qpp::internal::Singleton< T >::Singleton() [protected], [default], [noexcept]`

7.17.2.2 `template<typename T> qpp::internal::Singleton< T >::Singleton(const Singleton< T > &) [protected], [delete]`

7.17.2.3 `template<typename T> virtual qpp::internal::Singleton< T >::~Singleton() [protected], [virtual], [default]`

7.17.3 Member Function Documentation

7.17.3.1 `template<typename T> static T& qpp::internal::Singleton< T >::get_instance() [inline], [static], [noexcept]`

7.17.3.2 `template<typename T> static thread_local T& qpp::internal::Singleton< T >::get_thread_local_instance() [inline], [static], [noexcept]`

7.17.3.3 `template<typename T> Singleton& qpp::internal::Singleton< T >::operator=(const Singleton< T > &) [protected], [delete]`

The documentation for this class was generated from the following file:

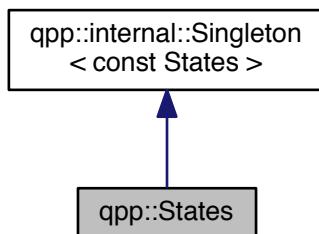
- internal/classes/[singleton.h](#)

7.18 qpp::States Class Reference

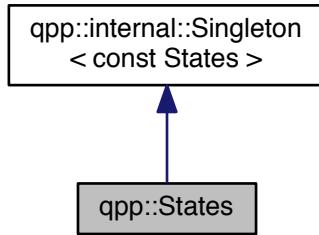
const Singleton class that implements most commonly used states

```
#include <classes/states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



Public Attributes

- **ket x0** {ket::Zero(2)}
Pauli Sigma-X 0-eigenstate $|+\rangle$
- **ket x1** {ket::Zero(2)}
Pauli Sigma-X 1-eigenstate $|-\rangle$
- **ket y0** {ket::Zero(2)}
Pauli Sigma-Y 0-eigenstate $|y+\rangle$
- **ket y1** {ket::Zero(2)}
Pauli Sigma-Y 1-eigenstate $|y-\rangle$
- **ket z0** {ket::Zero(2)}
Pauli Sigma-Z 0-eigenstate $|0\rangle$
- **ket z1** {ket::Zero(2)}
Pauli Sigma-Z 1-eigenstate $|1\rangle$
- **cmat px0** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-X 0-eigenstate $|+\rangle\langle +|$.
- **cmat px1** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-X 1-eigenstate $|-\rangle\langle -|$.
- **cmat py0** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Y 0-eigenstate $|y+\rangle\langle y+|$.
- **cmat py1** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Y 1-eigenstate $|y-\rangle\langle y-|$.
- **cmat pz0** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Z 0-eigenstate $|0\rangle\langle 0|$.
- **cmat pz1** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Z 1-eigenstate $|1\rangle\langle 1|$.
- **ket b00** {ket::Zero(4)}
Bell-00 state (following the convention in Nielsen and Chuang)
- **ket b01** {ket::Zero(4)}
Bell-01 state (following the convention in Nielsen and Chuang)
- **ket b10** {ket::Zero(4)}
Bell-10 state (following the convention in Nielsen and Chuang)
- **ket b11** {ket::Zero(4)}
Bell-11 state (following the convention in Nielsen and Chuang)
- **cmat pb00** {cmat::Zero(4, 4)}

- **cmat pb01** {cmat::Zero(4, 4)}

Projector onto the Bell-00 state.

- **cmat pb10** {cmat::Zero(4, 4)}

Projector onto the Bell-01 state.

- **cmat pb11** {cmat::Zero(4, 4)}

Projector onto the Bell-10 state.

- **ket GHZ** {ket::Zero(8)}

GHZ state.

- **ket W** {ket::Zero(8)}

W state.

- **cmat pGHZ** {cmat::Zero(8, 8)}

Projector onto the GHZ state.

- **cmat pW** {cmat::Zero(8, 8)}

Projector onto the W state.

Private Member Functions

- **States ()**
 - **~States ()=default**
- Default destructor.*

Friends

- class **internal::Singleton< const States >**

Additional Inherited Members

7.18.1 Detailed Description

const Singleton class that implements most commonly used states

7.18.2 Constructor & Destructor Documentation

7.18.2.1 **qpp::States::States()** [inline], [private]

Initialize the states

7.18.2.2 **qpp::States::~States()** [private], [default]

Default destructor.

7.18.3 Friends And Related Function Documentation

7.18.3.1 **friend class internal::Singleton< const States >** [friend]

7.18.4 Member Data Documentation

7.18.4.1 **ket qpp::States::b00** {ket::Zero(4)}

Bell-00 state (following the convention in Nielsen and Chuang)

7.18.4.2 ket qpp::States::b01 {ket::Zero(4)}

Bell-01 state (following the convention in Nielsen and Chuang)

7.18.4.3 ket qpp::States::b10 {ket::Zero(4)}

Bell-10 state (following the convention in Nielsen and Chuang)

7.18.4.4 ket qpp::States::b11 {ket::Zero(4)}

Bell-11 state (following the convention in Nielsen and Chuang)

7.18.4.5 ket qpp::States::GHZ {ket::Zero(8)}

GHZ state.

7.18.4.6 cmat qpp::States::pb00 {cmat::Zero(4, 4)}

Projector onto the Bell-00 state.

7.18.4.7 cmat qpp::States::pb01 {cmat::Zero(4, 4)}

Projector onto the Bell-01 state.

7.18.4.8 cmat qpp::States::pb10 {cmat::Zero(4, 4)}

Projector onto the Bell-10 state.

7.18.4.9 cmat qpp::States::pb11 {cmat::Zero(4, 4)}

Projector onto the Bell-11 state.

7.18.4.10 cmat qpp::States::pGHZ {cmat::Zero(8, 8)}

Projector onto the GHZ state.

7.18.4.11 cmat qpp::States::pW {cmat::Zero(8, 8)}

Projector onto the W state.

7.18.4.12 cmat qpp::States::px0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-X 0-eigenstate $|+><+|$.

7.18.4.13 cmat qpp::States::px1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-X 1-eigenstate $|-><-|$.

7.18.4.14 cmat qpp::States::py0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Y 0-eigenstate $|y+><y+|$.

7.18.4.15 cmat qpp::States::py1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Y 1-eigenstate $|y-><y-|$.

7.18.4.16 cmat qpp::States::pz0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Z 0-eigenstate $|0><0|$.

7.18.4.17 cmat qpp::States::pz1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Z 1-eigenstate $|1><1|$.

7.18.4.18 ket qpp::States::W {ket::Zero(8)}

W state.

7.18.4.19 ket qpp::States::x0 {ket::Zero(2)}

Pauli Sigma-X 0-eigenstate $|+>$

7.18.4.20 ket qpp::States::x1 {ket::Zero(2)}

Pauli Sigma-X 1-eigenstate $|->$

7.18.4.21 ket qpp::States::y0 {ket::Zero(2)}

Pauli Sigma-Y 0-eigenstate $|y+>$

7.18.4.22 ket qpp::States::y1 {ket::Zero(2)}

Pauli Sigma-Y 1-eigenstate $|y->$

7.18.4.23 ket qpp::States::z0 {ket::Zero(2)}

Pauli Sigma-Z 0-eigenstate $|0>$

7.18.4.24 ket qpp::States::z1 {ket::Zero(2)}

Pauli Sigma-Z 1-eigenstate $|1>$

The documentation for this class was generated from the following file:

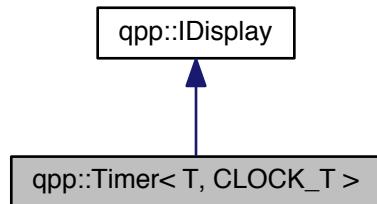
- [classes/states.h](#)

7.19 qpp::Timer< T, CLOCK_T > Class Template Reference

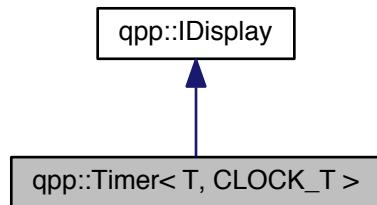
Chronometer.

```
#include <classes/timer.h>
```

Inheritance diagram for qpp::Timer< T, CLOCK_T >:



Collaboration diagram for qpp::Timer< T, CLOCK_T >:



Public Member Functions

- **Timer () noexcept**
Constructs an instance with the current time as the starting point.
- **void tic () noexcept**
Resets the chronometer.
- **const Timer & toc () noexcept**
Stops the chronometer.
- **double tics () const noexcept**
Time passed in the duration specified by T.
- template<typename U = T>
U get_duration () const noexcept
Duration specified by U.
- **Timer (const Timer &)=default**
Default copy constructor.
- **Timer (Timer &&)=default**

- `Timer & operator= (const Timer &) =default`
Default copy assignment operator.
- `Timer & operator= (Timer &&) =default`
Default move assignment operator.
- `virtual ~Timer () =default`
Default virtual destructor.

Protected Attributes

- `CLOCK_T::time_point _start`
- `CLOCK_T::time_point _end`

Private Member Functions

- `std::ostream & display (std::ostream &os) const override`
`qpp::IDisplay::display() override`

7.19.1 Detailed Description

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> class qpp::Timer<T, CLOCK_T >
```

Chronometer.

Template Parameters

<code>T</code>	Ticks duration, default is <code>std::chrono::duration<double, 1></code> i.e. seconds in double precision
<code>CLOCK_T</code>	Clock's type, default is <code>std::chrono::steady_clock</code> , not affected by wall clock changes during runtime

7.19.2 Constructor & Destructor Documentation

7.19.2.1 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> qpp::Timer<T, CLOCK_T >::Timer() [inline], [noexcept]`

Constructs an instance with the current time as the starting point.

7.19.2.2 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> qpp::Timer<T, CLOCK_T >::Timer(const Timer<T, CLOCK_T > &) [default]`

Default copy constructor.

7.19.2.3 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> qpp::Timer<T, CLOCK_T >::Timer(Timer<T, CLOCK_T > &&) [default]`

Default move constructor.

7.19.2.4 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> virtual qpp::Timer<T, CLOCK_T >::~Timer() [virtual], [default]`

Default virtual destructor.

7.19.3 Member Function Documentation

7.19.3.1 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> std::ostream& qpp::Timer< T, CLOCK_T >::display (std::ostream & os) const [inline], [override], [private], [virtual]`

`qpp::IDisplay::display()` override

Parameters

<code>os</code>	Output stream
-----------------	---------------

Returns

Writes to the output stream the number of tics (specified by T) that passed between the instantiation/reset and invocation of `qpp::Timer::toc()`.

Implements `qpp::IDisplay`.

7.19.3.2 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> template<typename U = T> U qpp::Timer< T, CLOCK_T >::get_duration () const [inline], [noexcept]`

Duration specified by U.

Template Parameters

<code>U</code>	Duration, default is T, which defaults to <code>std::chrono::duration<double, 1></code> , i.e. seconds in double precision
----------------	----------------------------------------------------------------------------------------------------------------------------------

Returns

Duration that passed between the instantiation/reset and invocation of `qpp::Timer::toc()`

7.19.3.3 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> Timer& qpp::Timer< T, CLOCK_T >::operator= (const Timer< T, CLOCK_T > &) [default]`

Default copy assignment operator.

7.19.3.4 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> Timer& qpp::Timer< T, CLOCK_T >::operator= (Timer< T, CLOCK_T > &&) [default]`

Default move assignment operator.

7.19.3.5 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> void qpp::Timer< T, CLOCK_T >::tic () [inline], [noexcept]`

Resets the chronometer.

Resets the starting/ending point to the current time

7.19.3.6 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> double qpp::Timer< T, CLOCK_T >::tics () const [inline], [noexcept]`

Time passed in the duration specified by T.

Returns

Number of tics (specified by T) that passed between the instantiation/reset and invocation of [qpp::Timer::toc\(\)](#)

7.19.3.7 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> const Timer& qpp::Timer<T, CLOCK_T>::toc() [inline], [noexcept]`

Stops the chronometer.

Set the current time as the ending point

Returns

Current instance

7.19.4 Member Data Documentation

7.19.4.1 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> CLOCK_T::time_point qpp::Timer<T, CLOCK_T>::_end [protected]`

7.19.4.2 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> CLOCK_T::time_point qpp::Timer<T, CLOCK_T>::_start [protected]`

The documentation for this class was generated from the following file:

- [classes/timer.h](#)

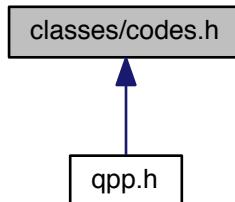
Chapter 8

File Documentation

8.1 classes/codes.h File Reference

Quantum error correcting codes.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Codes](#)
const Singleton class that defines quantum error correcting codes

Namespaces

- [qpp](#)
Quantum++ main namespace.

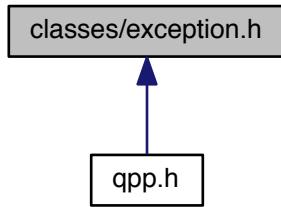
8.1.1 Detailed Description

Quantum error correcting codes.

8.2 classes/exception.h File Reference

Exceptions.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Exception](#)
Generates custom exceptions, used when validating function parameters.

Namespaces

- [qpp](#)
Quantum++ main namespace.

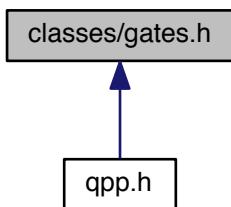
8.2.1 Detailed Description

Exceptions.

8.3 classes/gates.h File Reference

Quantum gates.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Gates](#)

const Singleton class that implements most commonly used gates

Namespaces

- [qpp](#)

Quantum++ main namespace.

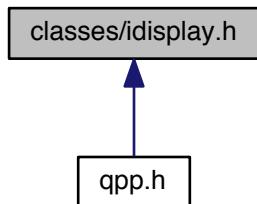
8.3.1 Detailed Description

Quantum gates.

8.4 classes/idisplay.h File Reference

Display interface via the non-virtual interface (NVI)

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::IDisplay](#)

Abstract class (interface) that mandates the definition of virtual std::ostream& `display(std::ostream& os) const`.

Namespaces

- [qpp](#)

Quantum++ main namespace.

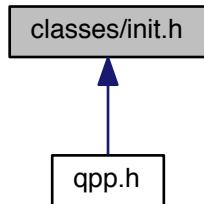
8.4.1 Detailed Description

Display interface via the non-virtual interface (NVI)

8.5 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Init](#)
const Singleton class that performs additional initializations/cleanups

Namespaces

- [qpp](#)
Quantum++ main namespace.

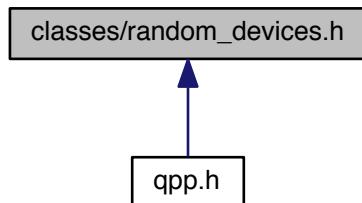
8.5.1 Detailed Description

Initialization.

8.6 classes/random_devices.h File Reference

Random devices.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::RandomDevices](#)

Singleton class that manages the source of randomness in the library.

Namespaces

- [qpp](#)

Quantum++ main namespace.

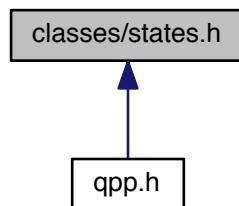
8.6.1 Detailed Description

Random devices.

8.7 classes/states.h File Reference

Quantum states.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::States](#)

const Singleton class that implements most commonly used states

Namespaces

- [qpp](#)

Quantum++ main namespace.

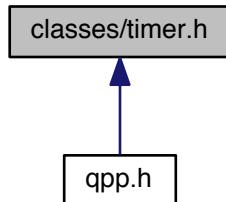
8.7.1 Detailed Description

Quantum states.

8.8 classes/timer.h File Reference

Timing.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Timer< T, CLOCK_T >](#)
Chronometer.

Namespaces

- [qpp](#)
Quantum++ main namespace.

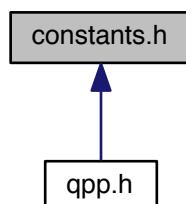
8.8.1 Detailed Description

Timing.

8.9 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Quantum++ main namespace.

Functions

- `constexpr cplx qpp::operator""_i` (`unsigned long long int x`) `noexcept`
User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- `constexpr cplx qpp::operator""_i` (`long double x`) `noexcept`
User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- `cplx qpp::omega` (`idx D`)
D-th root of unity.

Variables

- `constexpr double qpp::chop = 1e-10`
Used in `qpp::disp()` for setting to zero numbers that have their absolute value smaller than `qpp::chop`.
- `constexpr double qpp::eps = 1e-12`
Used to decide whether a number or expression in double precision is zero or not.
- `constexpr idx qpp::maxn = 64`
Maximum number of allowed qu(d)its (subsystems)
- `constexpr double qpp::pi = 3.141592653589793238462643383279502884`
 π
- `constexpr double qpp::ee = 2.718281828459045235360287471352662497`
Base of natural logarithm, e.
- `constexpr double qpp::infty = std::numeric_limits<double>::infinity()`
Used to denote infinity in double precision.

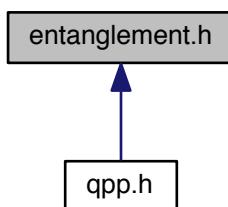
8.9.1 Detailed Description

Constants.

8.10 entanglement.h File Reference

Entanglement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Quantum++ main namespace.

Functions

- template<typename Derived>
`dyn_col_vect< double > qpp::schmidtcoeffs` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt coefficients of the bi-partite pure state A.

- template<typename Derived>
`cmat qpp::schmidtA` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt basis on Alice side.

- template<typename Derived>
`cmat qpp::schmidtB` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt basis on Bob side.

- template<typename Derived>
`std::vector< double > qpp::schmidtprobs` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt probabilities of the bi-partite pure state A.

- template<typename Derived>
`double qpp::entanglement` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Entanglement of the bi-partite pure state A.

- template<typename Derived>
`double qpp::gconcurrence` (const Eigen::MatrixBase< Derived > &A)

G-concurrence of the bi-partite pure state A.

- template<typename Derived>
`double qpp::negativity` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Negativity of the bi-partite mixed state A.

- template<typename Derived>
`double qpp::lognegativity` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Logarithmic negativity of the bi-partite mixed state A.

- template<typename Derived>
`double qpp::concence` (const Eigen::MatrixBase< Derived > &A)

Wootters concurrence of the bi-partite qubit mixed state A.

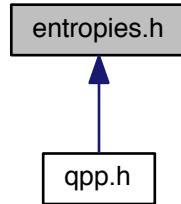
8.10.1 Detailed Description

Entanglement functions.

8.11 entropies.h File Reference

Entropy functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- template<typename Derived >
`double qpp::entropy (const Eigen::MatrixBase< Derived > &A)`
von-Neumann entropy of the density matrix A
- `double qpp::entropy (const std::vector< double > &prob)`
Shannon entropy of the probability distribution prob.
- template<typename Derived >
`double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)`
Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- `double qpp::renyi (const std::vector< double > &prob, double alpha)`
Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template<typename Derived >
`double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)`
Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- `double qpp::tsallis (const std::vector< double > &prob, double q)`
Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template<typename Derived >
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)`
Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived >
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)`
Quantum mutual information between 2 subsystems of a composite system.

8.11.1 Detailed Description

Entropy functions.

8.12 experimental/experimental.h File Reference

Experimental/test functions/classes.

Namespaces

- [qpp](#)
Quantum++ main namespace.
- [qpp::experimental](#)
Experimental/test functions/classes, do not use or modify.

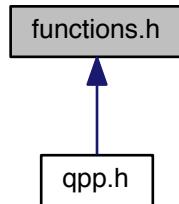
8.12.1 Detailed Description

Experimental/test functions/classes.

8.13 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- template<typename Derived >
`dyn_mat< typename Derived::Scalar > qpp::transpose` (const Eigen::MatrixBase< Derived > &A)
Transpose.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > qpp::conjugate` (const Eigen::MatrixBase< Derived > &A)
Complex conjugate.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > qpp::adjoint` (const Eigen::MatrixBase< Derived > &A)
Adjoint.

- template<typename Derived>
`dyn_mat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)`
Inverse.
- template<typename Derived>
`Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)`
Trace.
- template<typename Derived>
`Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)`
Determinant.
- template<typename Derived>
`Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)`
Logarithm of the determinant.
- template<typename Derived>
`Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)`
Element-wise sum of A.
- template<typename Derived>
`Derived::Scalar qpp::prod (const Eigen::MatrixBase< Derived > &A)`
Element-wise product of A.
- template<typename Derived>
`double qpp::norm (const Eigen::MatrixBase< Derived > &A)`
Frobenius norm.
- template<typename Derived>
`std::pair< dyn_col_vect< cplx >, cmat > qpp::eig (const Eigen::MatrixBase< Derived > &A)`
Full eigen decomposition.
- template<typename Derived>
`dyn_col_vect< cplx > qpp::evals (const Eigen::MatrixBase< Derived > &A)`
Eigenvalues.
- template<typename Derived>
`cmat qpp::evecs (const Eigen::MatrixBase< Derived > &A)`
Eigenvectors.
- template<typename Derived>
`std::pair< dyn_col_vect< double >, cmat > qpp::heig (const Eigen::MatrixBase< Derived > &A)`
Full eigen decomposition of Hermitian expression.
- template<typename Derived>
`dyn_col_vect< double > qpp::hevals (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvalues.
- template<typename Derived>
`cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvectors.
- template<typename Derived>
`std::tuple< cmat, dyn_col_vect< double >, cmat > qpp::svd (const Eigen::MatrixBase< Derived > &A)`
Full singular value decomposition.
- template<typename Derived>
`dyn_col_vect< double > qpp::svals (const Eigen::MatrixBase< Derived > &A)`
Singular values.
- template<typename Derived>
`cmat qpp::svdU (const Eigen::MatrixBase< Derived > &A)`
Left singular vectors.
- template<typename Derived>
`cmat qpp::svdV (const Eigen::MatrixBase< Derived > &A)`
Right singular vectors.
- template<typename Derived>
`cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))`

- Functional calculus f(A)*
- template<typename Derived >
cmat `qpp::sqrtm` (const Eigen::MatrixBase< Derived > &A)
Matrix square root.
 - template<typename Derived >
cmat `qpp::absm` (const Eigen::MatrixBase< Derived > &A)
Matrix absolut value.
 - template<typename Derived >
cmat `qpp::expm` (const Eigen::MatrixBase< Derived > &A)
Matrix exponential.
 - template<typename Derived >
cmat `qpp::logm` (const Eigen::MatrixBase< Derived > &A)
Matrix logarithm.
 - template<typename Derived >
cmat `qpp::sinm` (const Eigen::MatrixBase< Derived > &A)
Matrix sin.
 - template<typename Derived >
cmat `qpp::cosm` (const Eigen::MatrixBase< Derived > &A)
Matrix cos.
 - template<typename Derived >
cmat `qpp::spectralpowm` (const Eigen::MatrixBase< Derived > &A, const cplx z)
Matrix power.
 - template<typename Derived >
dyn_mat< typename Derived::Scalar > `qpp::powm` (const Eigen::MatrixBase< Derived > &A, idx n)
Matrix power.
 - template<typename Derived >
double `qpp::schatten` (const Eigen::MatrixBase< Derived > &A, double p)
Schatten matrix norm.
 - template<typename OutputScalar , typename Derived >
dyn_mat< OutputScalar > `qpp::cwise` (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename Derived::Scalar &))
Functor.
 - template<typename T >
dyn_mat< typename T::Scalar > `qpp::kron` (const T &head)
Kronecker product.
 - template<typename T , typename... Args>
dyn_mat< typename T::Scalar > `qpp::kron` (const T &head, const Args &...tail)
Kronecker product.
 - template<typename Derived >
dyn_mat< typename Derived::Scalar > `qpp::kron` (const std::vector< Derived > &As)
Kronecker product.
 - template<typename Derived >
dyn_mat< typename Derived::Scalar > `qpp::kron` (const std::initializer_list< Derived > &As)
Kronecker product.
 - template<typename Derived >
dyn_mat< typename Derived::Scalar > `qpp::kronpow` (const Eigen::MatrixBase< Derived > &A, idx n)
Kronecker power.
 - template<typename T >
dyn_mat< typename T::Scalar > `qpp::dirsum` (const T &head)
Direct sum.
 - template<typename T , typename... Args>
dyn_mat< typename T::Scalar > `qpp::dirsum` (const T &head, const Args &...tail)
Direct sum.

- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::vector< Derived > &As)
```

Direct sum.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::initializer_list< Derived > &As)
```

Direct sum.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)
```

Direct sum power.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)
```

Reshape.
- template<typename Derived1 , typename Derived2 >


```
dyn_mat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
```

Commutator.
- template<typename Derived1 , typename Derived2 >


```
dyn_mat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
```

Anti-commutator.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)
```

Projector.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs)
```

Gram-Schmidt orthogonalization.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &Vs)
```

Gram-Schmidt orthogonalization.
- template<typename Derived>


```
dyn_mat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)
```

Gram-Schmidt orthogonalization.
- std::vector< idx > qpp::n2multiidx (idx n, const std::vector< idx > &dims)

Non-negative integer index to multi-index.
- idx qpp::multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)

Multi-index to non-negative integer index.
- ket qpp::mket (const std::vector< idx > &mask, const std::vector< idx > &dims)

Multi-partite qudit ket.
- ket qpp::mket (const std::vector< idx > &mask, idx d=2)

Multi-partite qudit ket.
- cmat qpp::mpqr (const std::vector< idx > &mask, const std::vector< idx > &dims)

Projector onto multi-partite qudit ket.
- cmat qpp::mpqr (const std::vector< idx > &mask, idx d=2)

Projector onto multi-partite qudit ket.
- template<typename InputIterator >


```
std::vector< double > qpp::abssq (InputIterator first, InputIterator last)
```

Computes the absolute values squared of an STL-like range of complex numbers.
- template<typename Container >


```
std::vector< double > qpp::abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type * = nullptr)
```

Computes the absolute values squared of an STL-like container.

- template<typename Derived >
`std::vector< double > qpp::abssq (const Eigen::MatrixBase< Derived > &A)`
Computes the absolute values squared of an Eigen expression.
- template<typename InputIterator >
`std::iterator_traits< InputIterator >::value_type qpp::sum (InputIterator first, InputIterator last)`
Element-wise sum of an STL-like range.
- template<typename Container >
`Container::value_type qpp::sum (const Container &c)`
Element-wise sum of the elements of an STL-like container.
- template<typename InputIterator >
`std::iterator_traits< InputIterator >::value_type qpp::prod (InputIterator first, InputIterator last)`
Element-wise product of an STL-like range.
- template<typename Container >
`Container::value_type qpp::prod (const Container &c)`
Element-wise product of the elements of an STL-like container.
- template<typename Derived >
`dyn_col_vect< typename Derived::Scalar > qpp::rho2pure (const Eigen::MatrixBase< Derived > &A)`
Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- template<typename T >
`std::vector< T > qpp::complement (std::vector< T > subsys, idx N)`
Constructs the complement of a subsystem vector.
- template<typename Derived >
`std::vector< double > qpp::rho2bloch (const Eigen::MatrixBase< Derived > &A)`
Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- cmat [qpp::bloch2rho](#) (const std::vector< double > &r)
Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

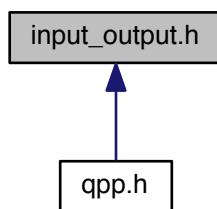
8.13.1 Detailed Description

Generic quantum computing functions.

8.14 input_output.h File Reference

Input/output functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Quantum++ main namespace.

Functions

- template<typename Derived >
internal::IOManipEigen `qpp::disp` (const Eigen::MatrixBase< Derived > &A, double chop=`qpp::chop`)

Eigen expression ostream manipulator.
- internal::IOManipEigen `qpp::disp` (cplx z, double chop=`qpp::chop`)

Complex number ostream manipulator.
- template<typename InputIterator >
internal::IOManipRange< InputIterator > `qpp::disp` (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[, const std::string &end="]"")

Range ostream manipulator.
- template<typename Container >
internal::IOManipRange< typename Container::const_iterator > `qpp::disp` (const Container &c, const std::string &separator, const std::string &start="[, const std::string &end="]"")

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template<typename PointerType >
internal::IOManipPointer< PointerType > `qpp::disp` (const PointerType *p, idx n, const std::string &separator, const std::string &start="[, const std::string &end="]"")

C-style pointer ostream manipulator.
- template<typename Derived >
void `qpp::save` (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

Saves Eigen expression to a binary file (internal format) in double precision.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > `qpp::load` (const std::string &fname)

Loads Eigen matrix from a binary file (internal format) in double precision.

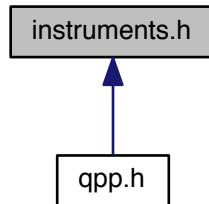
8.14.1 Detailed Description

Input/output functions.

8.15 instruments.h File Reference

Measurement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- template<typename Derived >
dyn_col_vect< typename Derived::Scalar > [qpp::ip](#) (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)
Generalized inner product.
- template<typename Derived >
dyn_col_vect< typename Derived::Scalar > [qpp::ip](#) (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)
Generalized inner product.
- template<typename Derived >
std::tuple< idx, std::vector< double >, std::vector< cmat > > [qpp::measure](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)
Measures the state A using the set of Kraus operators Ks.
- template<typename Derived >
std::tuple< idx, std::vector< double >, std::vector< cmat > > [qpp::measure](#) (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)
Measures the state A using the set of Kraus operators Ks.
- template<typename Derived >
std::tuple< idx, std::vector< double >, std::vector< cmat > > [qpp::measure](#) (const Eigen::MatrixBase< Derived > &A, const cmat &U)
Measures the state A in the orthonormal basis specified by the unitary matrix U.
- template<typename Derived >
std::tuple< idx, std::vector< double >, std::vector< cmat > > [qpp::measure](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
std::tuple< idx, std::vector< double >, std::vector< cmat > > [qpp::measure](#) (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- template<typename Derived>
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived>
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived>
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived>
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)`
Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived>
`std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)`
Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
- template<typename Derived>
`std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)`
Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

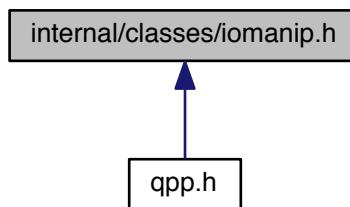
8.15.1 Detailed Description

Measurement functions.

8.16 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



Classes

- struct `qpp::internal::_details::_Display_Impl`
- class `qpp::internal::IOManipRange< InputIterator >`
- class `qpp::internal::IOManipPointer< PointerType >`
- class `qpp::internal::IOManipEigen`

Namespaces

- `qpp`
Quantum++ main namespace.
- `qpp::internal`
Internal utility functions, do not use/modify.
- `qpp::internal::_details`

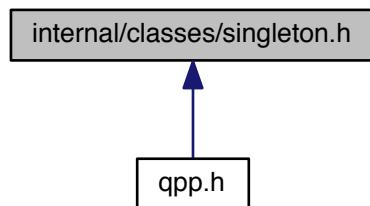
8.16.1 Detailed Description

Input/output manipulators.

8.17 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



Classes

- class `qpp::internal::Singleton< T >`
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Namespaces

- `qpp`
Quantum++ main namespace.
- `qpp::internal`
Internal utility functions, do not use/modify.

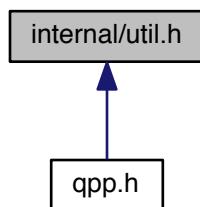
8.17.1 Detailed Description

Singleton pattern via CRTP.

8.18 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.
- [qpp::internal](#)
Internal utility functions, do not use/modify.

Functions

- void [qpp::internal::_n2multiidx](#) (idx n, idx numdims, const idx *dims, idx *result) noexcept
- idx [qpp::internal::_multiidx2n](#) (const idx *midx, idx numdims, const idx *dims) noexcept
- template<typename Derived >
 bool [qpp::internal::_check_square_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
 bool [qpp::internal::_check_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
 bool [qpp::internal::_check_rvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
 bool [qpp::internal::_check_cvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
 bool [qpp::internal::_check_nonzero_size](#) (const T &x) noexcept
- template<typename T1 , typename T2 >
 bool [qpp::internal::_check_matching_sizes](#) (const T1 &lhs, const T2 &rhs) noexcept
- bool [qpp::internal::_check_dims](#) (const std::vector< idx > &dims)
- template<typename Derived >
 bool [qpp::internal::_check_dims_match_mat](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
 bool [qpp::internal::_check_dims_match_cvect](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)

- template<typename Derived>
bool [qpp::internal::_check_dims_match_rvect](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)
- bool [qpp::internal::_check_eq_dims](#) (const std::vector< idx > &dims, idx dim) noexcept
- bool [qpp::internal::_check_subsys_match_dims](#) (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template<typename Derived>
bool [qpp::internal::_check_qubit_matrix](#) (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived>
bool [qpp::internal::_check_qubit_cvector](#) (const Eigen::MatrixBase< Derived > &V) noexcept
- template<typename Derived>
bool [qpp::internal::_check_qubit_rvector](#) (const Eigen::MatrixBase< Derived > &V) noexcept
- template<typename Derived>
bool [qpp::internal::_check_qubit_vector](#) (const Eigen::MatrixBase< Derived > &V) noexcept
- bool [qpp::internal::_check_perm](#) (const std::vector< idx > &perm)
- template<typename Derived1, typename Derived2>
dyn_mat< typename Derived1::Scalar > [qpp::internal::_kron2](#) (const Eigen::MatrixBase< Derived1 > &A,
const Eigen::MatrixBase< Derived2 > &B)
- template<typename Derived1, typename Derived2>
dyn_mat< typename Derived1::Scalar > [qpp::internal::_dirsum2](#) (const Eigen::MatrixBase< Derived1 > &A,
const Eigen::MatrixBase< Derived2 > &B)
- template<typename T>
void [qpp::internal::variadic_vector_emplace](#) (std::vector< T > &)
- template<typename T, typename First, typename... Args>
void [qpp::internal::variadic_vector_emplace](#) (std::vector< T > &v, First &&first, Args &&...args)

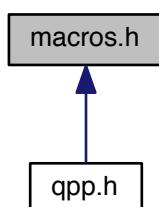
8.18.1 Detailed Description

Internal utility functions.

8.19 macros.h File Reference

Preprocessor macros.

This graph shows which files directly or indirectly include this file:



Macros

- #define [PRINT\(x\)](#)
- #define [PRINTLN\(x\)](#)

- `#define ERROR(x)`
- `#define ERRORLN(x)`

8.19.1 Detailed Description

Preprocessor macros.

8.19.2 Macro Definition Documentation

8.19.2.1 `#define ERROR(x)`

Prints an error message to std::cerr

8.19.2.2 `#define ERRORLN(x)`

Prints an error message to std::cerr and adds a new line

8.19.2.3 `#define PRINT(x)`

Prints a message

8.19.2.4 `#define PRINTLN(x)`

Prints a message and adds a new line

8.20 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

Namespaces

- `qpp`

Quantum++ main namespace.

Functions

- template<typename Derived >
 Derived `qpp::loadMATLABmatrix` (const std::string &mat_file, const std::string &var_name)
 Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.
- template<>
 dmat `qpp::loadMATLABmatrix` (const std::string &mat_file, const std::string &var_name)
 Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (`qpp::dmat`)
- template<>
 cmat `qpp::loadMATLABmatrix` (const std::string &mat_file, const std::string &var_name)
 Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (`qpp::cmat`)

- template<typename Derived>
`void qpp::saveMATLABmatrix` (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.
- template<>
`void qpp::saveMATLABmatrix` (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
- template<>
`void qpp::saveMATLABmatrix` (const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

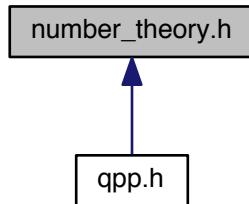
8.20.1 Detailed Description

Input/output interfacing with MATLAB.

8.21 number_theory.h File Reference

Number theory functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `std::vector< int > qpp::x2contfrac` (double x, idx n, idx cut=1e5)
Simple continued fraction expansion.
- `double qpp::contfrac2x` (const std::vector< int > &cf, idx n)
Real representation of a simple continued fraction.
- `double qpp::contfrac2x` (const std::vector< int > &cf)
Real representation of a simple continued fraction.
- `ubigint qpp::gcd` (ubigint m, ubigint n)

Greatest common divisor of two non-negative integers.

- ubigint [qpp::gcd](#) (const std::vector< ubigint > &ns)

Greatest common divisor of a list of non-negative integers.

- ubigint [qpp::lcm](#) (ubigint m, ubigint n)

Least common multiple of two positive integers.

- ubigint [qpp::lcm](#) (const std::vector< ubigint > &ns)

Least common multiple of a list of positive integers.

- std::vector< idx > [qpp::invperm](#) (const std::vector< idx > &perm)

Inverse permutation.

- std::vector< idx > [qpp::compperm](#) (const std::vector< idx > &perm, const std::vector< idx > &sigma)

Compose permutations.

- std::vector< ubigint > [qpp::factors](#) (ubigint n)

Prime factor decomposition.

- bool [qpp::isprime](#) (ubigint n)

Primality test.

- ubigint [qpp::modpow](#) (ubigint a, ubigint n, ubigint p)

Integer power modulo p.

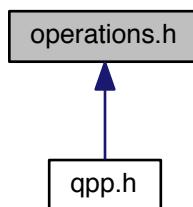
8.21.1 Detailed Description

Number theory functions.

8.22 operations.h File Reference

Quantum operation functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)`

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
`dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)`

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived >
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`

Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.
- template<typename Derived >
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- template<typename Derived >
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`

Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- cmat `qpp::kraus2super` (const std::vector< cmat > &Ks)

Superoperator matrix.
- cmat `qpp::kraus2choi` (const std::vector< cmat > &Ks)

Choi matrix.
- std::vector< cmat > `qpp::choi2kraus` (const cmat &A)

Orthogonal Kraus operators from Choi matrix.
- cmat `qpp::choi2super` (const cmat &A)

Converts Choi matrix to superoperator matrix.
- cmat `qpp::super2choi` (const cmat &A)

Converts superoperator matrix to Choi matrix.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

Partial trace.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

Partial trace.
- template<typename Derived >
`dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Partial trace.

- template<typename Derived >
dyn_mat< typename Derived::Scalar > **qpp::ptrace** (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

Partial trace.

- template<typename Derived >
dyn_mat< typename Derived::Scalar > **qpp::ptranspose** (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Partial transpose.

- template<typename Derived >
dyn_mat< typename Derived::Scalar > **qpp::ptranspose** (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

Partial transpose.

- template<typename Derived >
dyn_mat< typename Derived::Scalar > **qpp::syspermute** (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)

Subsystem permutation.

- template<typename Derived >
dyn_mat< typename Derived::Scalar > **qpp::syspermute** (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)

Subsystem permutation.

8.22.1 Detailed Description

Quantum operation functions.

8.23 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```
#include <algorithm>
#include <cassert>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <ctime>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <limits>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "macros.h"
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/idisplay.h"
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/init.h"
#include "functions.h"
#include "classes/codes.h"
#include "classes/gates.h"
#include "classes/states.h"
#include "classes/random_devices.h"
#include "statistics.h"
#include "operations.h"
#include "entropies.h"
#include "entanglement.h"
#include "random.h"
#include "classes/timer.h"
#include "instruments.h"
#include "number_theory.h"
```

Namespaces

- [qpp](#)

Quantum++ main namespace.

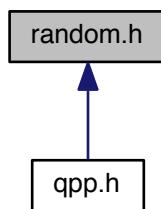
8.23.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

8.24 random.h File Reference

Randomness-related functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- [double qpp::rand \(double a=0, double b=1\)](#)
Generates a random real number uniformly distributed in the interval [a, b]
- [bigint qpp::rand \(bigint a=std::numeric_limits< bigint >::min\(\), bigint b=std::numeric_limits< bigint >::max\(\)\)](#)
Generates a random big integer uniformly distributed in the interval [a, b].
- [ubigint qpp::rand \(ubigint a=std::numeric_limits< ubigint >::min\(\), ubigint b=std::numeric_limits< ubigint >::max\(\)\)](#)
Generates a random non-negative big integer uniformly distributed in the interval [a, b].
- [idx qpp::randidx \(idx a=std::numeric_limits< idx >::min\(\), idx b=std::numeric_limits< idx >::max\(\)\)](#)
Generates a random index (idx) uniformly distributed in the interval [a, b].
- [template<typename Derived > Derived qpp::rand \(idx rows, idx cols, double a=0, double b=1\)](#)
Generates a random matrix with entries uniformly distributed in the interval [a, b]
- [template<> dmat qpp::rand \(idx rows, idx cols, double a, double b\)](#)
Generates a random real matrix with entries uniformly distributed in the interval [a, b], specialization for double matrices (qpp::dmat)
- [template<> cmat qpp::rand \(idx rows, idx cols, double a, double b\)](#)

- Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (`qpp::cmat`)*
- template<typename Derived>
Derived `qpp::randn` (idx rows, idx cols, double mean=0, double sigma=1)
Generates a random matrix with entries normally distributed in N(mean, sigma)
 - template<>
dmat `qpp::randn` (idx rows, idx cols, double mean, double sigma)
Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (`qpp::dmat`)
 - template<>
cmat `qpp::randn` (idx rows, idx cols, double mean, double sigma)
Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (`qpp::cmat`)
 - double `qpp::randn` (double mean=0, double sigma=1)
Generates a random real number (double) normally distributed in N(mean, sigma)
 - cmat `qpp::randU` (idx D)
Generates a random unitary matrix.
 - cmat `qpp::randV` (idx Din, idx Dout)
Generates a random isometry matrix.
 - std::vector< cmat > `qpp::randkraus` (idx N, idx D)
Generates a set of random Kraus operators.
 - cmat `qpp::randH` (idx D)
Generates a random Hermitian matrix.
 - ket `qpp::randket` (idx D)
Generates a random normalized ket (pure state vector)
 - cmat `qpp::randrho` (idx D)
Generates a random density matrix.
 - std::vector< idx > `qpp::randperm` (idx n)
Generates a random uniformly distributed permutation.

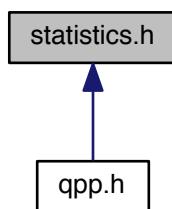
8.24.1 Detailed Description

Randomness-related functions.

8.25 statistics.h File Reference

Statistics functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Quantum++ main namespace.

Functions

- `std::vector< double > qpp::uniform (idx N)`
Uniform probability distribution vector.
- `std::vector< double > qpp::marginalX (const dmat &probXY)`
Marginal distribution.
- `std::vector< double > qpp::marginalY (const dmat &probXY)`
Marginal distribution.
- template<typename Container >
`double qpp::avg (const std::vector< double > &prob, const Container &X)`
Average.
- template<typename Container >
`double qpp::cov (const dmat &probXY, const Container &X, const Container &Y)`
Covariance.
- template<typename Container >
`double qpp::var (const std::vector< double > &prob, const Container &X)`
Variance.
- template<typename Container >
`double qpp::sigma (const std::vector< double > &prob, const Container &X)`
Standard deviation.
- template<typename Container >
`double qpp::cor (const dmat &probXY, const Container &X, const Container &Y)`
Correlation.

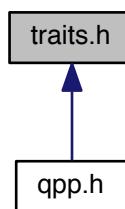
8.25.1 Detailed Description

Statistics functions.

8.26 traits.h File Reference

Type traits.

This graph shows which files directly or indirectly include this file:



Classes

- struct `qpp::is_iterable< T, typename >`
Checks whether `T` is compatible with an STL-like iterable container.
- struct `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type >`
Checks whether `T` is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct `qpp::is_matrix_expression< Derived >`
Checks whether the type is an Eigen matrix expression.
- struct `qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >`
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.
- struct `qpp::is_complex< T >`
Checks whether the type is a complex type.
- struct `qpp::is_complex< std::complex< T > >`
Checks whether the type is a complex number type, specialization for complex types.

Namespaces

- `qpp`
Quantum++ main namespace.

Typedefs

- template<typename... >
`using qpp::to_void = void`
Alias template that implements the proposal for void_t.

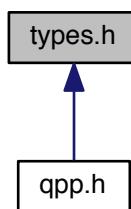
8.26.1 Detailed Description

Type traits.

8.27 types.h File Reference

Type aliases.

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Quantum++ main namespace.

Typedefs

- using `qpp::idx` = `std::size_t`
Non-negative integer index.
- using `qpp::bigint` = `long long int`
Big integer.
- using `qpp::ubigint` = `unsigned long long int`
Non-negative big integer.
- using `qpp::cplx` = `std::complex< double >`
Complex number in double precision.
- using `qpp::ket` = `Eigen::VectorXcd`
Complex (double precision) dynamic Eigen column vector.
- using `qpp::bra` = `Eigen::RowVectorXcd`
Complex (double precision) dynamic Eigen row vector.
- using `qpp::cmat` = `Eigen::MatrixXcd`
Complex (double precision) dynamic Eigen matrix.
- using `qpp::dmat` = `Eigen::MatrixXd`
Real (double precision) dynamic Eigen matrix.
- template<typename Scalar>
using `qpp::dyn_mat` = `Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >`
Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar>
using `qpp::dyn_col_vect` = `Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >`
Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar>
using `qpp::dyn_row_vect` = `Eigen::Matrix< Scalar, 1, Eigen::Dynamic >`
Dynamic Eigen row vector over the field specified by Scalar.

8.27.1 Detailed Description

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